

Feedback:

The simple and best solution.

Applications to self-optimizing control and stabilization of new operating regimes

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Abstract

- Feedback: The simple and best solution
- Applications to self-optimizing control and stabilization of new operating regimes
- Sigurd Skogestad, NTNU, Trondheim, Norway
- Most chemical engineers are (indirectly) trained to be “feedforward thinkers” and they immediately think of “model inversion” when it comes doing control. Thus, they prefer to rely on models instead of data, although simple feedback solutions in many cases are much simpler and certainly more robust.

The seminar starts with a simple comparison of feedback and feedforward control and their sensitivity to uncertainty. Then two nice applications of feedback are considered:

1. Implementation of optimal operation by "self-optimizing control".

The idea is to turn optimization into a setpoint control problem, and the trick is to find the right variable to control. Applications include process control, pizza baking, marathon running, biology and the central bank of a country.

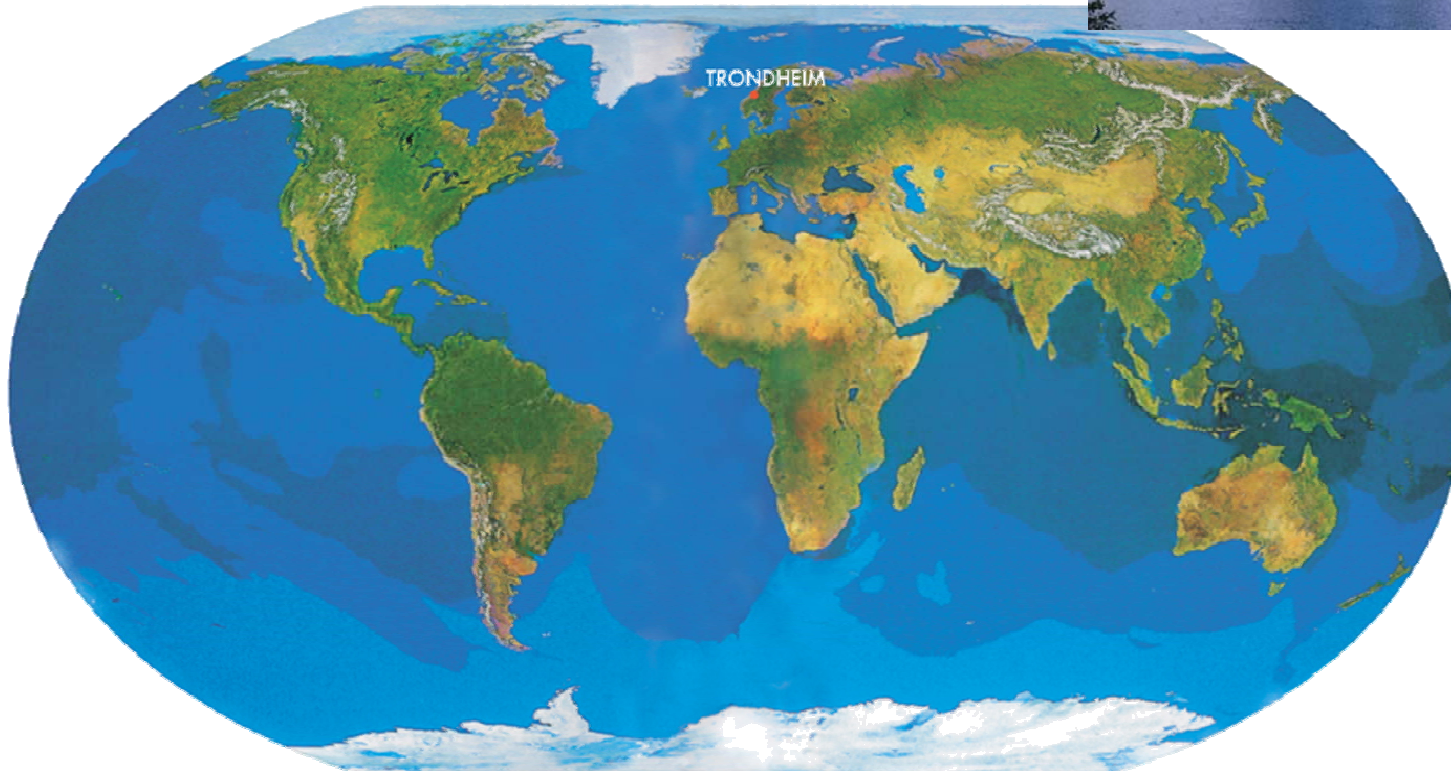
2. Stabilization of desired operating regimes.

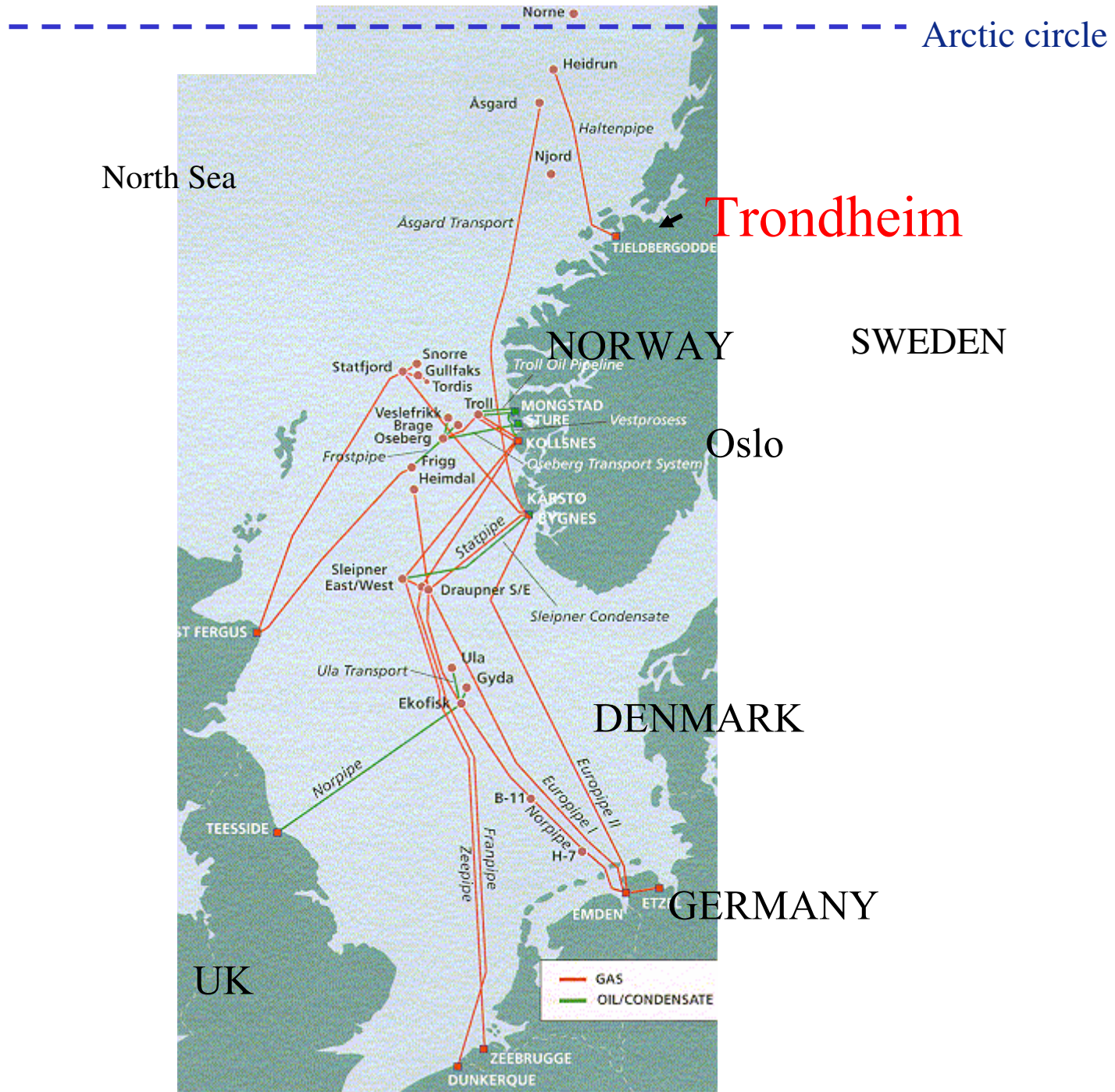
Here feedback control can lead to completely new and simple solutions. One example would be stabilization of laminar flow at conditions where we normally have turbulent flow. In the seminar a nice application to anti-slug control in multiphase pipeline flow is discussed.

Outline

- **About Trondheim**
 - I. Why feedback (and not feedforward) ?
 - II. Self-optimizing feedback control: What should we control?
 - III. Stabilizing feedback control: Anti-slug control
 - Conclusion
-
- More information:

Trondheim, Norway







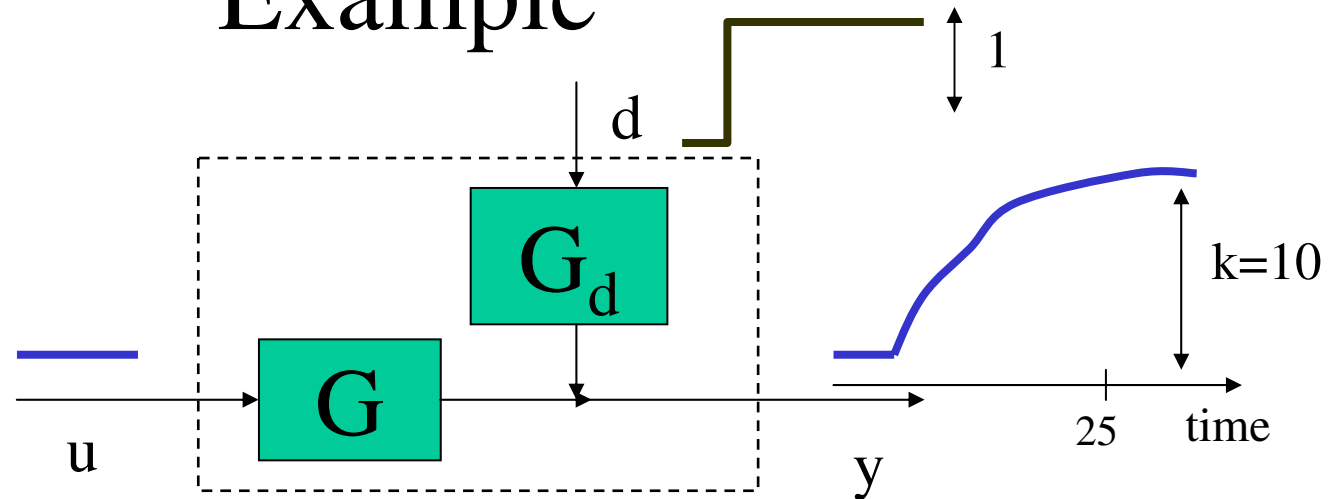
NTNU, Trondheim



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Example



Plant (uncontrolled system)

State space:

- $\frac{dx_1}{dt} = -\frac{1}{\tau}x_1(t) + k \cdot u(t - \theta), \quad \frac{dx_2}{dt} = -0.1x_2(t) + 10 \cdot d(t)$
- $y(t) = x_1(t) + x_2(t)$

Laplace:

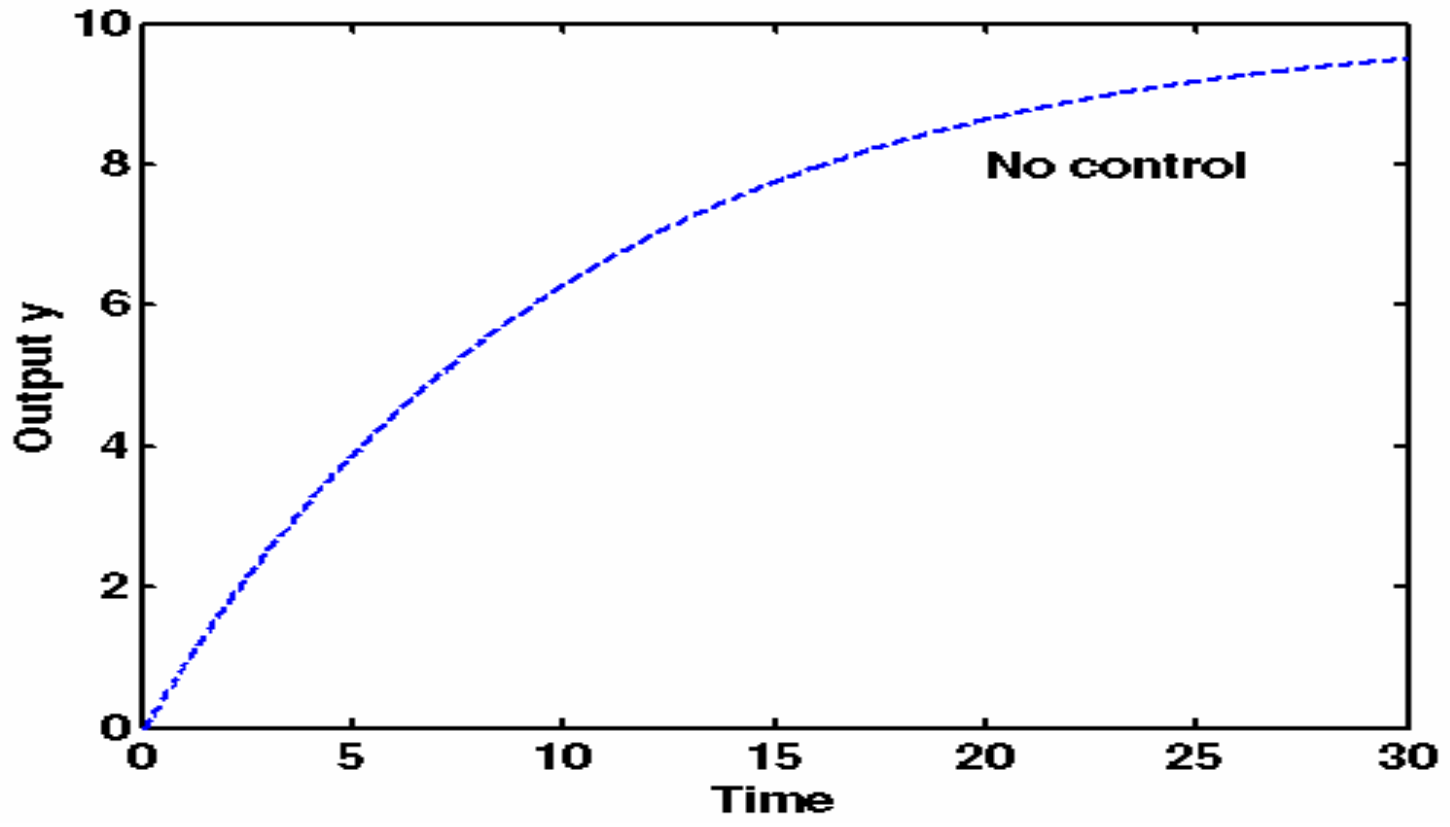
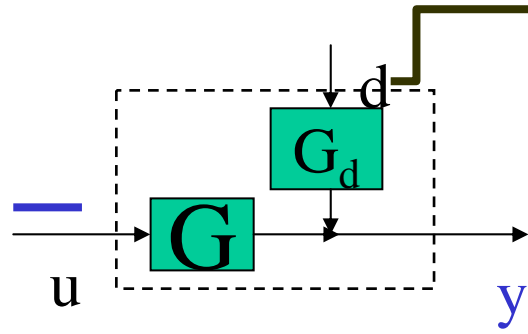
- $G(s) = \frac{k}{\tau s + 1} e^{-\theta s}, \quad G_d(s) = \frac{10}{10s + 1}$

Nominal parameters ($G = G_d$):

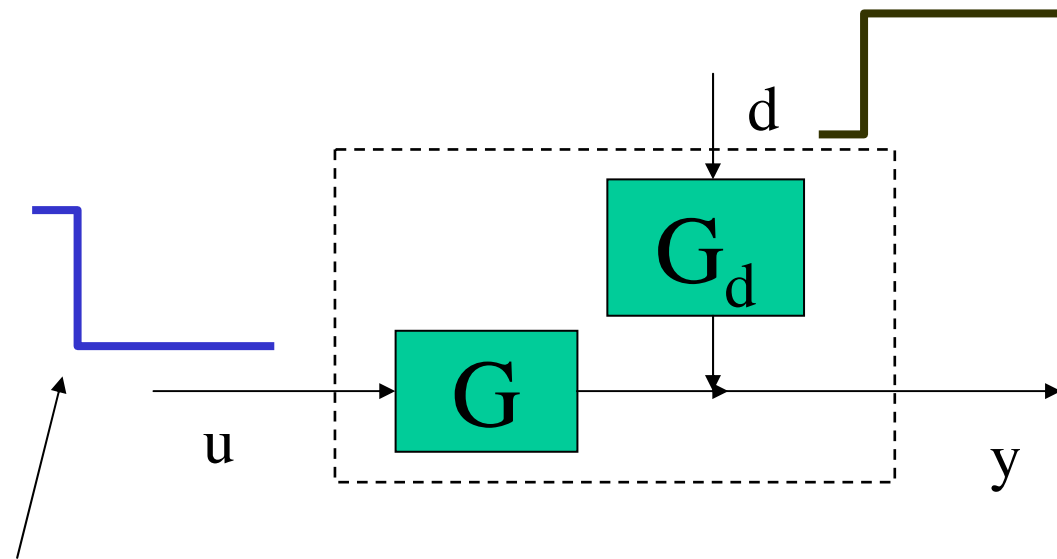
- $k = 10; \quad \tau = 10[s]; \quad \theta = 0$

Consider feedforward and feedback control:

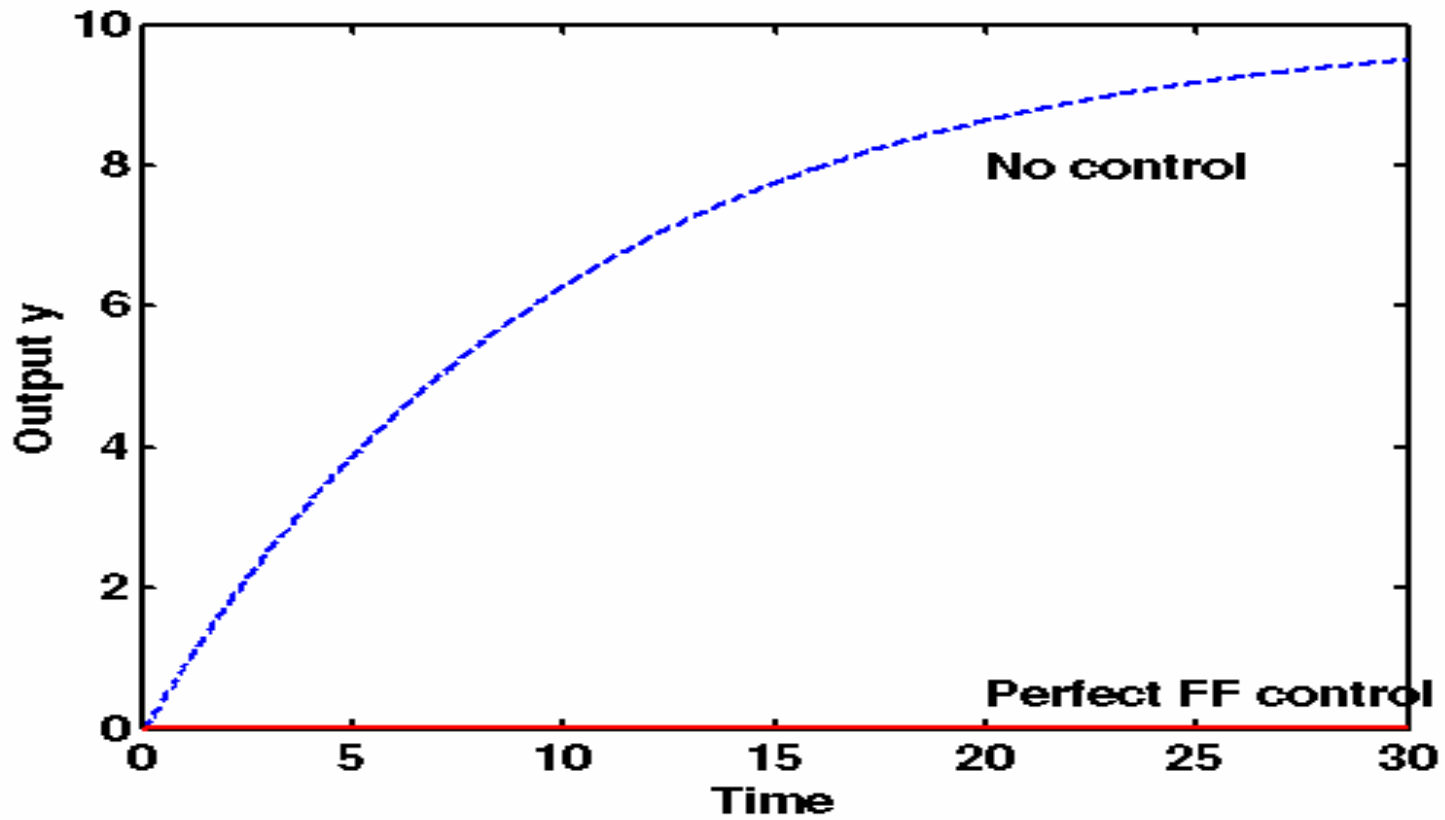
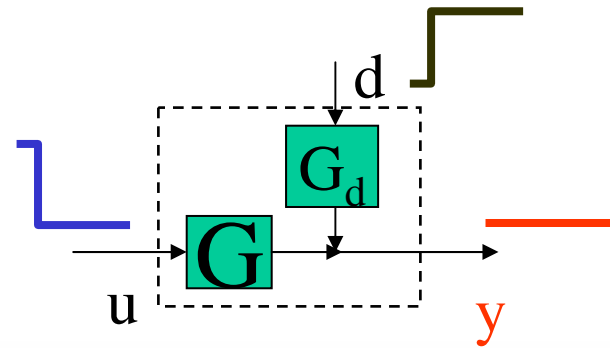
- with changes in G : gain (k), time constant (τ) and input delay (θ)

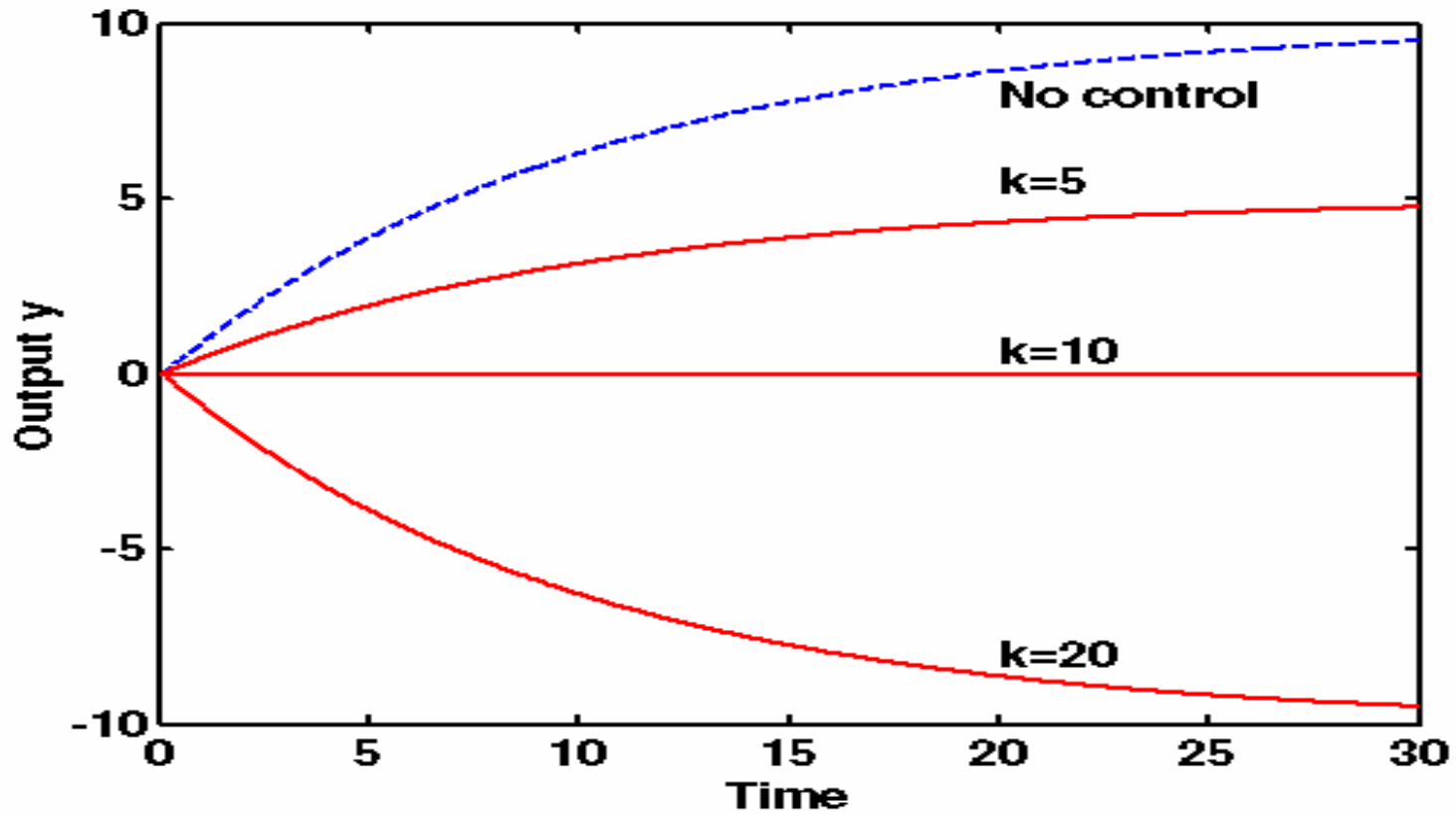
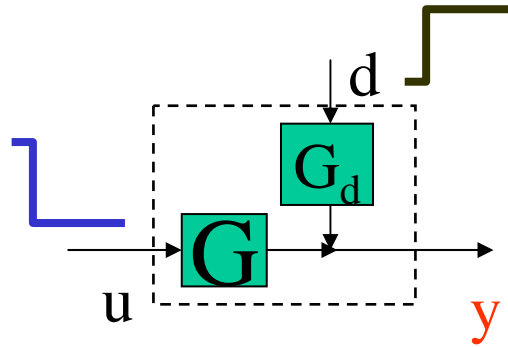


Model-based control = Feedforward (FF) control

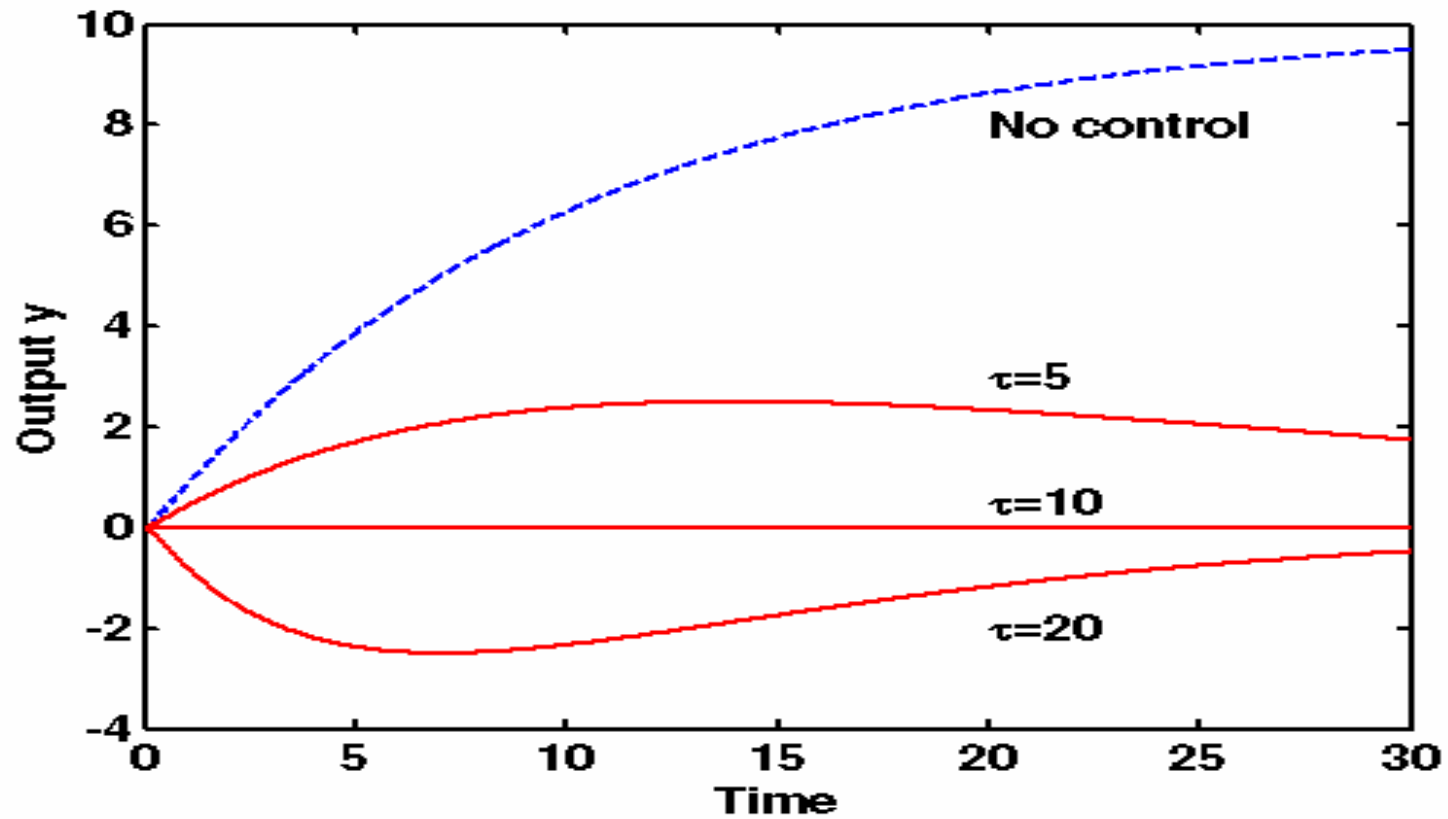
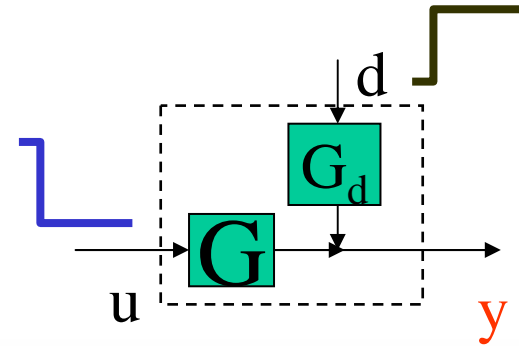


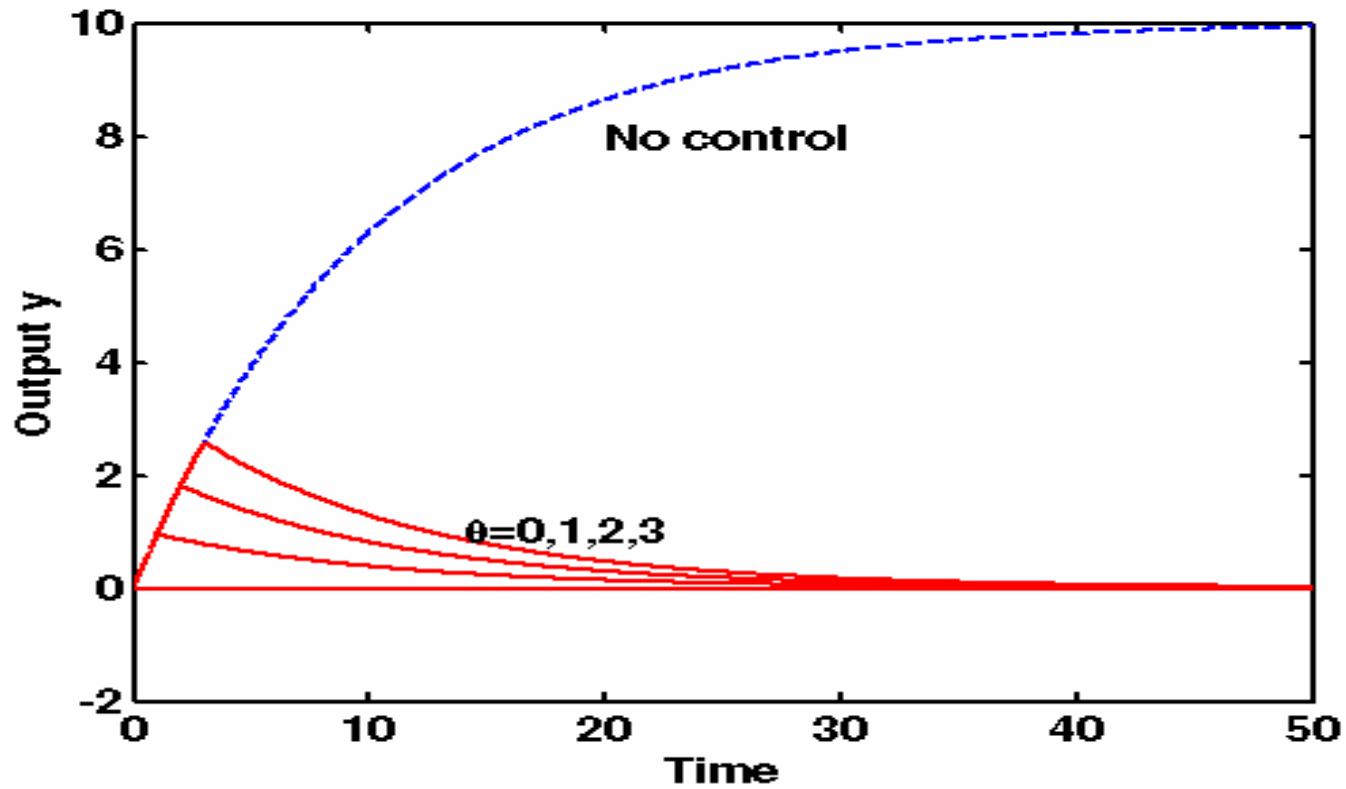
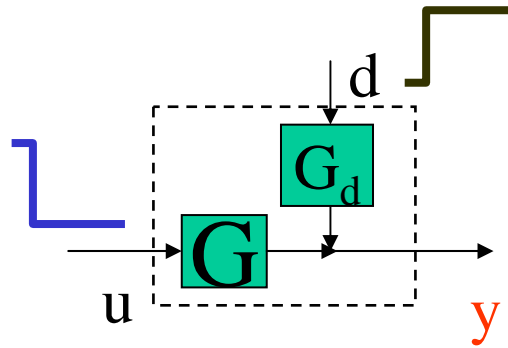
”Perfect” feedforward control: $u = - G^{-1} G_d d$
 Our case: $G=G_d \rightarrow$ Use $u = -d$





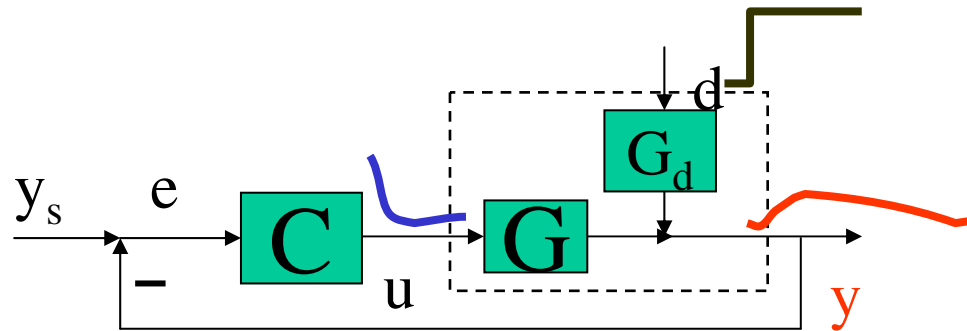
Feedforward: sensitive to gain error





Feedforward: Moderate sensitive to delay
(in G or G_d)

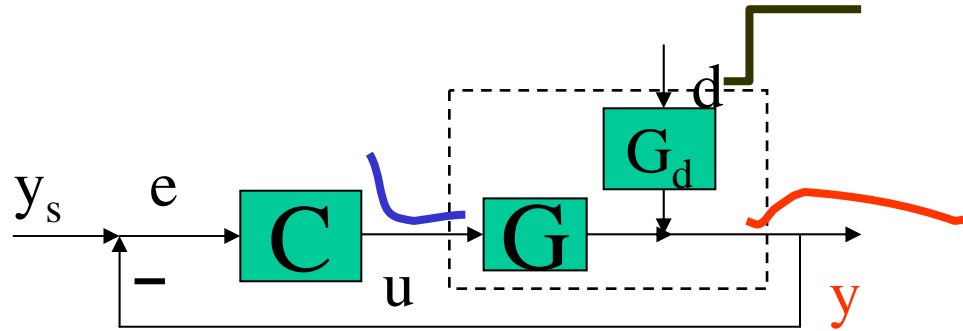
Measurement-based correction = Feedback (FB) control



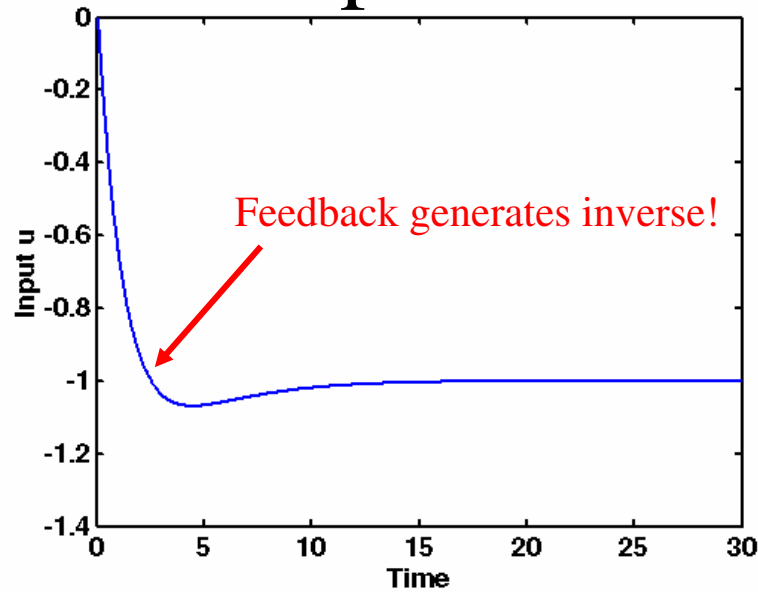
- Most common in industry: $C = \text{PID controller}$.
Two adjustable tuning parameters: K_c and τ_I
- Exists many tuning rules including Skogestad's (SIMC) tuning rules
 $K_c = \frac{1}{k} \cdot \frac{\tau}{\tau_c + \theta}$; $\tau_I = \min\{\tau, 4(\tau_c + \theta)\}$

“Probably the best simple PID tuning rules in the world”

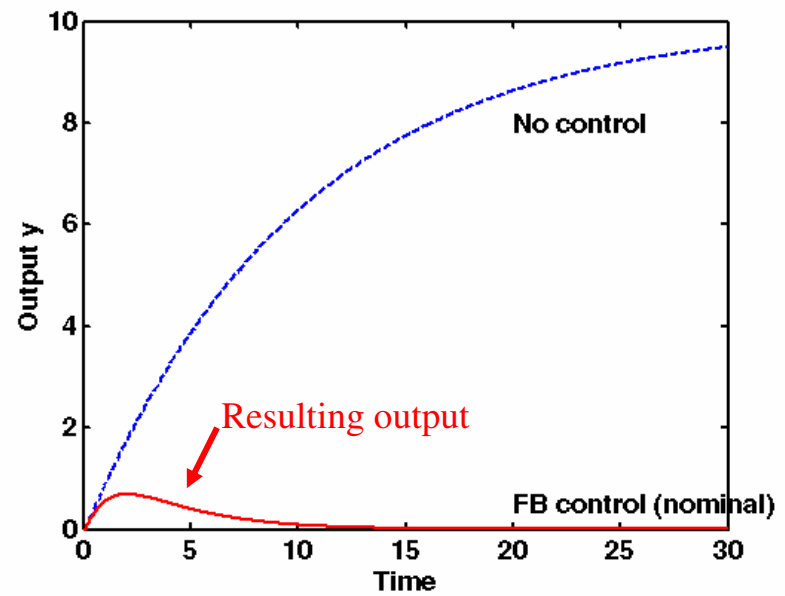
- Example ($k = 10$, $\tau = 10$, $\theta = 0$ and $\tau_c = 1$):
 $K_c = \frac{1}{10} \cdot \frac{10}{1} = 1$ $\tau_I = \min\{10, 4 \cdot 1\} = 4$ [s]



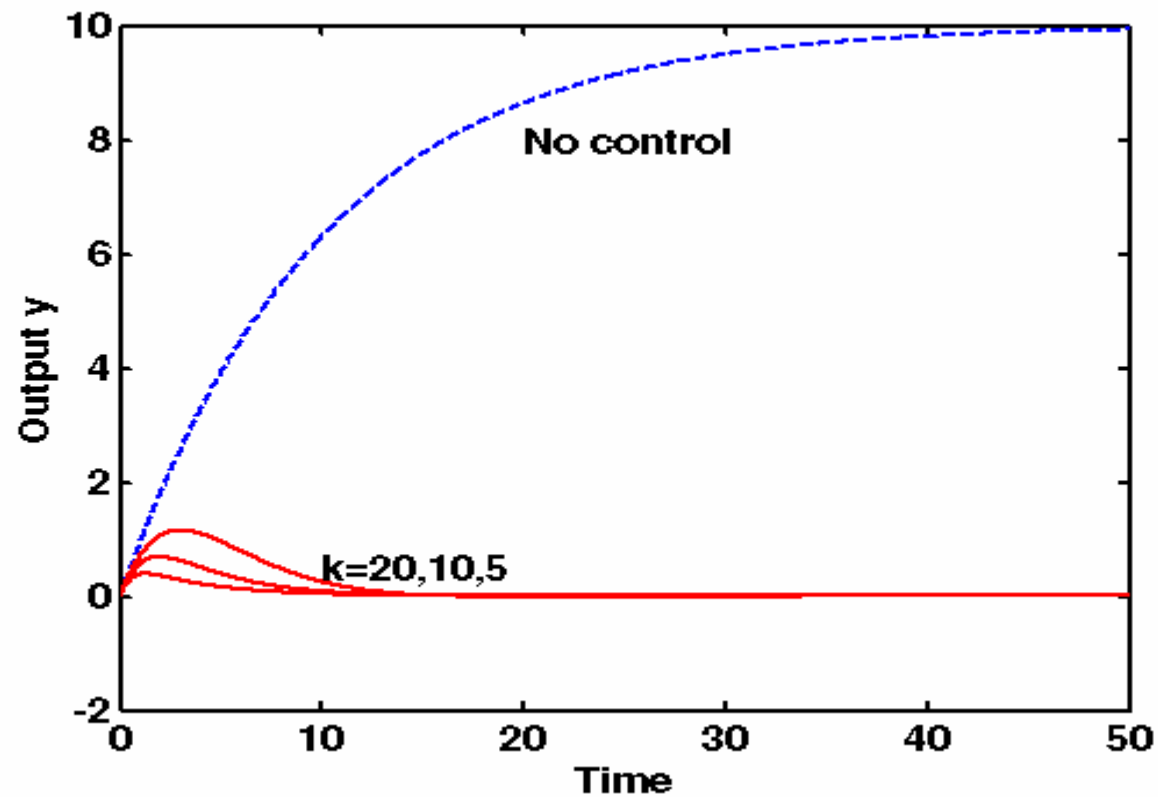
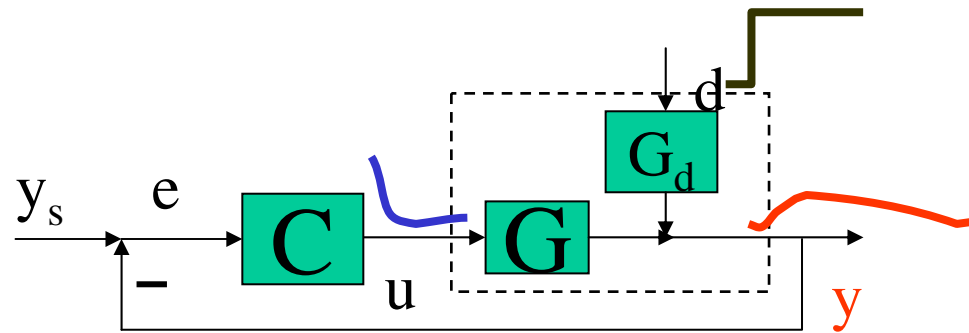
Input u

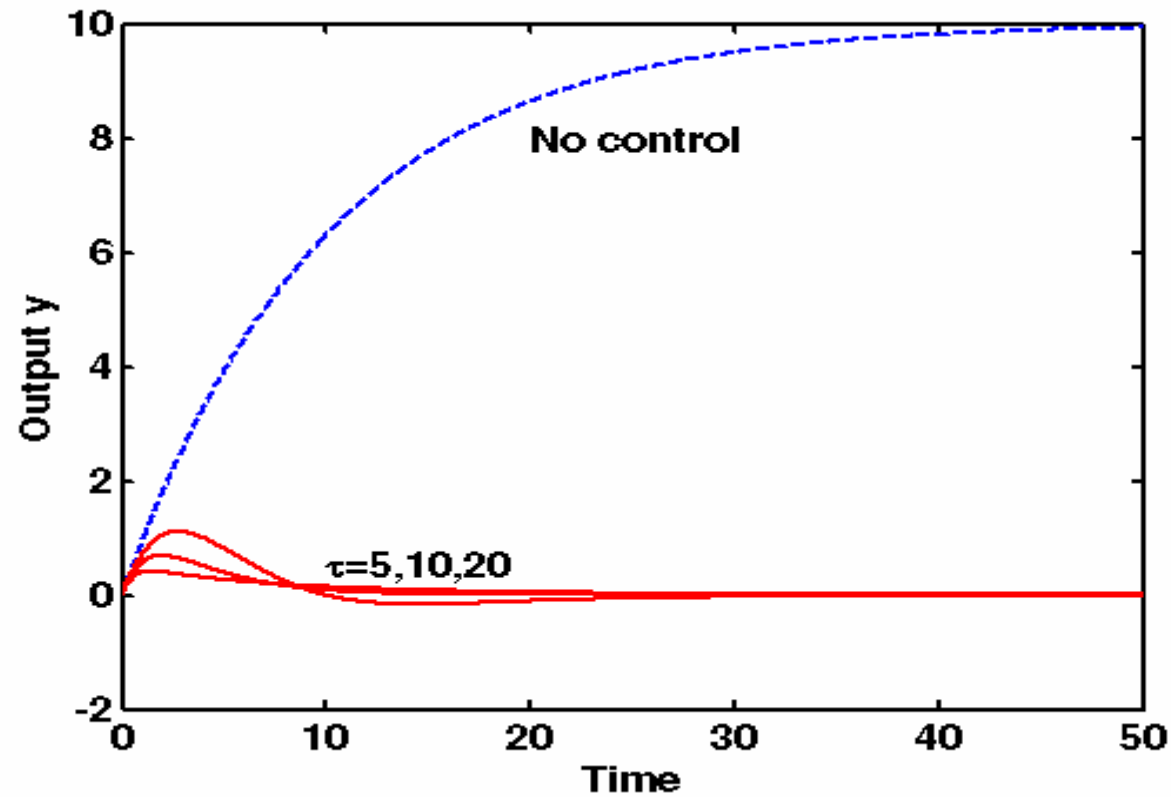
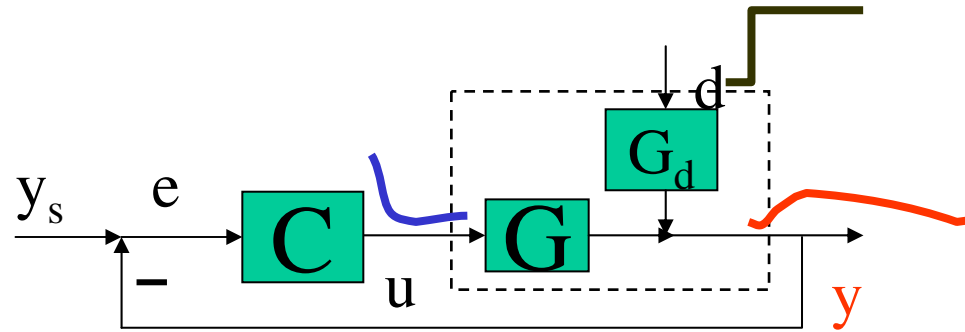


Output y

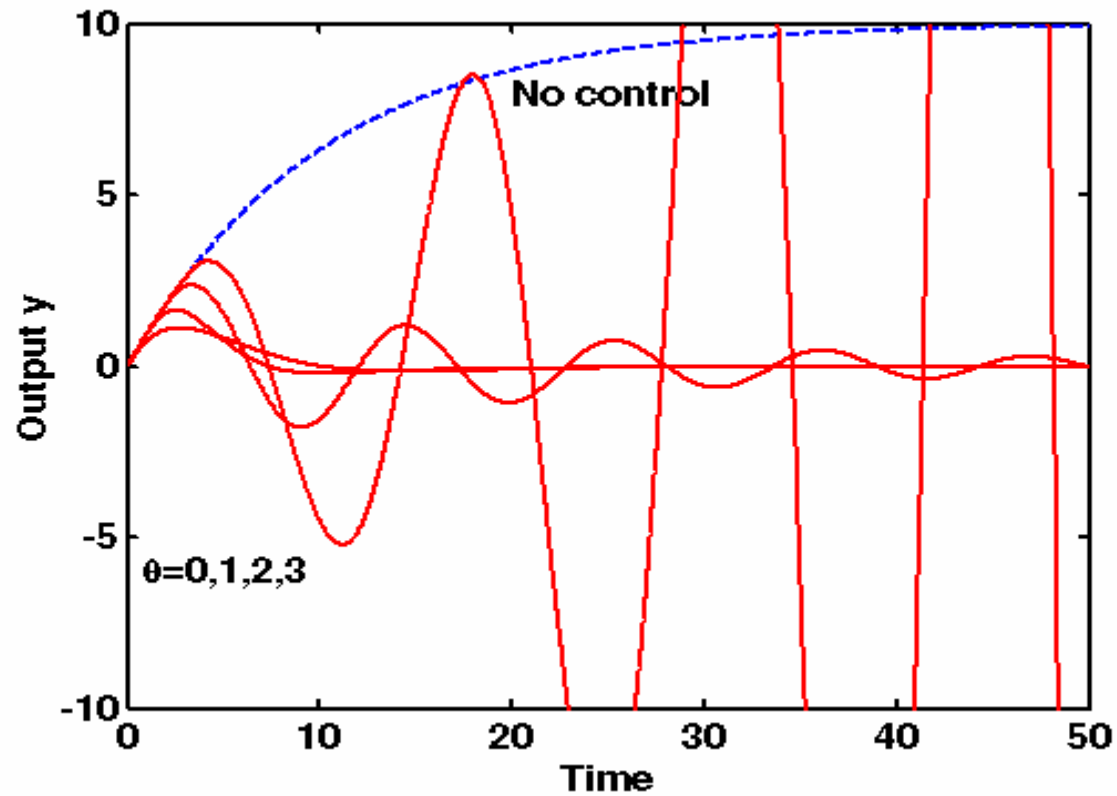
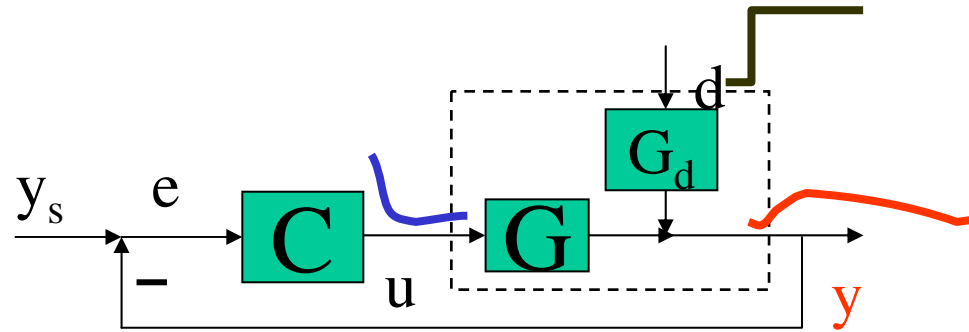


Feedback PI-control: Nominal case





Feedback: insensitive to time constant error



Feedback control: sensitive to time delay

Comment

- Time delay error in disturbance model (G_d): No effect (!) with feedback (except time shift)
- Feedforward: Similar effect as time delay error in G

Conclusion: Why feedback? (and not feedforward control)

- Simple: High gain feedback!
- Counteract unmeasured disturbances
- Reduce effect of changes / uncertainty (robustness)
- Change system dynamics (including stabilization)
- Linearize the behavior
- No explicit model required

- MAIN PROBLEM
- Potential instability (may occur “suddenly”) with time delay/RHP-zero

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Optimal operation (economics)

- Define scalar cost function $J(u_0, d)$
 - u_0 : degrees of freedom
 - d : disturbances
- Optimal operation for given d :

$$\min_{u_0} J(u_0, x, d)$$

subject to:

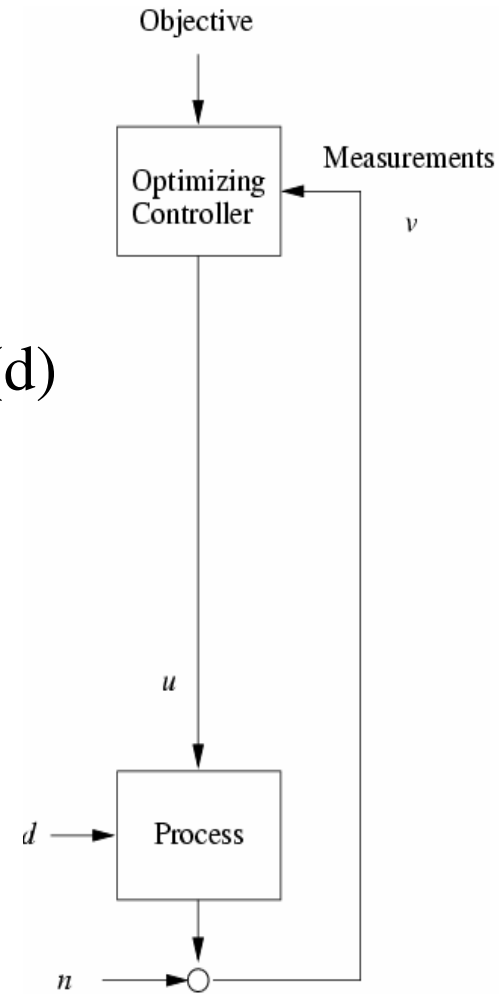
$$f(u_0, x, d) = 0$$

$$g(u_0, x, d) < 0$$

”Obvious” solution:
 Optimizing control =
 ”Feedforward”

Estimate d and compute new $u_{opt}(d)$

Problem: Complicated and sensitive to uncertainty



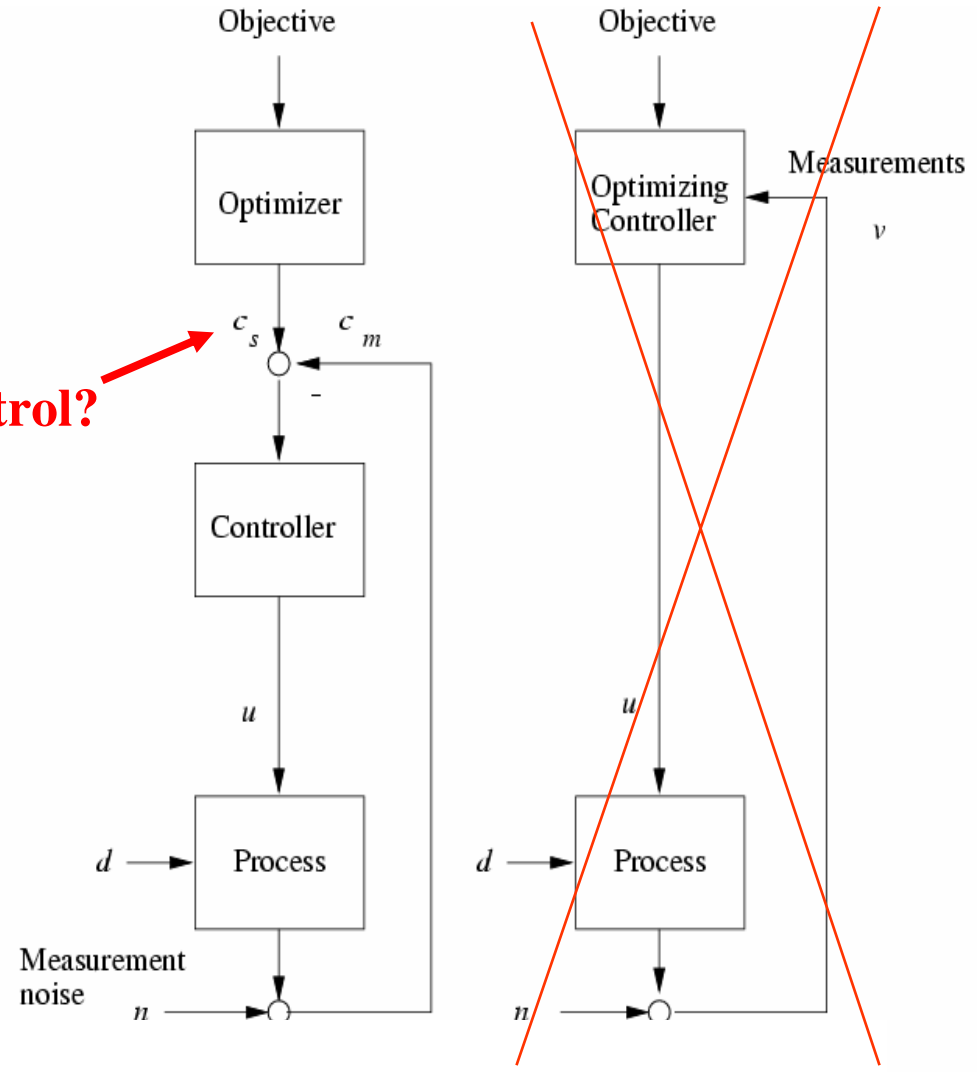
Engineering systems

- Most (all?) large-scale engineering systems are controlled using hierarchies of quite simple single-loop controllers
 - Commercial aircraft
 - Large-scale chemical plant (refinery)
- 1000's of loops
- Simple components:
 - on-off + P-control + PI-control + nonlinear fixes + some feedforward

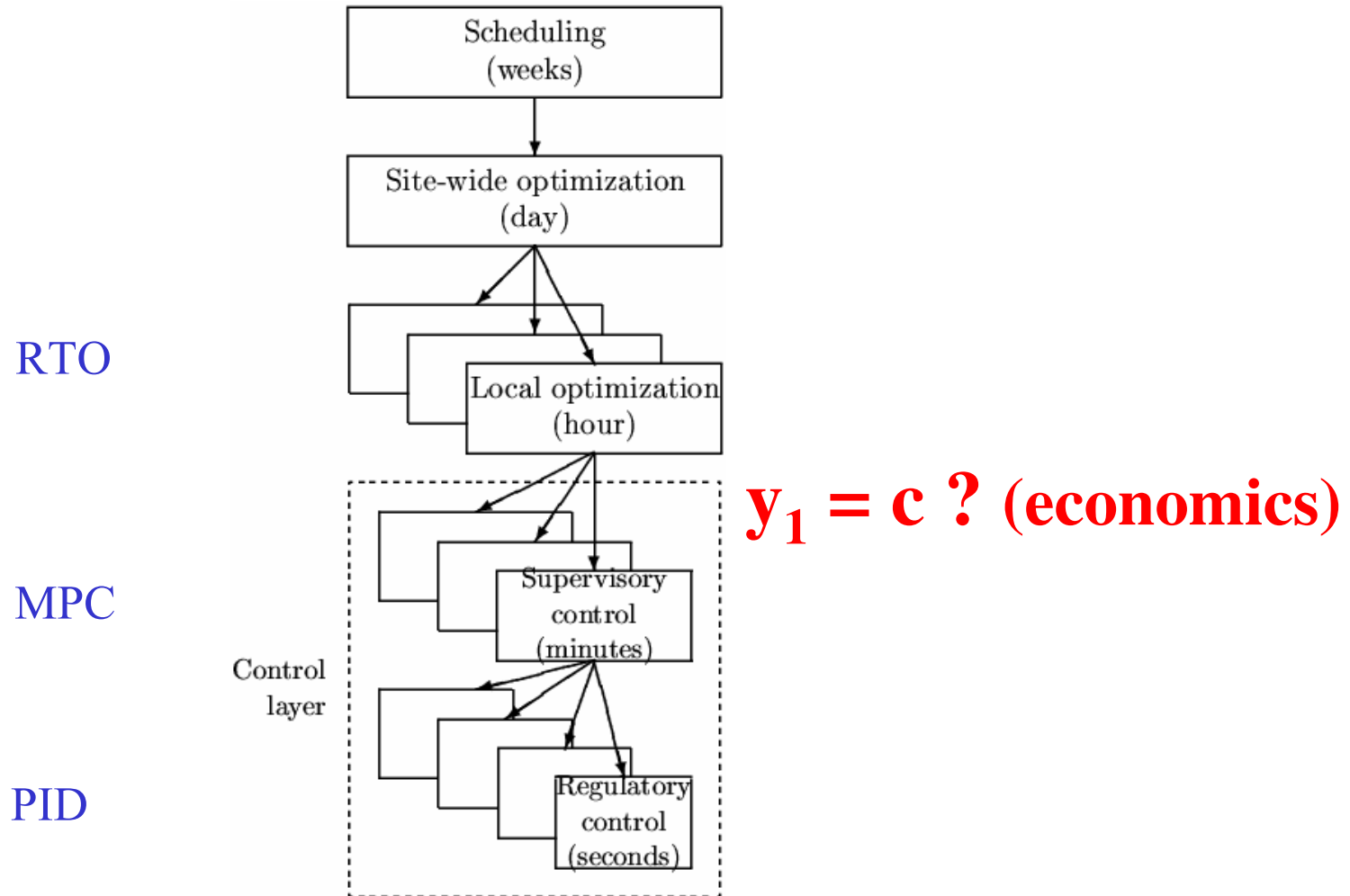
Same in biological systems

In Practice: Feedback implementation

Issue:
What should we control?



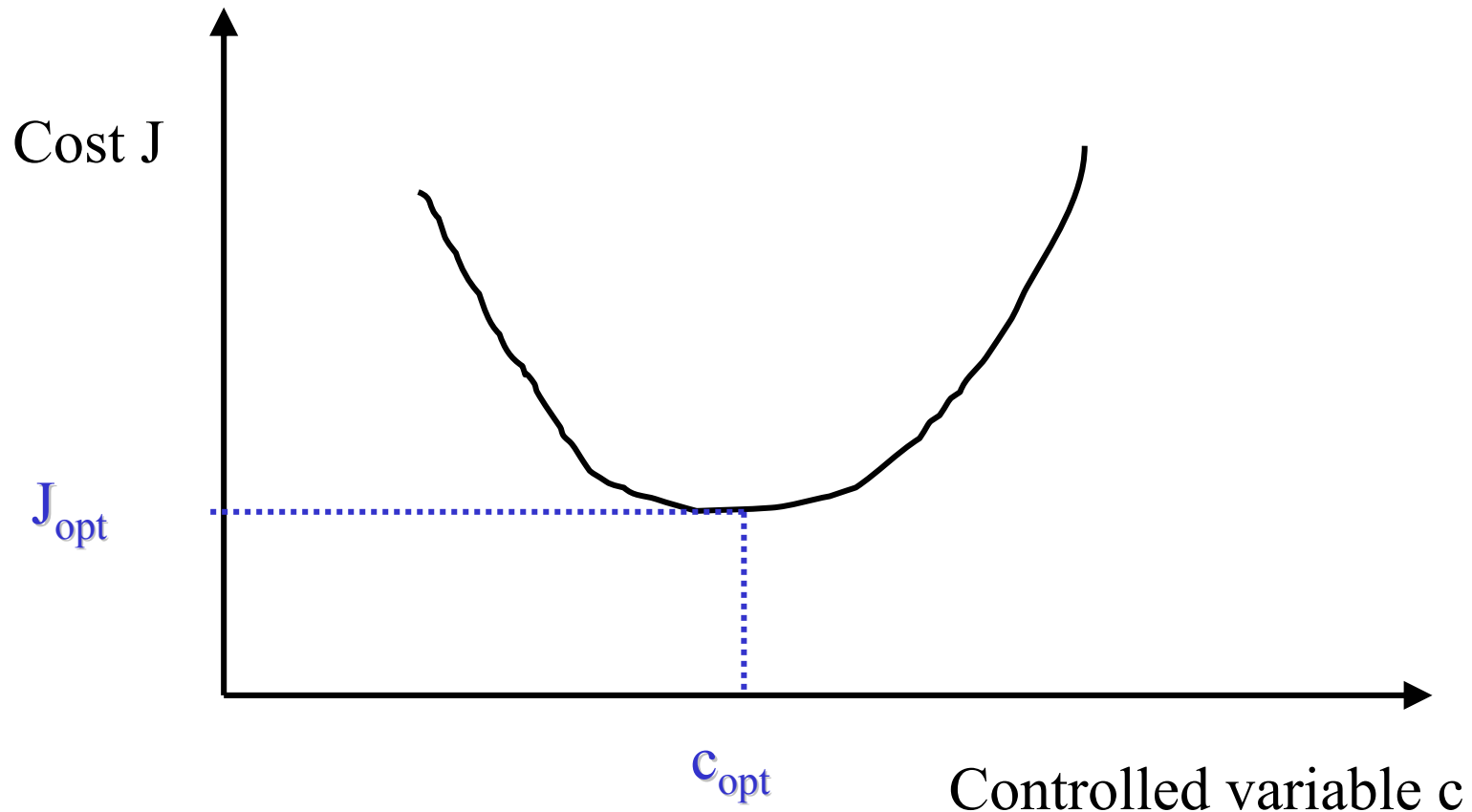
Further layers: Process control hierarchy



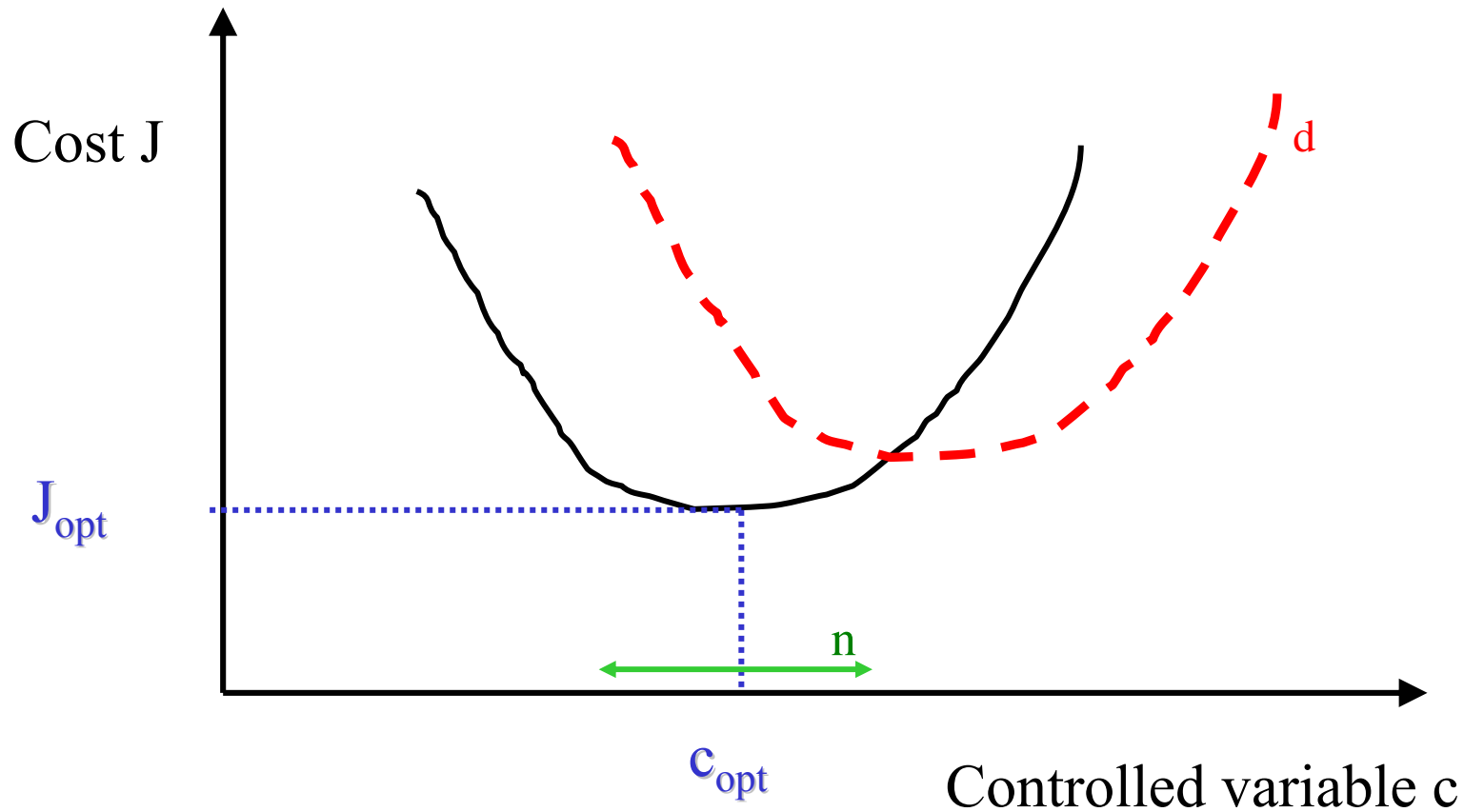
Implementation of optimal operation

- Optimal solution is usually at constraints, that is, most of the degrees of freedom are used to satisfy “active constraints”, $g(u_0, d) = 0$
- **CONTROL ACTIVE CONSTRAINTS!**
 - Implementation of active constraints is usually simple.
- **WHAT MORE SHOULD WE CONTROL?**
 - We here concentrate on the **remaining unconstrained degrees of freedom.**

Optimal operation



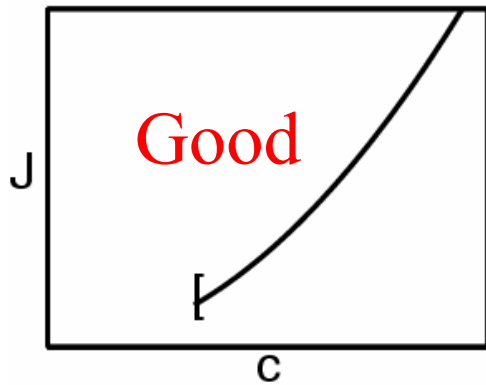
Optimal operation



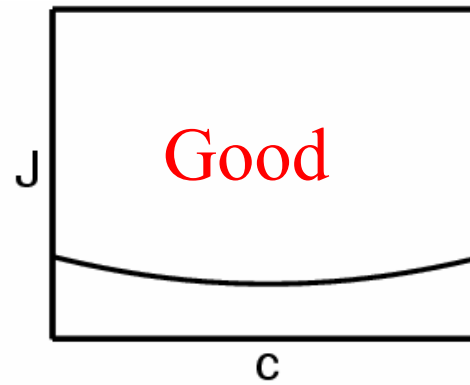
Two problems:

- 1. Optimum moves because of **disturbances d**: $c_{opt}(d)$
- 2. Implementation error, $c = c_{opt} + n$

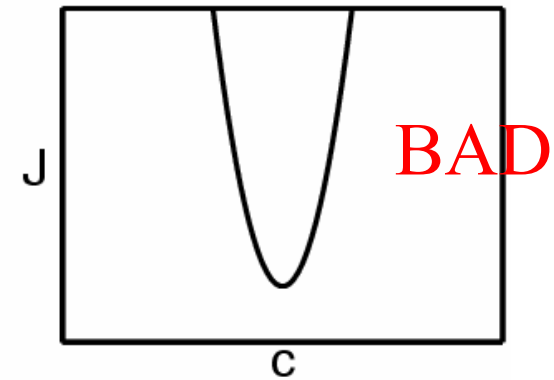
Effect of implementation error



(a) Active constraint control: Implementation easy



(b) Flat optimum: Implementation easy



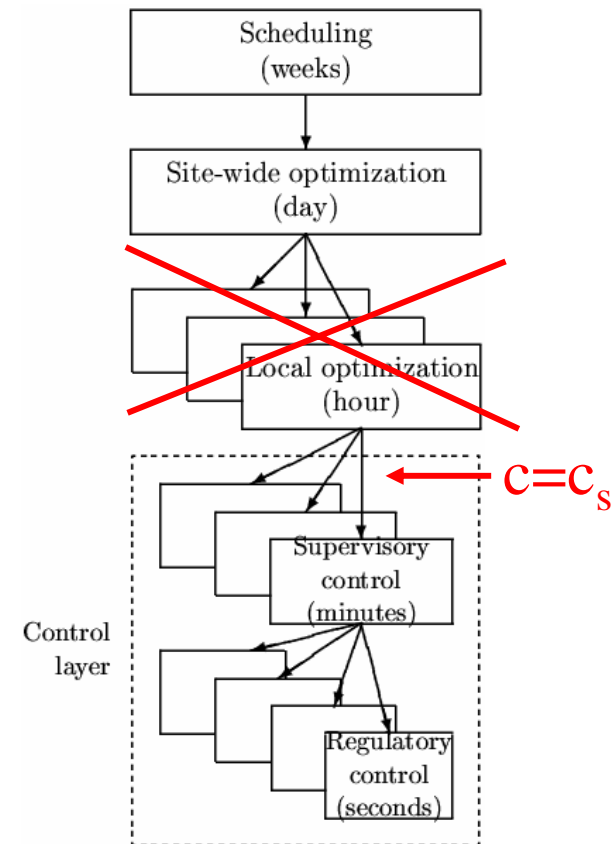
(c) Sharp optimum: Sensitive to implementation errors

Self-optimizing Control

- Define loss:

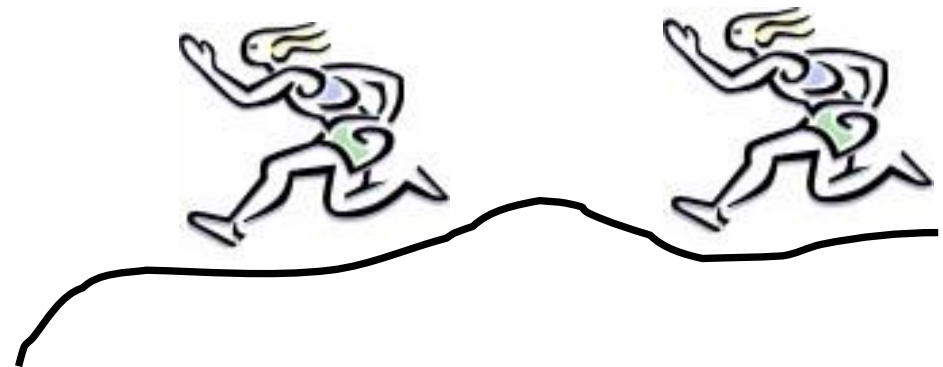
$$L(u, d) = J(c_s + n, d) - J_{opt}(d)$$

- Self-optimizing Control
 - Self-optimizing control is when *acceptable operation* (=acceptable loss) can be achieved using *constant set points* (c_s) for the controlled variables c (without the need for re-optimizing when disturbances occur).



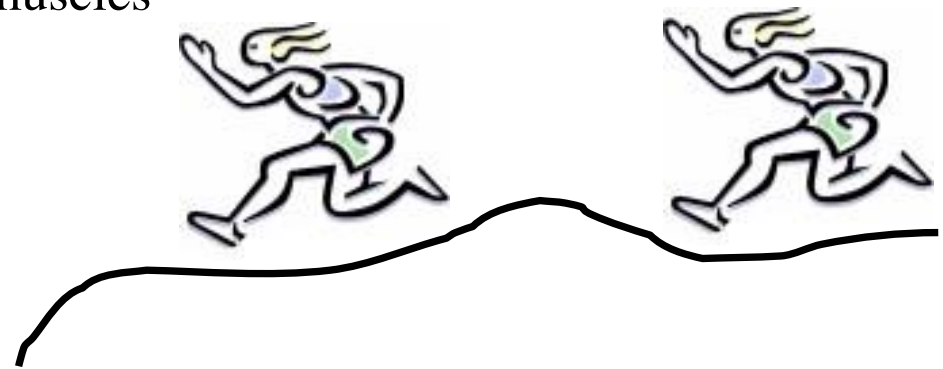
Self-optimizing Control – Marathon

- Optimal operation of Marathon runner, $J=T$
 - Any self-optimizing variable c (to control at constant setpoint)?



Self-optimizing Control – Marathon

- Optimal operation of Marathon runner, $J=T$
 - Any self-optimizing variable c (to control at constant setpoint)?
 - c_1 = distance to leader of race
 - c_2 = speed
 - c_3 = heart rate
 - c_4 = level of lactate in muscles



Self-optimizing Control – Marathon

- Optimal operation of Marathon runner, $J=T$
 - Any self-optimizing variable c (to control at constant setpoint)?
 - c_1 = distance to leader of race (**Problem: Feasibility for d**)
 - c_2 = speed (**Problem: Feasibility for d**)
 - c_3 = heart rate (**Problem: Impl. Error n**)
 - c_4 = level of lactate in muscles (**Problem: Impl.error n**)



Self-optimizing Control – Sprinter

- Optimal operation of Sprinter (100 m), $J=T$
 - Active constraint control:
 - Maximum speed (“no thinking required”)



Further examples

- **Central bank.** J = welfare. u = interest rate. c = inflation rate (2.5%)
- **Cake baking.** J = nice taste, u = heat input. c = Temperature (200C)
- **Business,** J = profit. c = "Key performance indicator (KPI), e.g.
 - Response time to order
 - Energy consumption pr. kg or unit
 - Number of employees
 - Research spending
 Optimal values obtained by "benchmarking"
- **Investment** (portofolio management). J = profit. c = Fraction of investment in shares (50%)
- **Biological systems:**
 - "Self-optimizing" controlled variables c have been found by natural selection
 - Need to do "reverse engineering" :
 - Find the controlled variables used in nature
 - From this possibly identify what overall objective J the biological system has been attempting to optimize

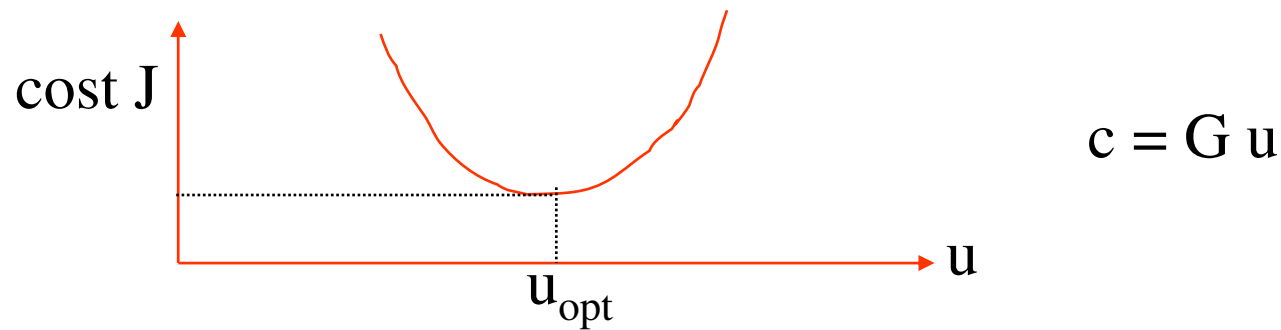
Candidate controlled variables c for self-optimizing control

Intuitive

1. The *optimal value* of c should be *insensitive* to disturbances (**avoid problem 1**)
2. Optimum should be flat (**avoid problem 2 – implementation error**).
Equivalently: *Value* of c should be *sensitive* to degrees of freedom u .
“Want large gain”

Charlie Moore (1980's): Maximize minimum singular value when selecting temperature locations for distillation

Mathematical: Local analysis



$$\begin{aligned}
 \text{LOSS} &= J(u, d) - J_{\text{opt}}(d) = \underbrace{\left(\frac{\partial J}{\partial u}\right)_{\text{opt}}^T}_{=0} (u - u_{\text{opt}}(d)) \\
 &\cdot + \frac{1}{2} (u - u_{\text{opt}}(d))^T \underbrace{\left(\frac{\partial^2 J}{\partial u^2}\right)_{\text{opt}}}_{=J_{uu}} (u - u_{\text{opt}}(d)) + \dots \\
 &\cdot \approx \frac{1}{2} (c - c_{\text{opt}}(d))^T G^{-T} J_{uu} G^{-1} (c - c_{\text{opt}}(d)) \\
 &\cdot \approx \frac{1}{2} G_s^{-T} J_{uu} G_s^{-1} \text{ where } G_s = \text{scaled gain}
 \end{aligned}$$

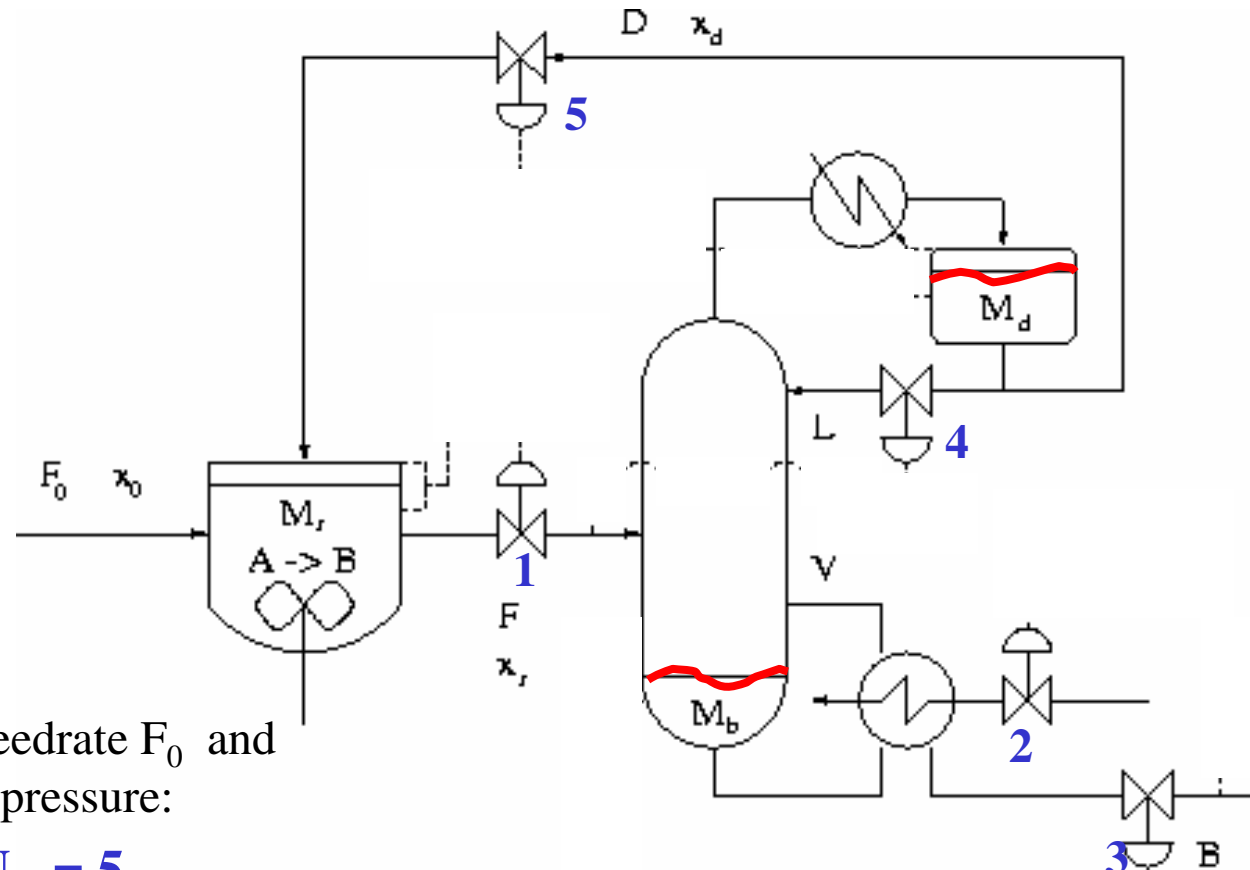
Minimum singular value of scaled gain

*Maximum gain rule (Skogestad and Postlethwaite, 1996):
Look for variables that maximize the scaled gain $\underline{\sigma}(G_s)$
(minimum singular value of the appropriately scaled
steady-state gain matrix G_s from u to c)*

$$\text{Loss} \approx \frac{\bar{\sigma}(J_{uu})}{2} \cdot \frac{1}{\underline{\sigma}(G)^2}$$

Self-optimizing control: Recycle process

$$J = V \text{ (minimize energy)}$$



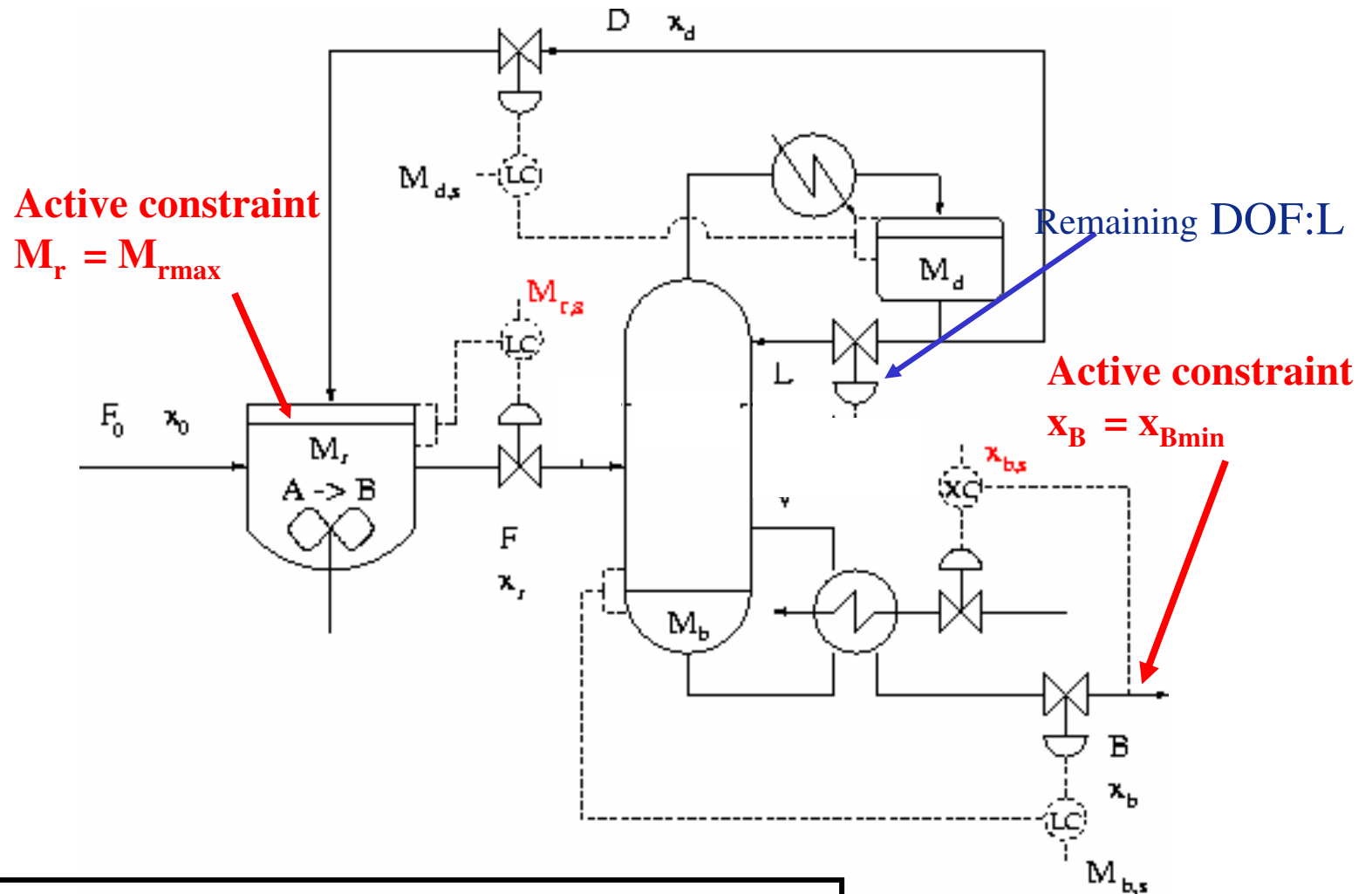
Given feedrate F_0 and column pressure:

$$N_m = 5$$

3 economic (steady-state) DOFs

Constraints: $M_r < M_{rmax}$,
 $x_B > x_{Bmin} = 0.98$

Recycle process: Control active constraints



One unconstrained DOF left for optimization:
What more should we control?

Maximum gain rule: Steady-state gain

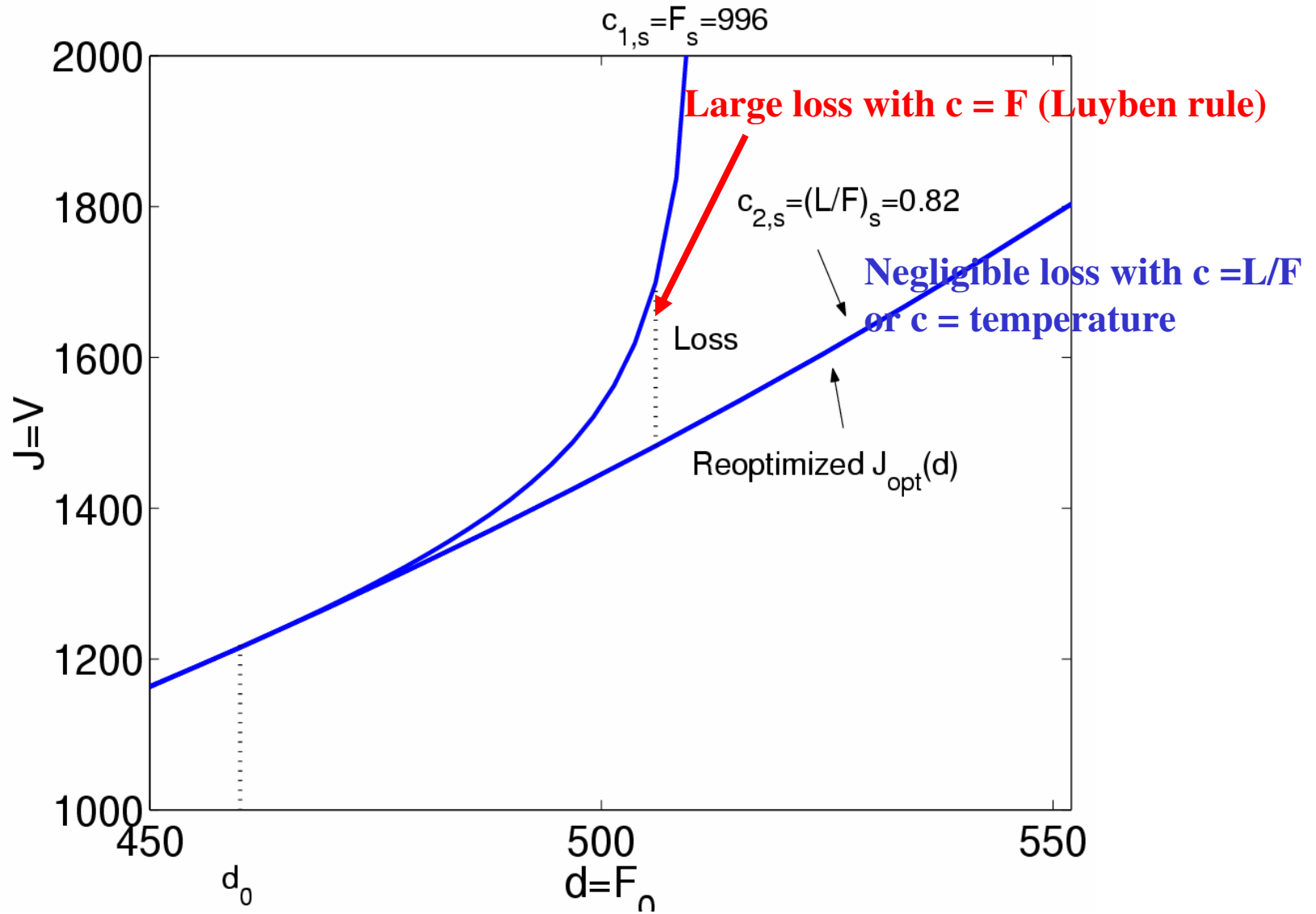
| Rank | c | $ G(0) \cdot 10^3$ |
|------|---------|---------------------|
| 1 | x_D | 13.1 |
| 2 | L/F | 8.9 |
| 3 | D/L | 7.7 |
| 4 | D/V | 5.8 |
| 5 | V/L | 4.5 |
| 6 | B/L | 4.1 |
| 7 | V/F | 4.0 |
| 8 | B/D | 3.3 |
| 9 | L | 3.0 |
| 10 | B/F | 2.6 |
| 11 | D | 2.6 |
| 12 | F/F_0 | 2.5 |
| 13 | D/F | 2.5 |
| 14 | F | 1.9 |
| 15 | B/V | 0 |
| 15 | V | 0 |
| 15 | x_r | 0 |
| 15 | B | 0 |

Conventional:
Looks good

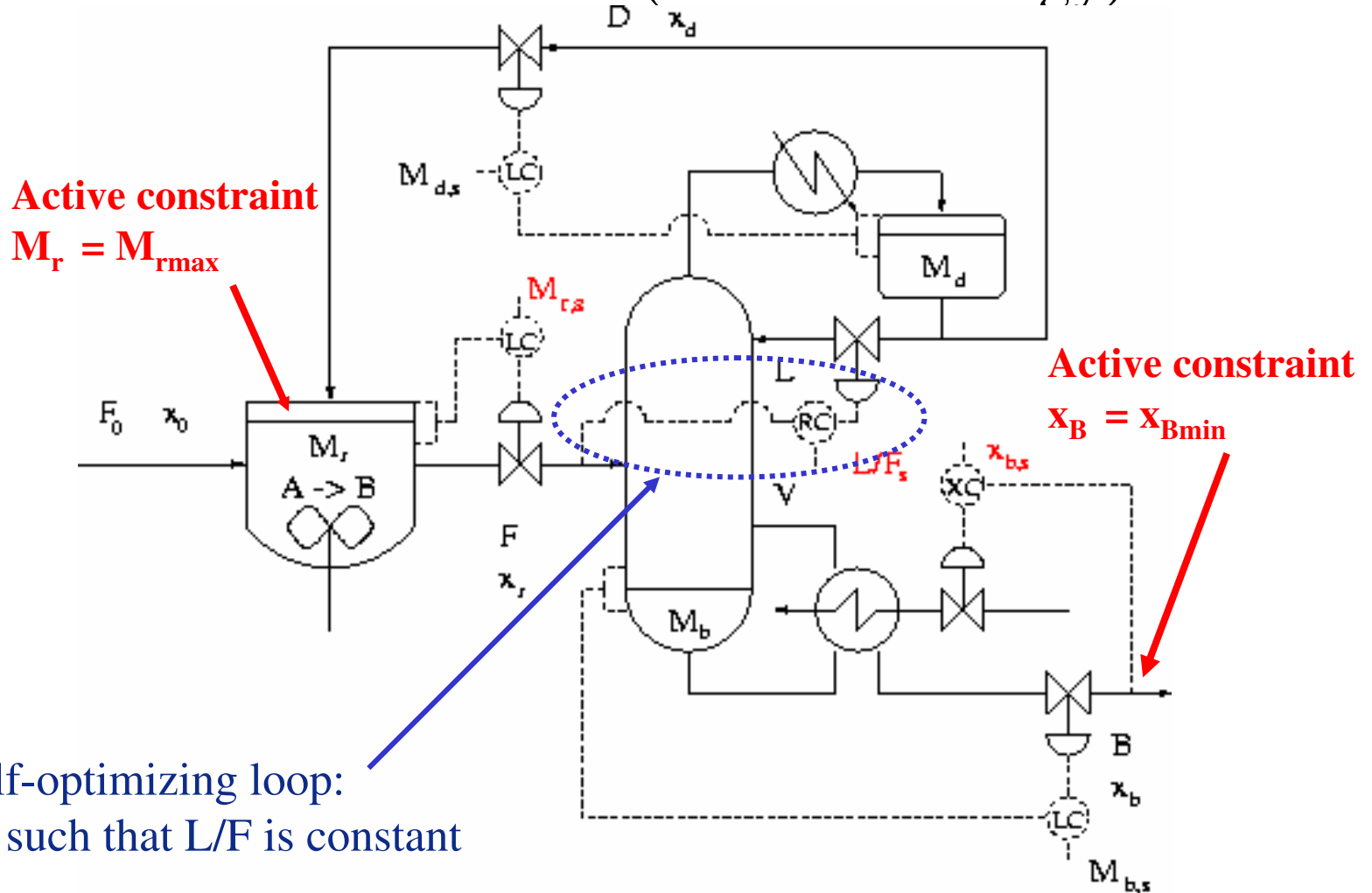
Luyben snow-ball
rule: Not promising
economically

Gain from $u = L$ to c with active constraints (M_r and x_B) constant.
 Scaling: $\Delta c_i = \max_d |c_{opt,i}(d) - c_{opt,i}(d^*)|$ + implementation error.
 $d = F_0, z_F$.

Recycle process: Loss with constant setpoint, c_s



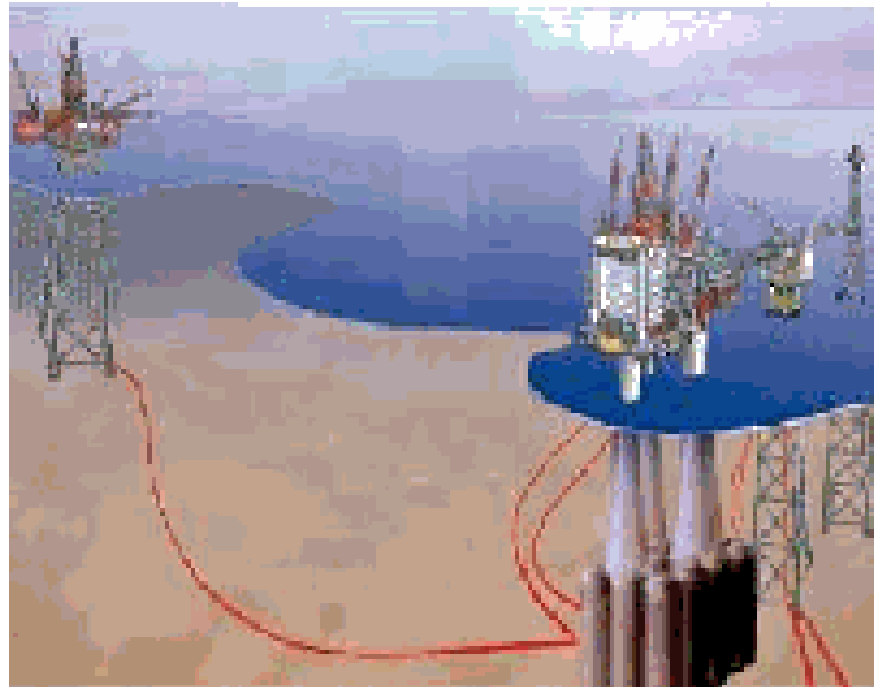
Recycle process: Proposed control structure for case with $J = V$ (minimize energy)



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Application stabilizing feedback control: Anti-slug control



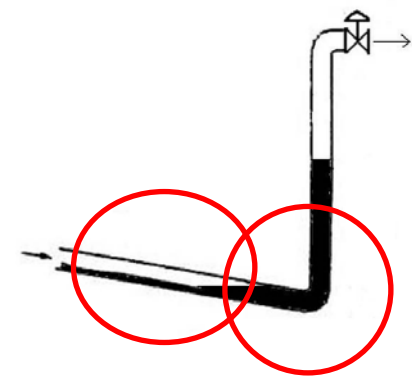
Two-phase pipe flow
(liquid and vapor)



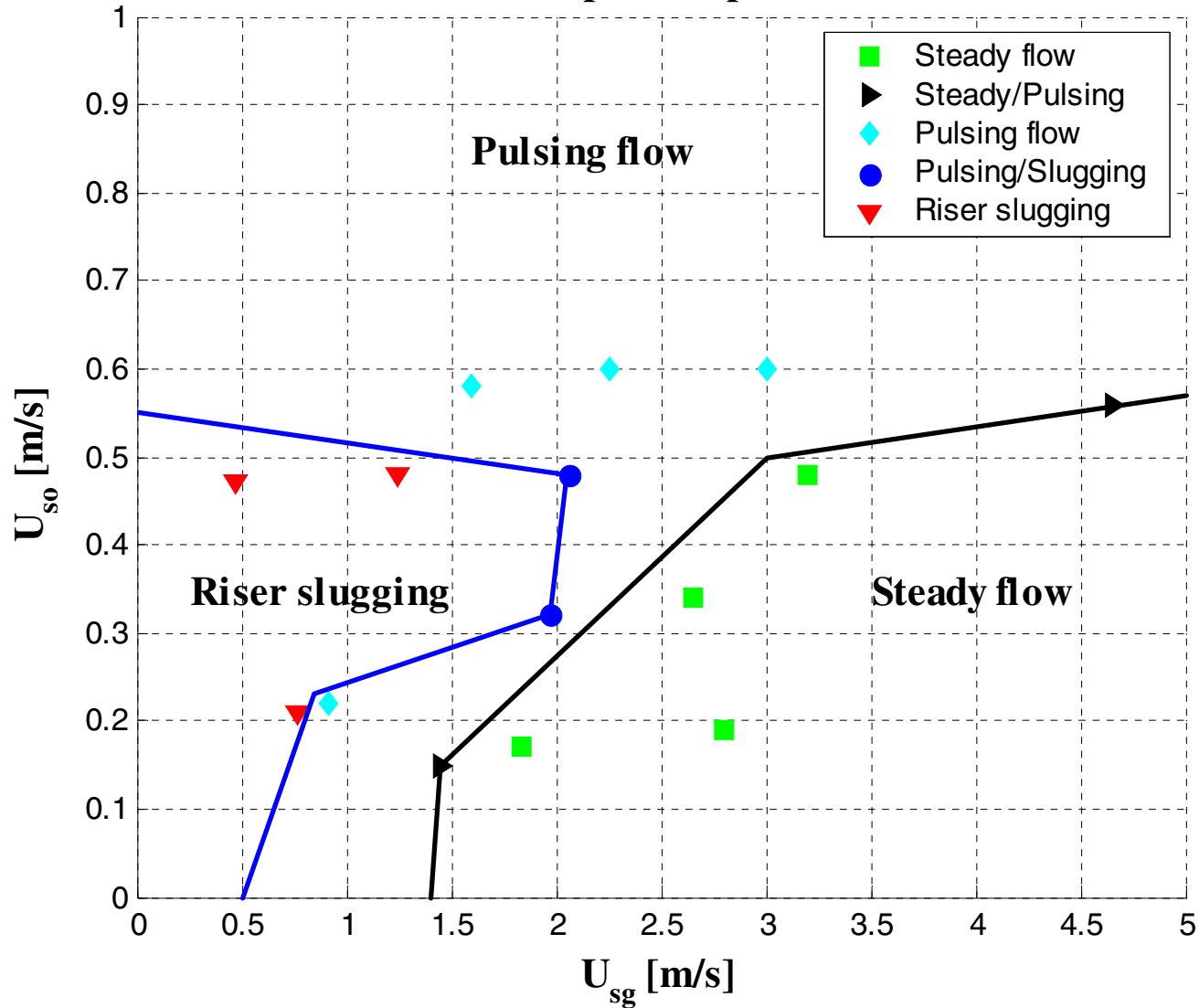
Slug cycle (stable limit cycle)



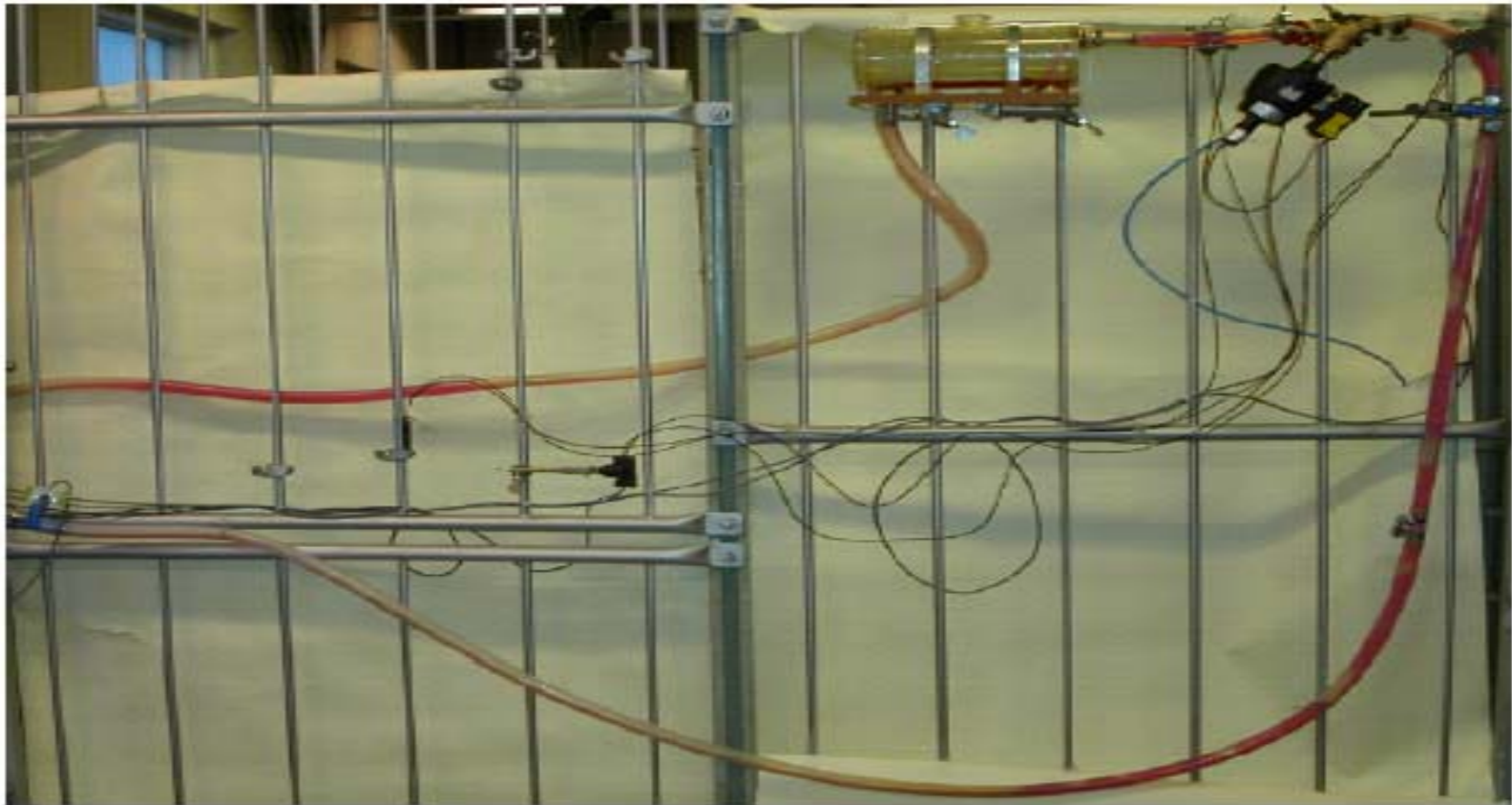
Experiments performed by the Multiphase Laboratory, NTNU



Flow map with open valve

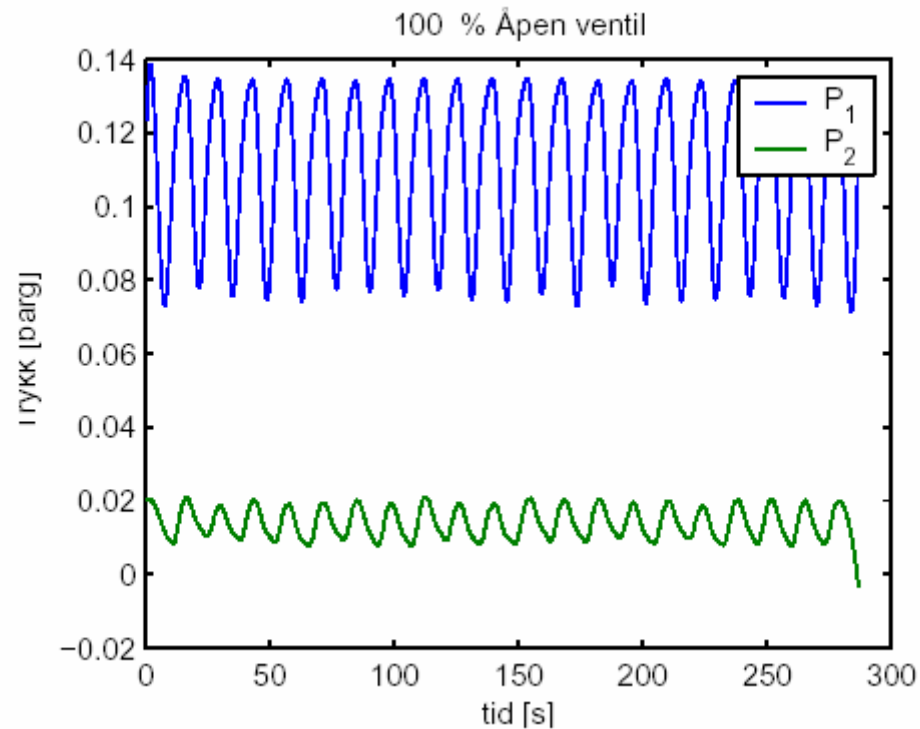
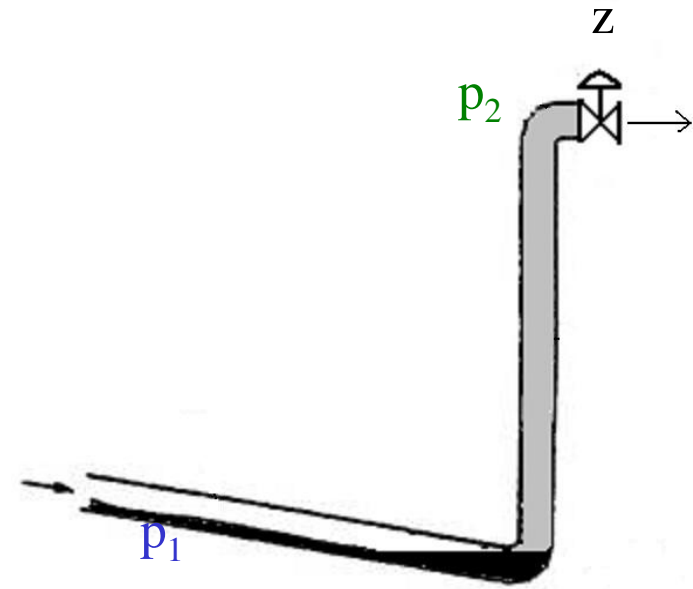


Experimental mini-loop



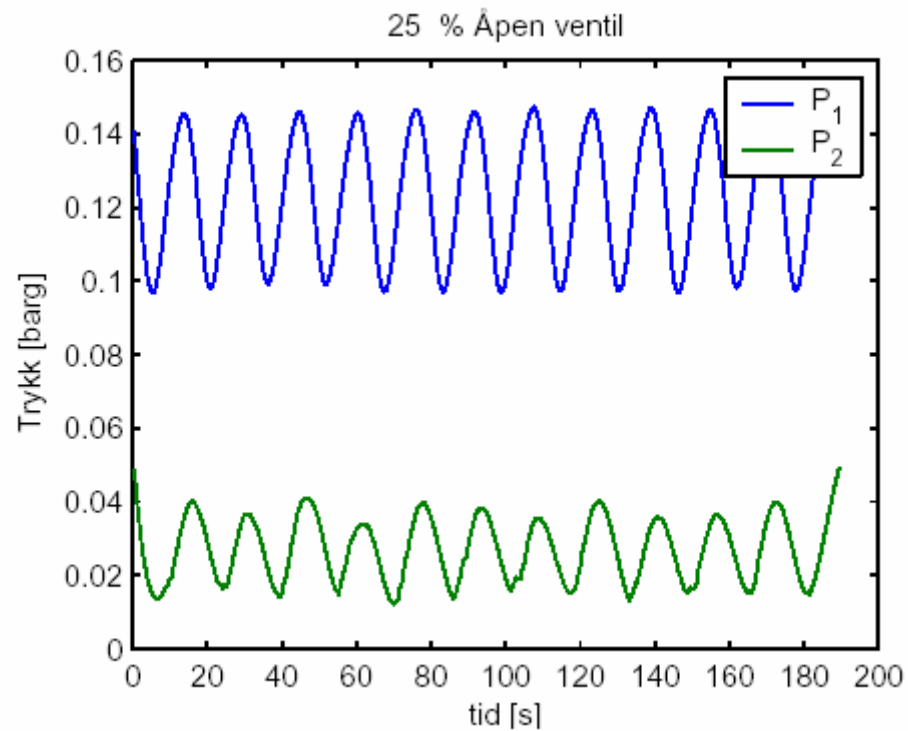
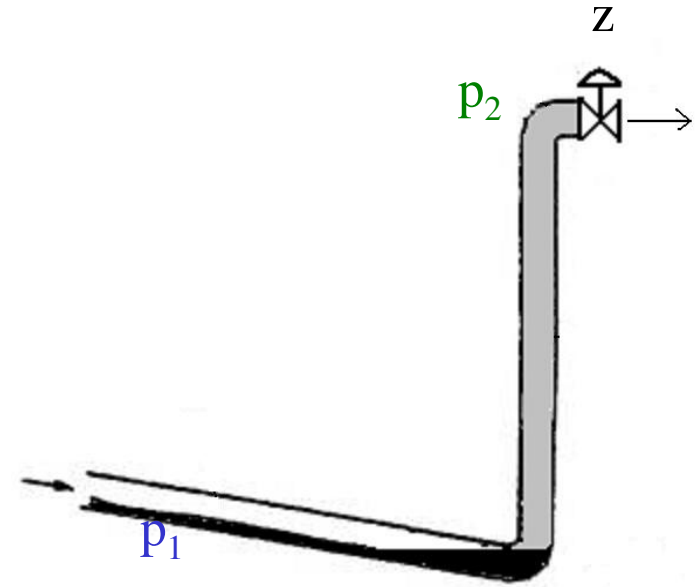
Experimental mini-loop

Valve opening (z) = 100%

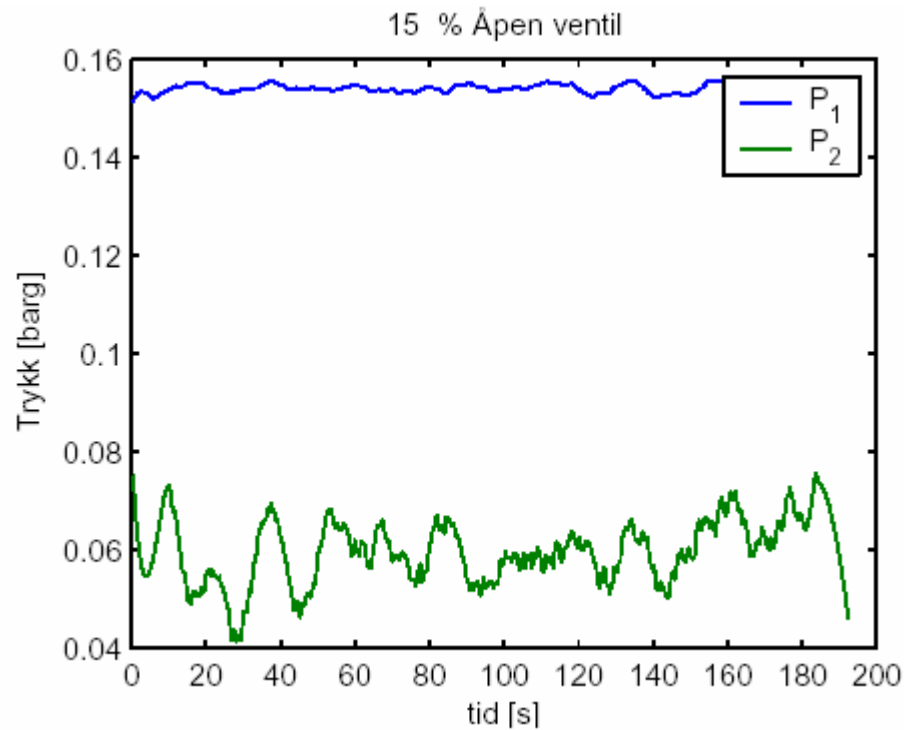
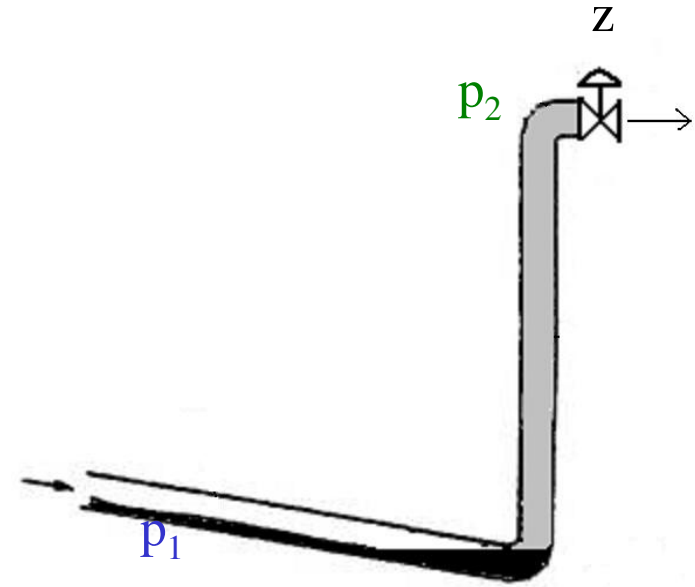


Experimental mini-loop

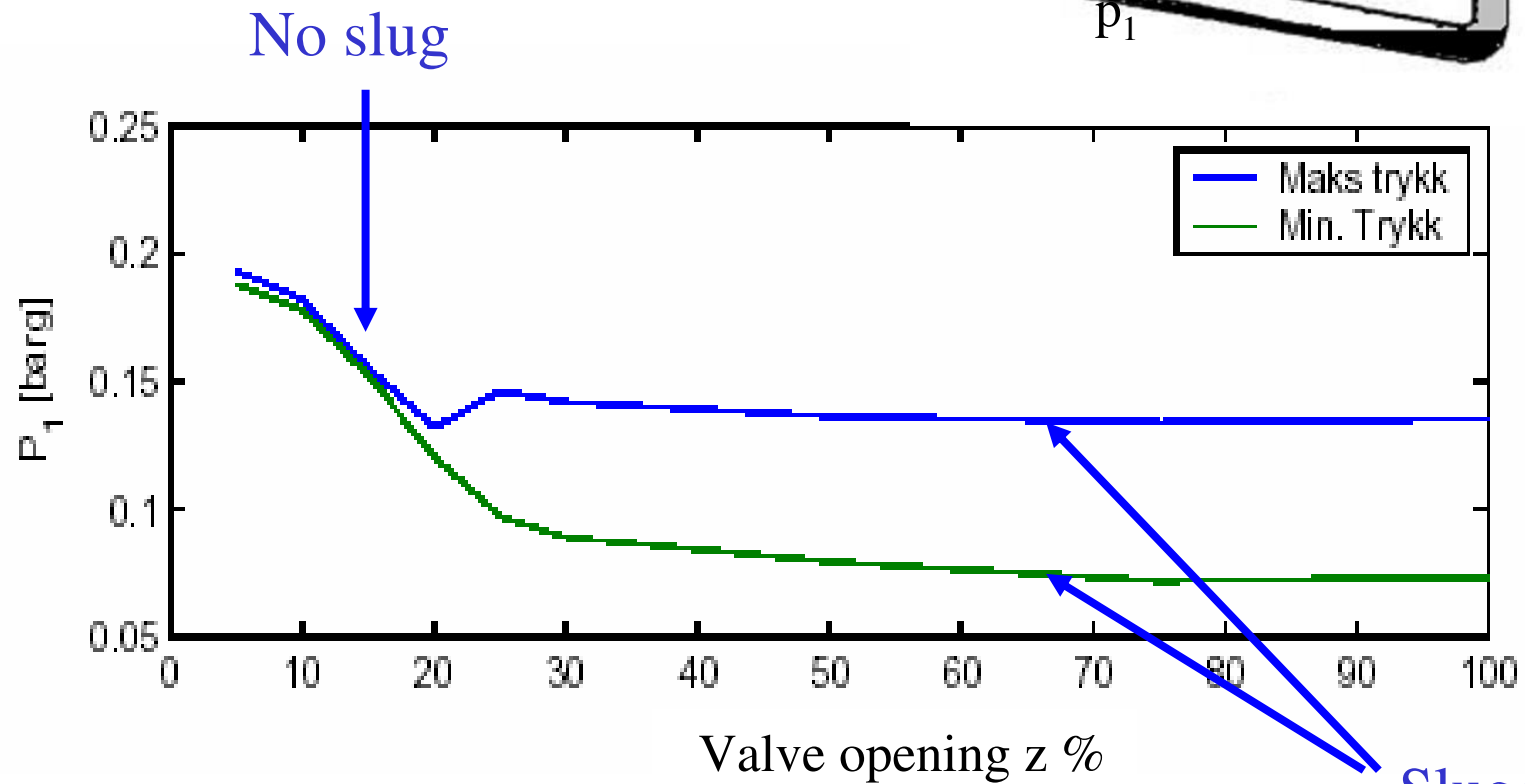
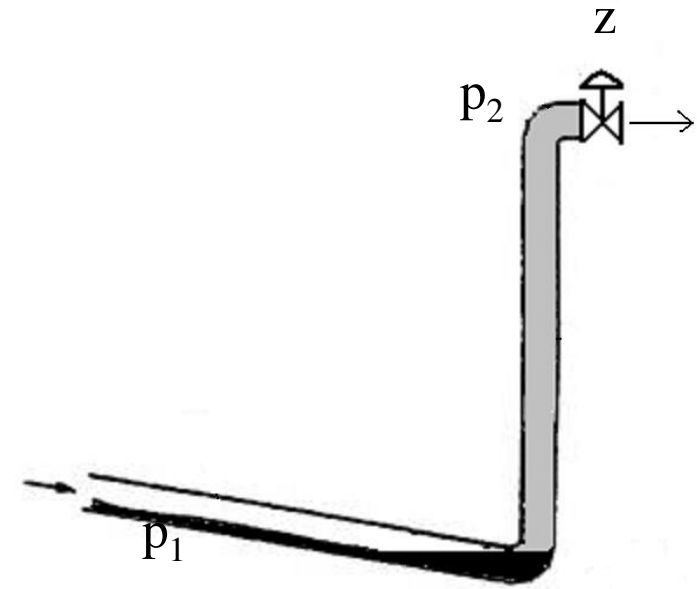
Valve opening (z) = 25%



Experimental mini-loop Valve opening (z) = 15%



Experimental mini-loop: Bifurcation diagram



Slugging

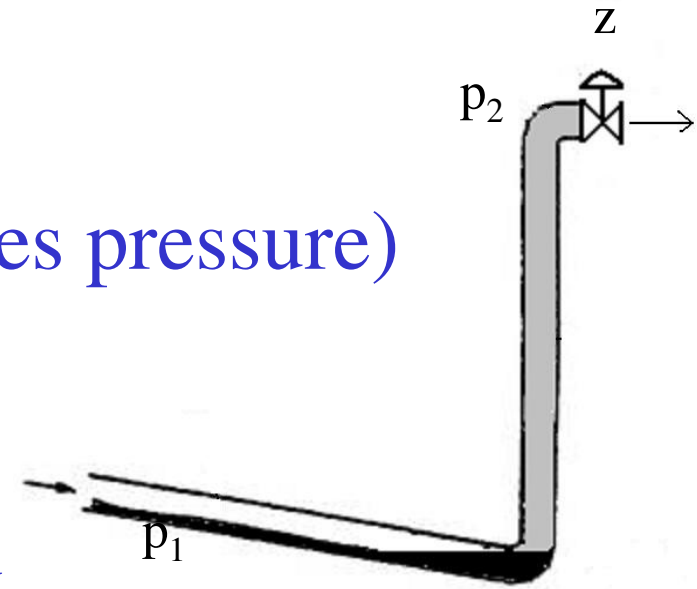
Avoid slugging?

- Design changes
- Feedforward control?
- Feedback control?

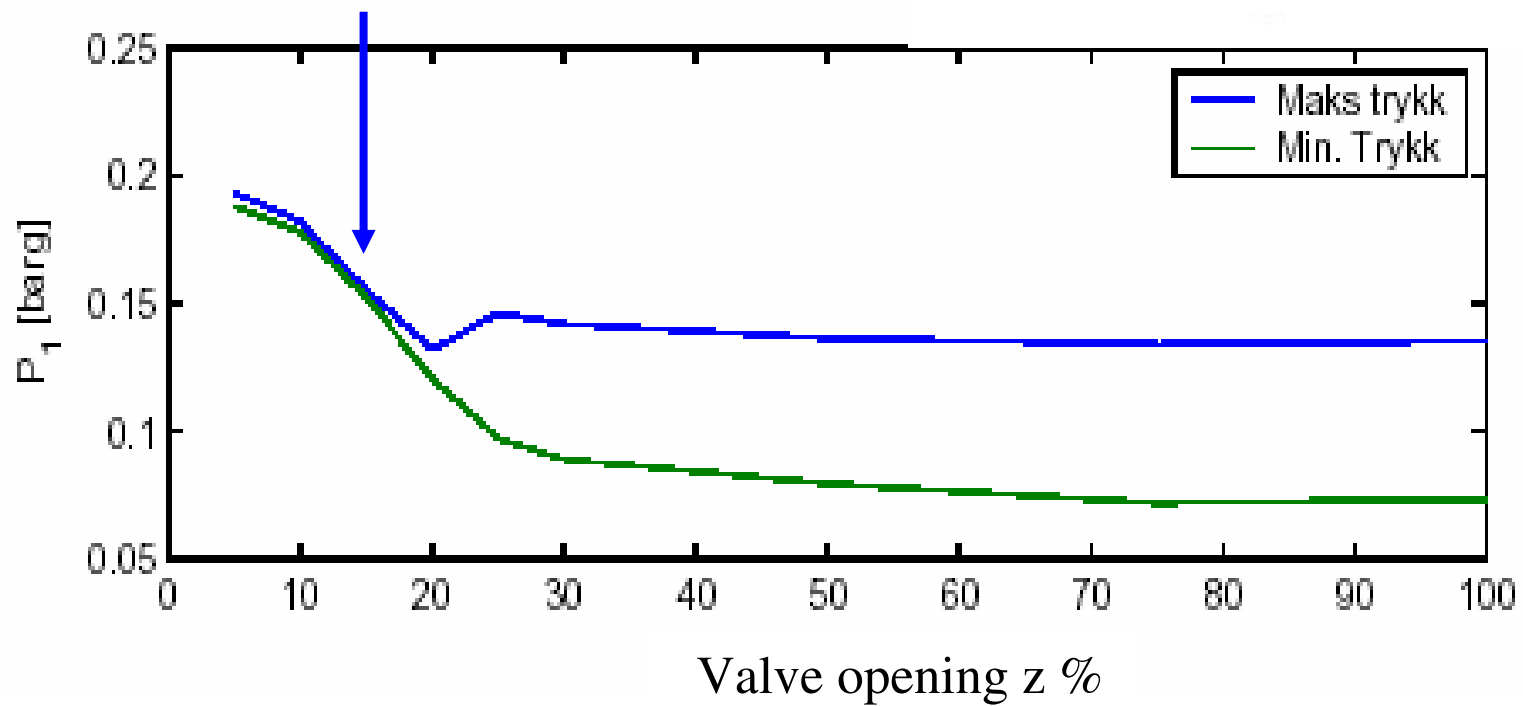
Design change

Avoid slugging:

1. Close valve (but increases pressure)



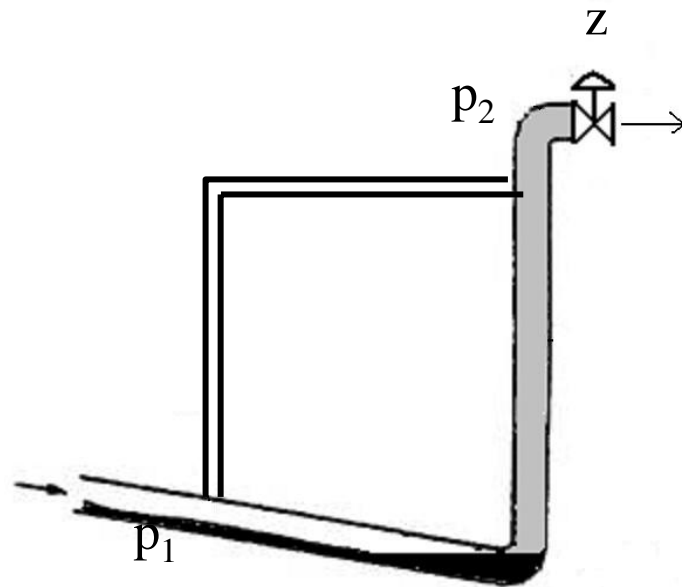
No slugging when valve is closed



Design change

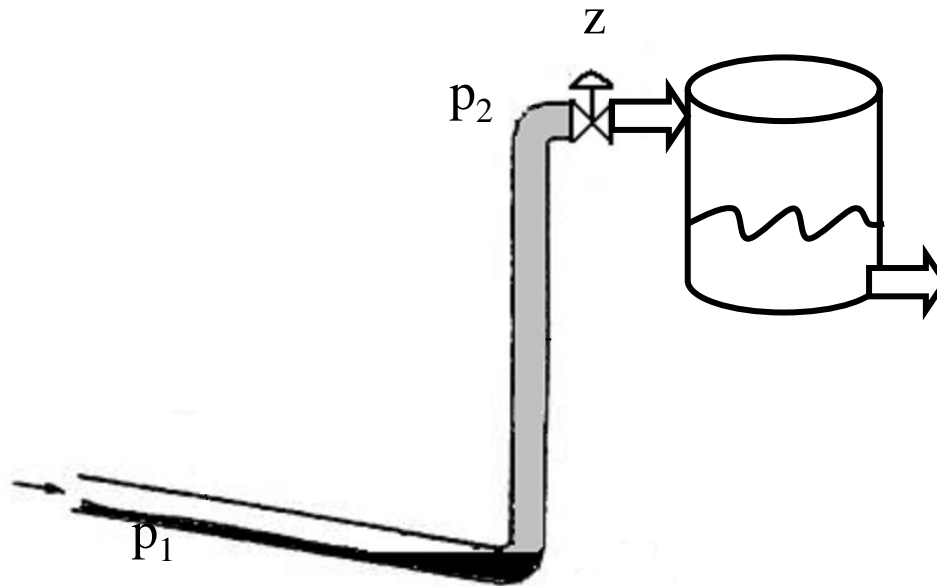
Avoid slugging:

2. Other design changes to avoid slugging



Design change

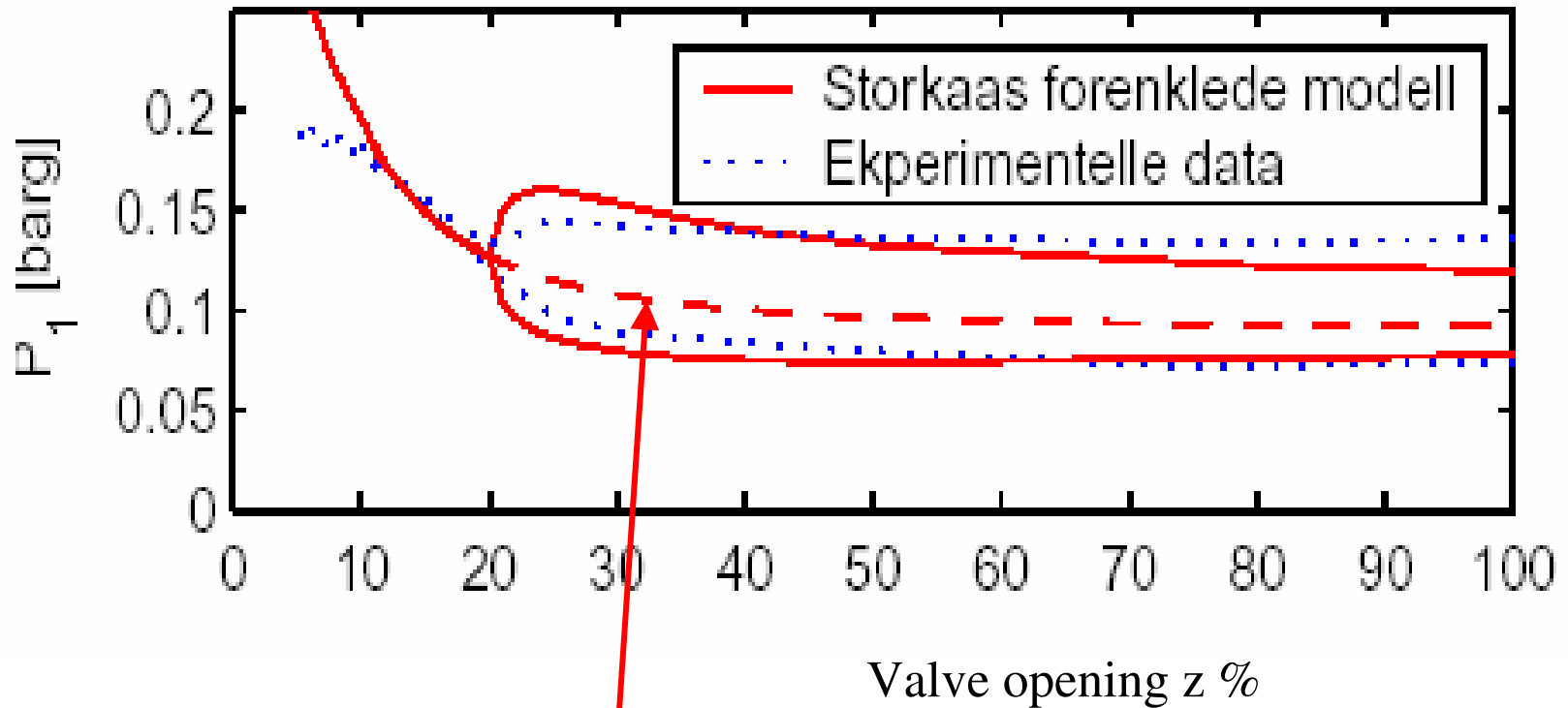
Minimize effect of slugging: 3. Build large slug-catcher



- Most common strategy in practice

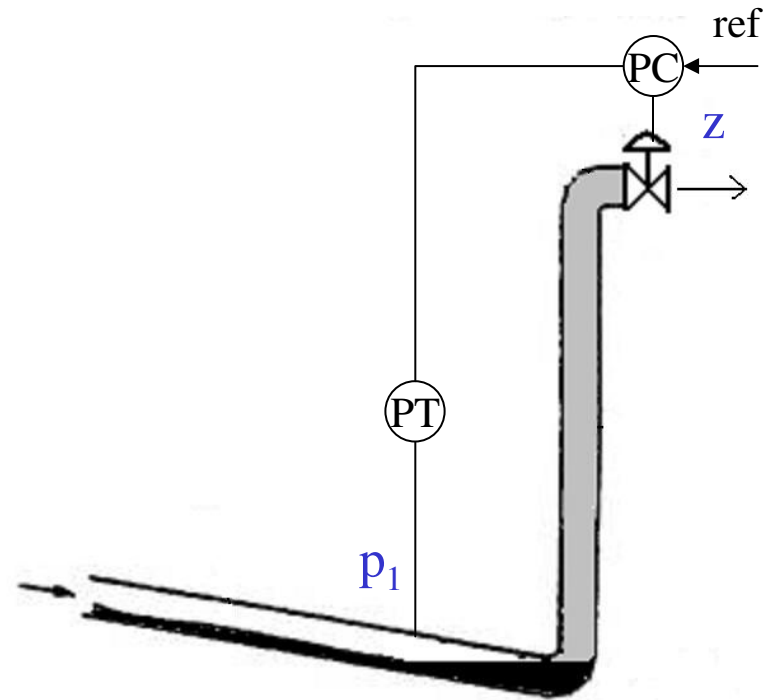
Avoid slugging: 4. Feedback control?

Comparison with simple 3-state model:



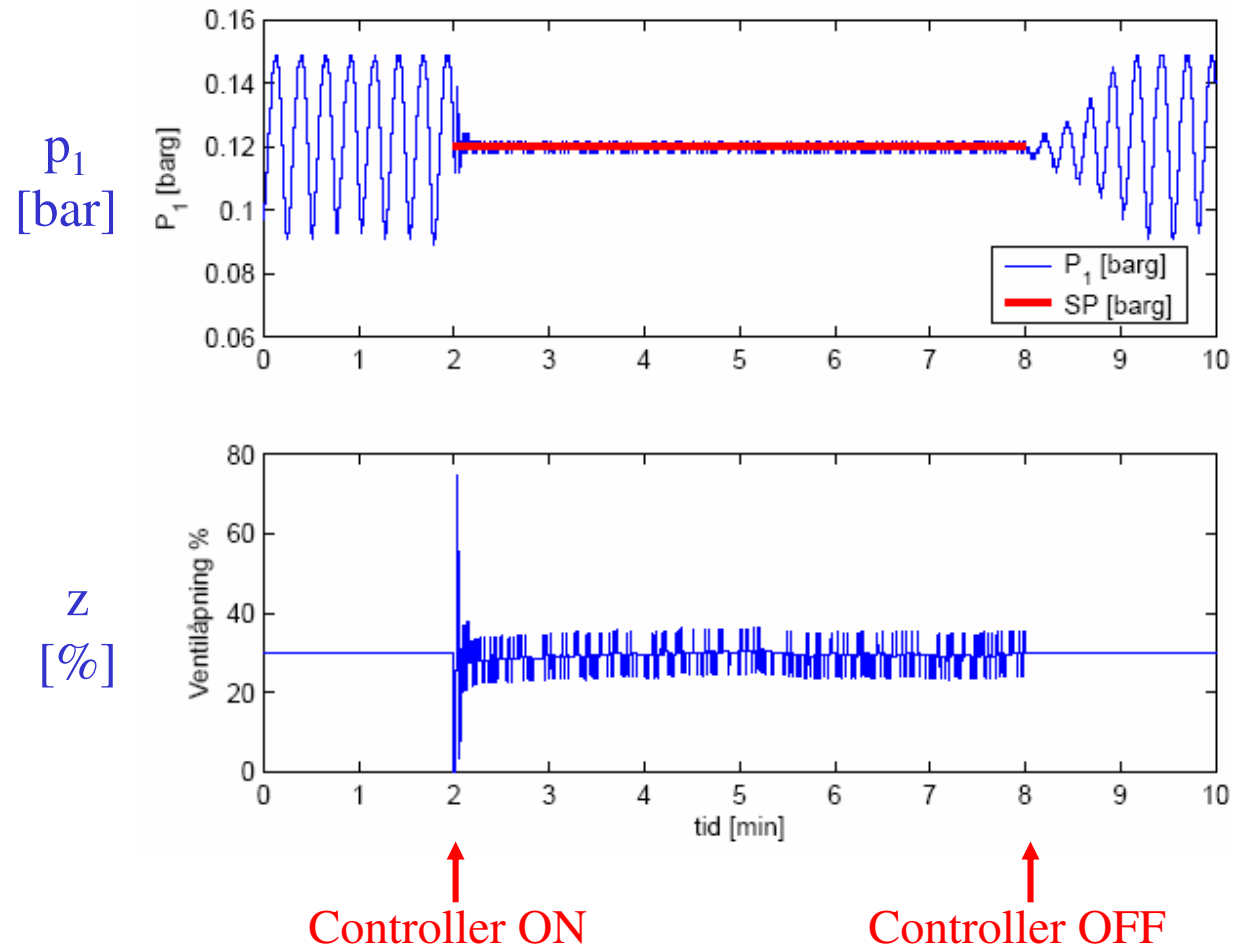
Predicted smooth flow: Desirable but open-loop unstable

Avoid slugging: 4. "Active" feedback control

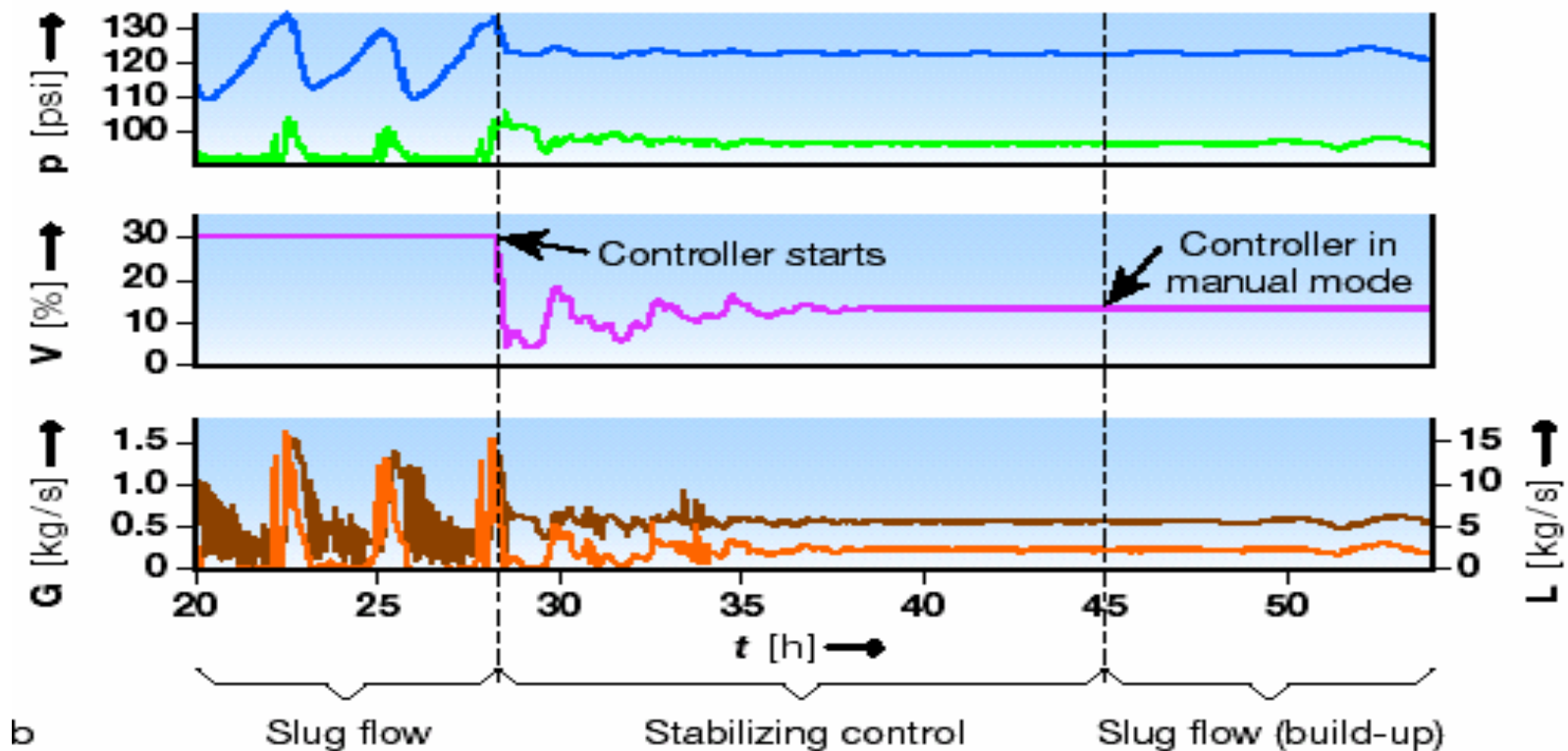


Simple PI-controller

Anti slug control: Mini-loop experiments



Anti slug control: Full-scale offshore experiments at Hod-Vallhall field (Havre, 1999)



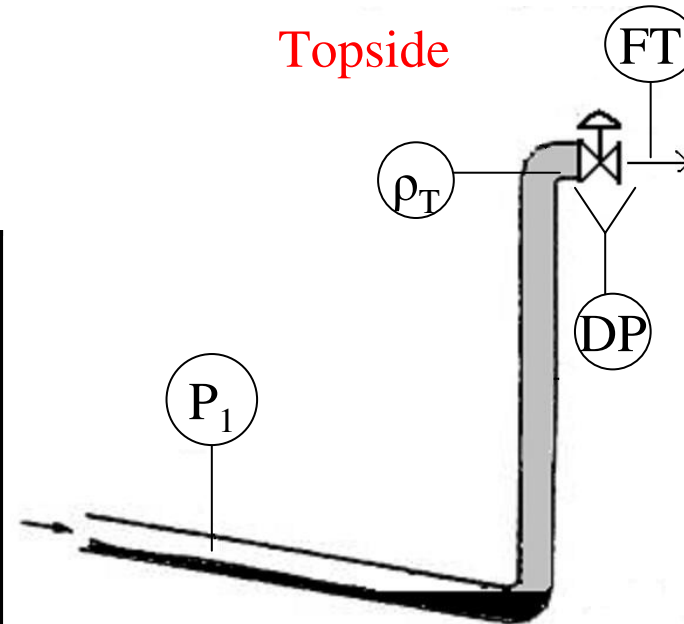
Analysis: Poles and zeros

Operation points:

| z \ y | P ₁ | DP | Poles |
|-------|----------------|------|-------------------------|
| 0.175 | 70.05 | 1.94 | -6.11 0.0008±0.0067i |
| 0.25 | 69 | 0.96 | -6.21 0.0027±0.0092i |

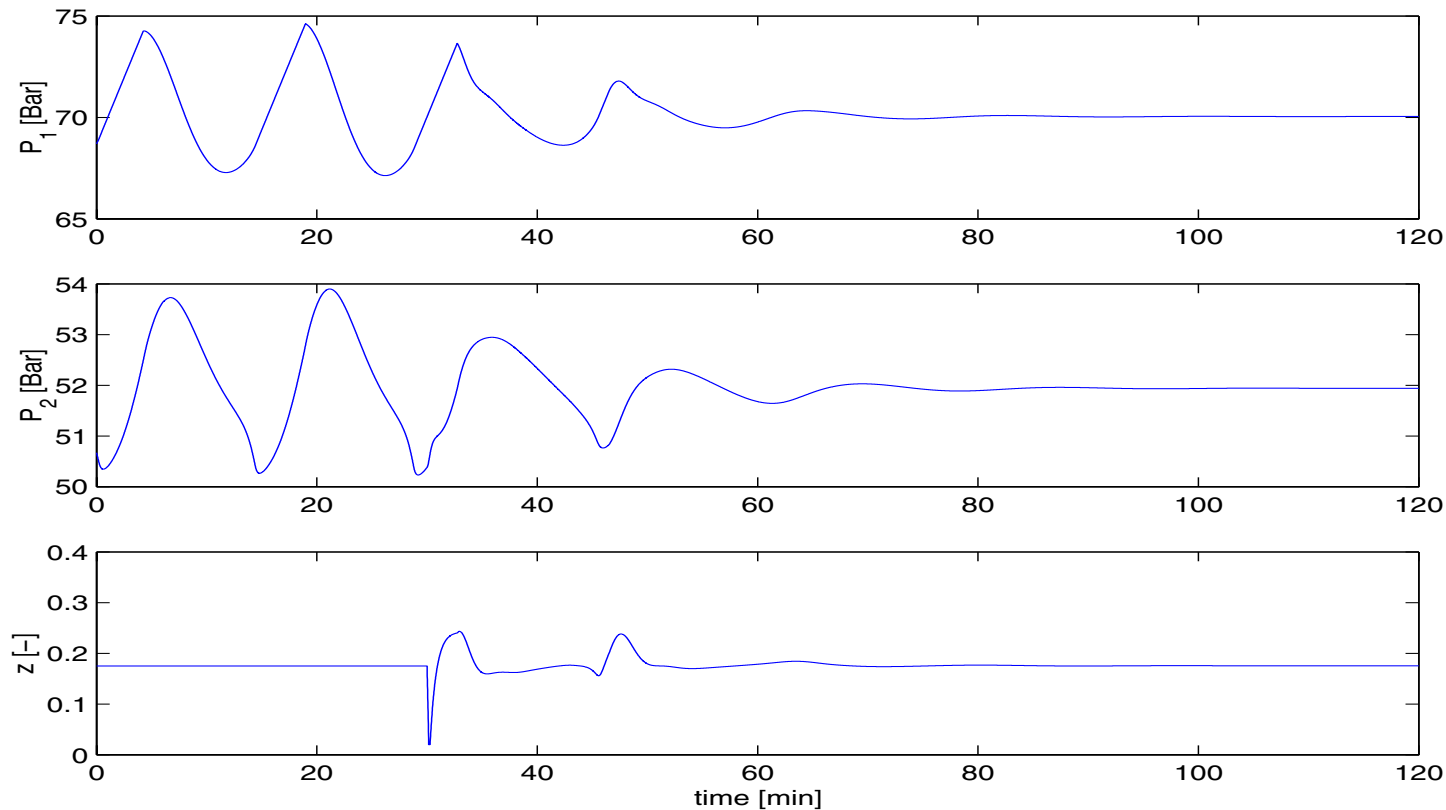
Zeros:

| z \ y | P ₁ [Bar] | DP[Bar] | ρ _T [kg/m ³] | F _Q [m ³ /s] | F _W [kg/s] |
|-------|----------------------|------------------|-------------------------------------|------------------------------------|-------------------------|
| 0.175 | -0.0034 | 3.2473 0.0142 | -0.0004 0.0048 | -4.5722 -0.0032 -0.0004 | -7.6315 -0.0004 0 |
| 0.25 | -0.0034 | 3.4828 0.0131 | -0.0004 0.0048 | -4.6276 -0.0032 -0.0004 | -7.7528 -0.0004 0 |



Topside measurements: Ooops.... RHP-zeros or zeros close to origin

Stabilization with topside measurements: Avoid ‘RHP-zeros by using 2 measurements



- Model based control (LQG) with 2 top measurements: DP and density ρ_T

Summary anti slug control

- Stabilization of smooth flow regime = \$\$\$\$!
- Stabilization using downhole pressure simple
- Stabilization using topside measurements possible
- Control can make a difference!

Thanks to: Espen Storkaas + Heidi Sivertsen and Ingvald Bårdsen

Conclusions

- **Feedback** is an extremely powerful tool
- Complex systems can be controlled by hierarchies (cascades) of single-input-single-output (SISO) control loops
- Control the right variables (primary outputs) to achieve **"self-optimizing control"**
- **Feedback** can make new things possible (anti-slug)