

# **Multiscale Modeling and its Application to Catalyst Design and Portable Power Generation**

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## **Outline**

- Decentralized, future energy production
- Miniaturization differs from scaling up
- Multiscale modeling
- Application of multiscale modeling to
  - Development of detailed reaction mechanisms
  - Microreactor design
  - Process optimization
  - Catalyst design
  - Experiment design

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## Down-scaling for future energy needs

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- Distributed energy
  - On-board  $H_2$  production
  - Electric reliability
  - Local solutions, e.g., farms based on biomass



Smart Car

Courtesy: Ballard Power Systems



- Portable energy (electronics)

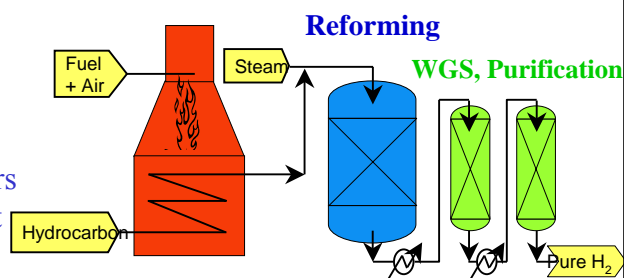


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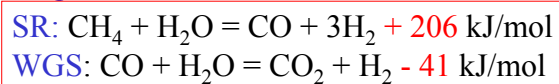
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## Large scale H<sub>2</sub> production is industrially mature

- Steady state operation
- Reforming:
  - endothermic, heat transfer controlled
  - Fixed bed catalytic reactors with Ni catalyst for syngas



- **Large scale flames supply the heat**
  - **Half of NG is burned to CO<sub>2</sub> and H<sub>2</sub>O**
- Complex downstream processing WGS and PROX or membrane separation/PSA
- Slow ( $\tau \sim 1s$ ); bulky



## Steam reforming is a bulky process

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Schested, *Cat. Today* 111 (2006) 103

## First example of on-board reforming

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- GM unveiled the world's first gasoline fuel processor for fuel cell propulsion at the annual automotive management conference in Traverse City, Mich.
- The Gen III processor, packaged in a Chevrolet S-10 pickup, reforms 'clean' gasoline onboard, extracting a stream of hydrogen to send to the fuel cell stack.

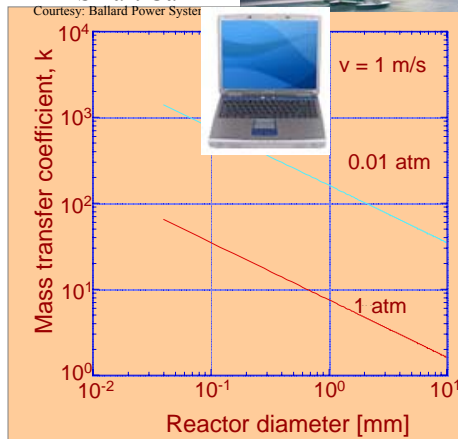


## Microsystems for transportation and portable applications

- Advantages
  - Process intensification
    - High heat and mass transfer coefficients
    - Multifunctionality
  - Compactness
  - Inherently safe
- Scale out is feasible for portable (small scale) devices



Smart Car



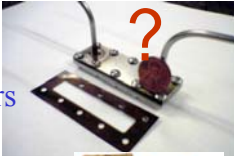

## Microscales impose challenges and offer opportunities<sup>1</sup>

- Laminar flows - mixing?
  - Small systems - enough catalyst?
  - Reactors shake - no moveable parts
  - Need small pressure drops
  - Transient operation very common
    - Fast startup and shutdown require active catalyst and fast heat transfer
    - Catalyst deactivation can become a major issue
  - Fast chemistry
  - Different systems' engineering<sup>2</sup>
- Monolithic type reactors

Dynamics

New chemistry and catalysts

Flowsheets/Optimization

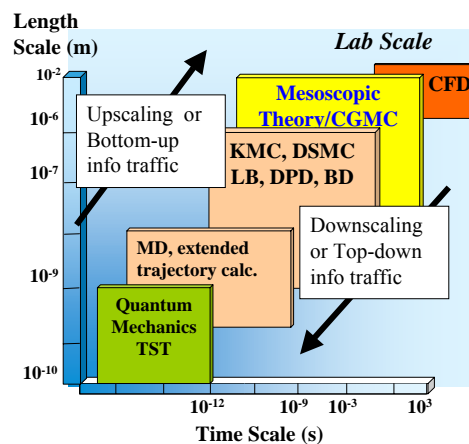
<sup>1</sup> Norton *et al.*, "Downsizing chemical processes for portable hydrogen production", in *Microreactor Techn. Process Intensification*, ACS Symp. Series 914, 179 (2005)

<sup>2</sup> Mitsos *et al.*, *IECR* 43, 74 (2004)

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## The multiscale simulation paradigm: A bottom-up ladder

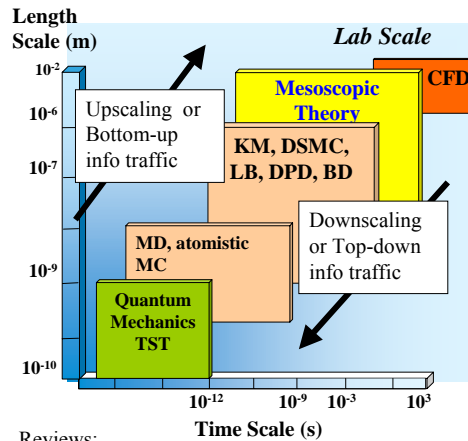


- Previous work
  - focused usually on a single scale and one way of information passing
  - developed structure-properties relations (molecular descriptors) without attention to processing

Reviews:

Raimondeau and Vlachos, *Chem. Eng. J.* **90**, 3 (2002);  
Chatterjee et al., *Chem. Eng. Sci.*, *ISCRE Issue* (2004);  
Vlachos, *Adv. Chem. Eng.* **30**, 1 (2005)

## The Multiscale Simulation Paradigm: Predict macroscopic performance from first principles



Reviews:

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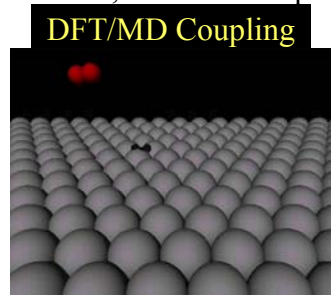
Chatterjee et al., *Chem. Eng. Sci.* **59**, 5559 (2004);

Vlachos, *Adv. Chem. Eng.* **30**, 1 (2005)

\* For noise control in hybrid siml, see work by groups of Braatz, Christofides, Vlachos

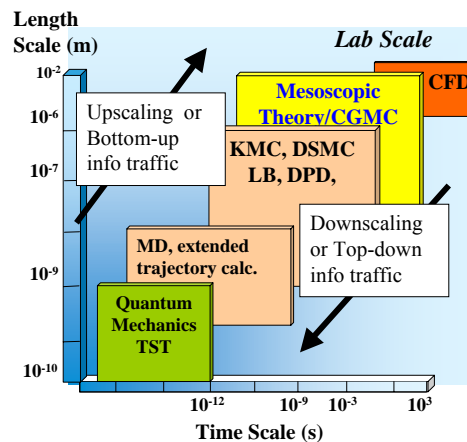
### Challenges

- Phenomena and models are strongly coupled
- Develop bridges between models of various scales to enable accurate, robust, efficient, seamless coupling\*



Ludwig and Vlachos, *Mol. Simul.* (2004)

## The multiscale simulation paradigm: A bottom-up ladder



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- Direct multiscale simulation (hybrid, coarse graining) is possible for systems of moderate complexity

- It is plagued by computational cost for complex systems, such as chemical reactors

- Are all scales and phenomena important?

## Hierarchical, multiscale model development

- Lower Level Theory
- Microkinetic model chemistry parameters
  - Semi-empirical techniques (BOC), TST
- Catalyst model
  - Mean field approximation
- Fluid flow/Transport
  - Simple reactor models (PFR, CSTR, transp. correlations)

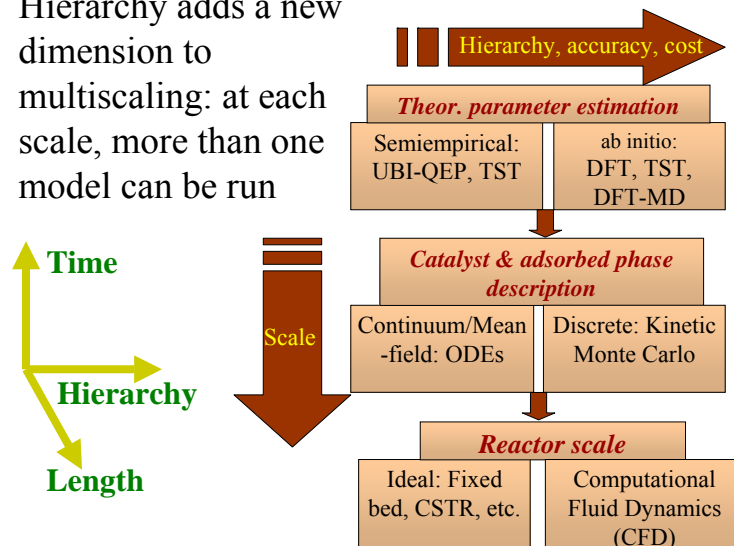
## Hierarchical, multiscale model development

- Last theoretical level:  
Engineering models are needed for reactor optimization and control and for model-based catalyst design
- Feature identification toolbox enables hierarchical model development and reduction



## Hierarchy enables rapid screening of chemistry, fuels, and catalysts

- Hierarchy adds a new dimension to multiscaling: at each scale, more than one model can be run



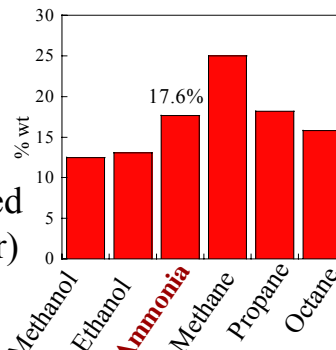
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## NH<sub>3</sub> cracking for H<sub>2</sub> production

- **Good hydrogen carrier**

- High energy density
- Stored as a liquid (at 25 °C, 8 atm)
- One of the most widely produced chemicals (>100 metric tones/yr)
  - Haber-Bosch Process
  - Infrastructure is already set up



- **Catalytic decomposition of pure NH<sub>3</sub> on Ru<sup>1,2</sup>**



– Slightly endothermic

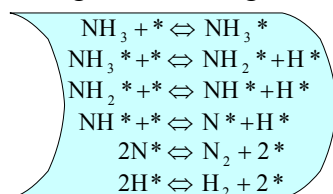
<sup>1</sup> Deshmukh et al., Ind. Eng. Chem. Res. (2004)

<sup>2</sup> Ganley et al., AIChE J. (2004)

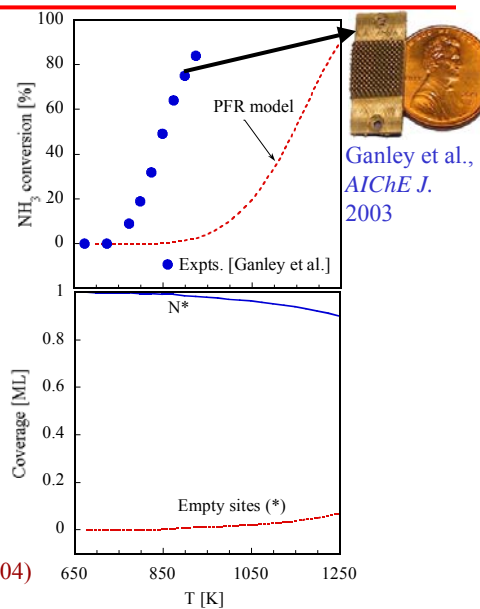
– Minimal downstream processing

## NH<sub>3</sub> decomposition on Ru: 2NH<sub>3</sub> = N<sub>2</sub> + 3H<sub>2</sub>

- NH<sub>3</sub> as a storage medium
- ‘Pure’ H<sub>2</sub> – No CO<sub>x</sub>
- A microkinetic model is build using BOC and TST
- Our microkinetic model captures the trend
- High N\* coverages

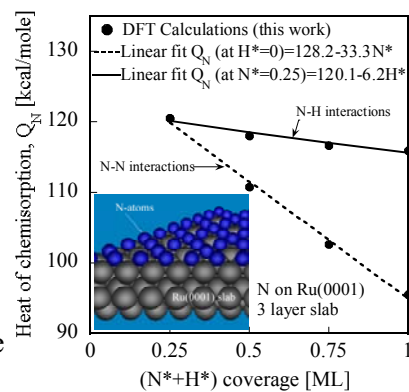


Mhadeshwar et al., *Cat. Letters* **96**, 13-22 (2004)



## DFT is used to estimate lateral interactions

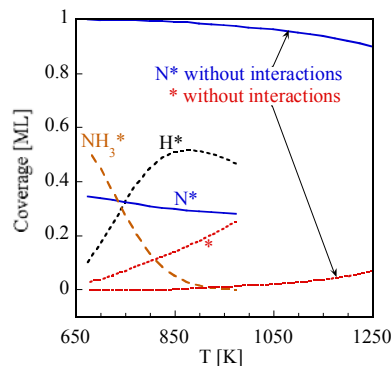
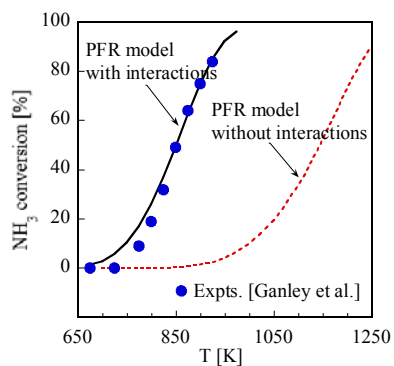
- DACAPO (solid-state electronic structure package by Hammer and coworkers\*)
- 3-Layer slab of Ru(0001)
- $2 \times 2$  unit cell
- All layers are relaxed
- Plane wave cutoff = 350eV
- 18 k-points for surface Brillouin zone
- Generalized gradient approximation (PW-91)



Deshmukh et al., *Int. J. Multiscale Comp. Eng.* 2, 221-238 (2004)

\* Hammer et al., DACAPO version 2.7 (CAMP, Technical University, Denmark)

## DFT-retrained microkinetic model describes the experimental data well

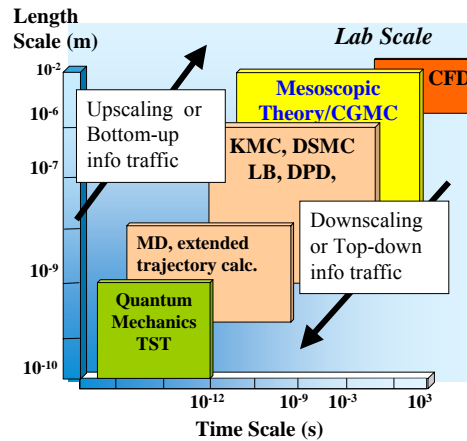


- H-H and N-H interactions are small
- N-N interactions completely change the chemistry
- **Extensive validation against UHV and high P data has been done**

Exps: Ganley et al., *AIChE J.* (2004)

Deshmukh et al., *Int. J. Multiscale Comp. Eng.* 2, 221-238 (2004)

## The multiscale simulation paradigm: A bottom-up ladder



### • Typical objective

- Mechanistic understanding
  - Reconcile large differences in published data
  - Process optimization:
- Process engineering**

#### Reviews:

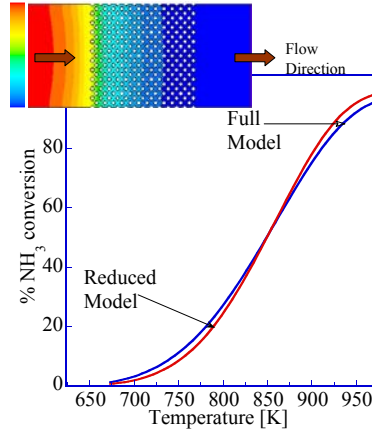
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## Computer-aided chemistry reduction

- Sensitivity and Principal Component Analyses
  - No *a priori* assumptions
  - Identification of important reactions and species
- Small parameter asymptotics on species balances and site conservation
  - Simple algebra to derive a rate expression



Mhadeshwar *et al.*, *Cat. Letters* **96**, 13 (2004)

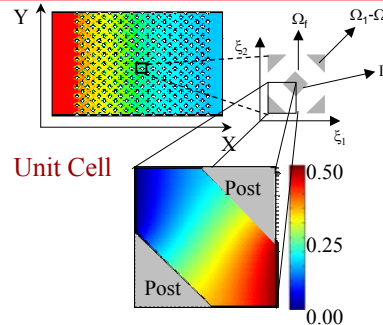
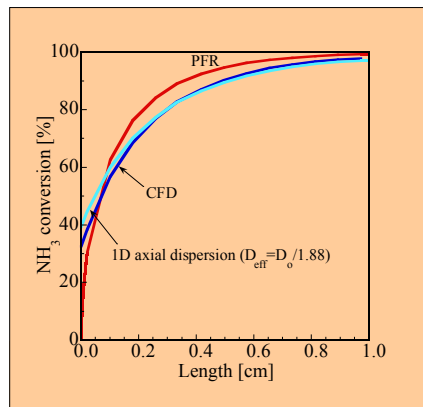
$$\text{Reduced Model} \quad \sigma_{N_2} = k_4 \theta_{N^*}^2 - k_3 P_{N_2} \theta_*^2 \quad \theta_* = \frac{1}{1 + \frac{k_{11} P_{NH_3}}{k_{12}} + \sqrt{\frac{k_1}{k_2} P_{H_2}} + \sqrt{\frac{k_3}{k_4} P_{N_2}} + \sqrt{\frac{k_2}{k_1} \frac{k_7 k_9 k_{11}}{2k_4 k_{10} k_{12}} P_{NH_3} P_{H_2}^{-0.5}}}$$

$$\sigma_{H_2} = 3 \sigma_{N_2} \quad \text{and} \quad \sigma_{NH_3} = -2 \sigma_{N_2}$$

## $\mu$ Reactor is close to axial dispersion model $D_{eff}$ vs. Geometric characteristics

- The method of homogenization is used that is based on separation of length scales

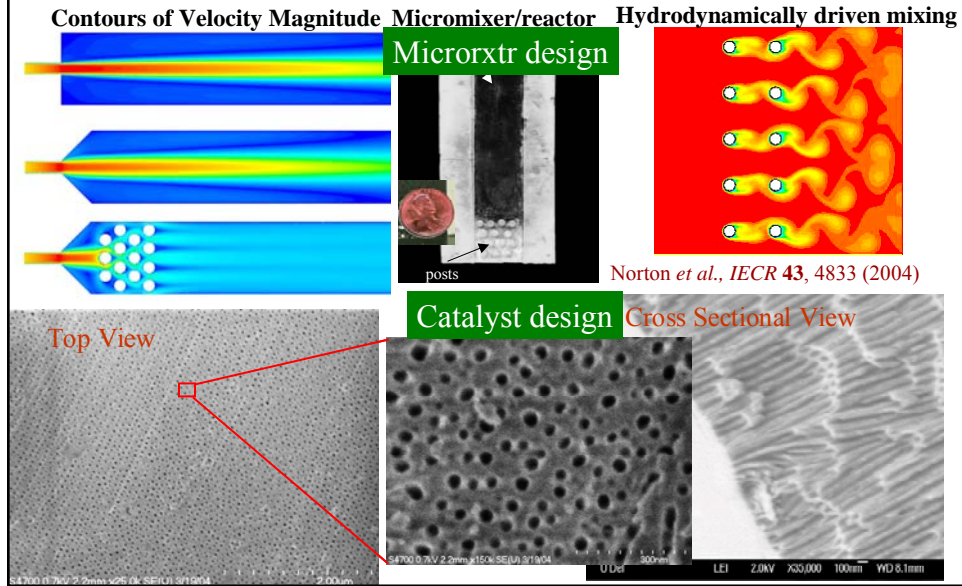
$$\varepsilon = \frac{\ell}{L} \ll 1$$



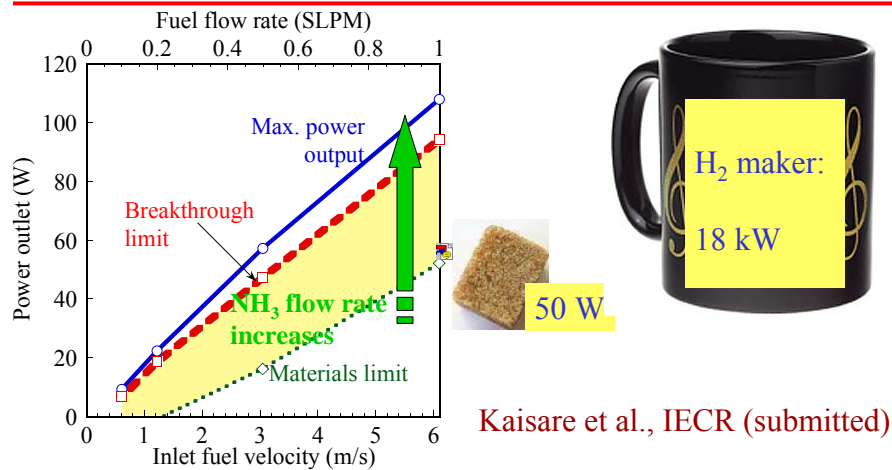
Multiscale simulation allows us to explore cheaply the effect of post shape, size, and density on microreactor performance by solving simple unit cell problems

Deshmukh *et al.*, *Int. J. Multiscale Comp. Eng.* **2**, 221-238 (2004)

## Design and fab of microchemical systems via multiscale modeling



## Attainable regions in multifunctional microdevices

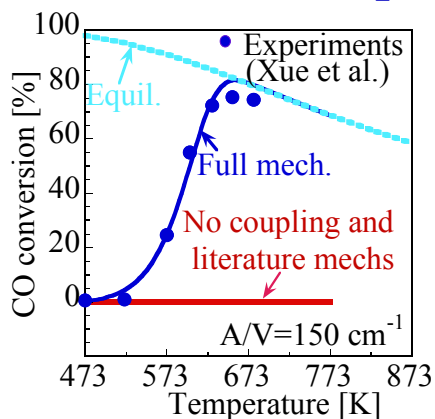


- Multifunctional devices provide **millisecond operation**
- Adjustment of flow rates can provide **variable power**
- Scaling out can supply transportation power levels

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## Water-gas shift reaction on Pt:

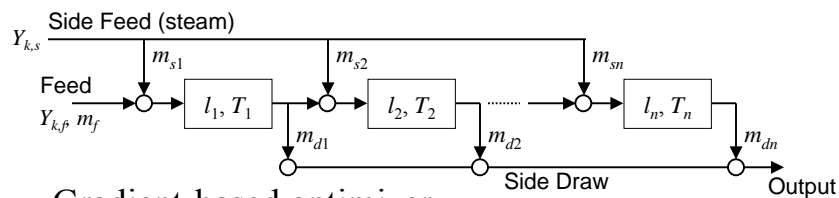


**Thermodynamics<sup>1</sup>** is important **but** not sufficient:  
**kinetics** ‘corrects’ the WGS speed

<sup>1</sup>Mhadeshwar et al., *J. Phys. Chem. B* (2003)

## Reactor Superstructure Optimization

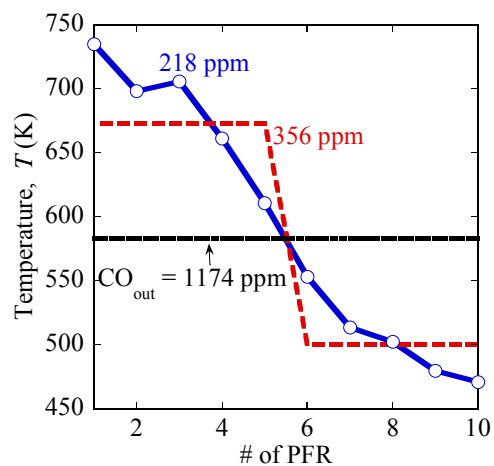
- Modeled as  $n$  PFRs in series
- Side feed and side draw from each reactor
- Each PFR: same length and different temperature



- Gradient-based optimizer

## Process optimization: Optimum temperature profile in the WGS reaction

- Total length:  $\sum_i l_i = 2 \text{ cm}$
- Inlet: 40 sccm feed (dry basis), with 18% CO
- Steam:  $\sum_i m_{s,i} \leq 40 \text{ sccm}$
- Temperature constraints:  $373 \text{ K} \leq T_i \leq 873 \text{ K}$
- All cases:
  - No split feed or side draw
  - All steam utilized
  - $T$  constraints were inactive



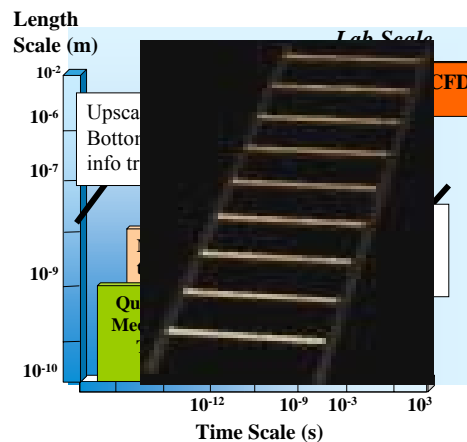
Vlachos et al., *Compt. Chem. Eng.* (2006)



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## The multiscale simulation paradigm: A bottom up and top-down ladder



- **Typical objective**
  - Mechanistic understanding
  - Reconcile large differences in published data
  - Process optimization:  
**Process engineering**

- **Opportunity**
  - Given a macroscopic behavior, design materials and/or control nanoscale
  - **Product engineering**

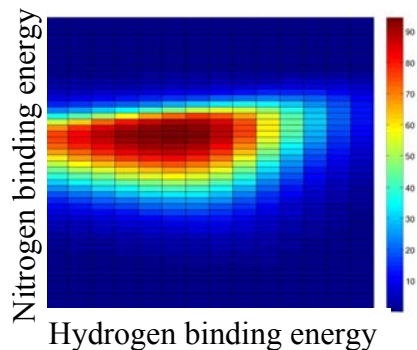
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Chatterjee et al., *Chem. Eng. Sci.*, *ISCRE Issue* (2004);  
Vlachos, *Adv. Chem. Eng.* **30**, 1 (2005)

## An example of catalyst optimization: NH<sub>3</sub> decomposition

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Ammonia conversion (%) at 380 °C



- Search is done on **atomic descriptors** while running the full chemistry model
- **Libraries of computational information** are created via DFT
- Models are built
- Potential catalyst candidates are identified

Ulissi et al.

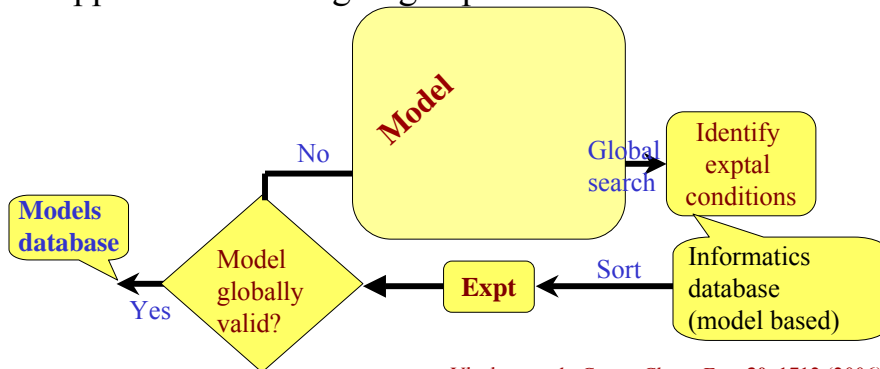
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## Maximizing information content of a model

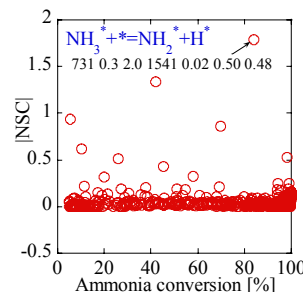
- Parameters are uncertain
- Often refined using statistically based experiments
- We need to bridge first-principles modeling with systems approaches in designing experiments



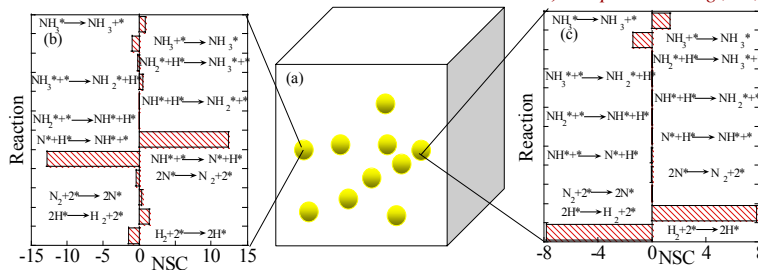
Vlachos *et al.*, *Comp. Chem. Eng.* **30**, 1712 (2006)

## Model-based design of experiments: Ensuring global accuracy of models

- Global Monte Carlo search in **exptl parameter space** ( $\tau$ , P, T, compos., A/V)
- Local sensitivity analysis
  - Only **a few model parameters are important** and can be **extracted, but change** in manipulated parameter space
- Sort by max NSC, RDS, MARI, ...

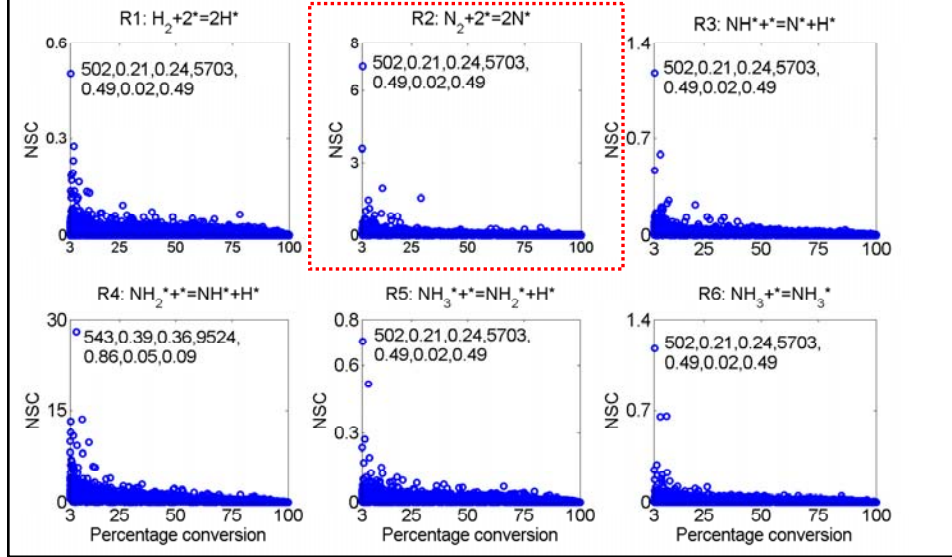


Vlachos *et al.*, *Comp. Chem. Eng.*, **30**, 1712 (2006)

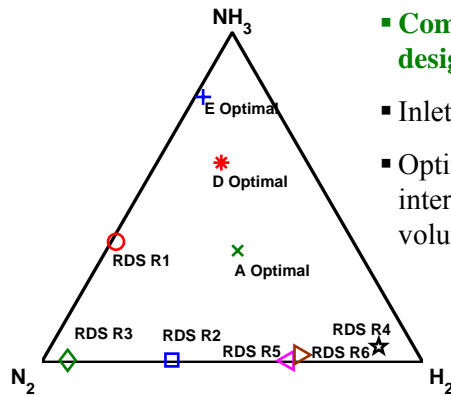


## Normalized parameter sensitivity vs. conversion (CSTR)

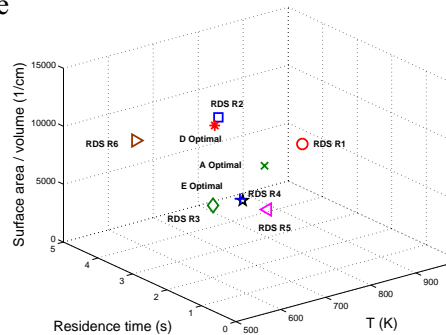
$\text{NH}_2^* + * = \text{NH}^* + \text{H}^*$  is the most sensitive reaction



## Optimal statistical and physics-aided designs

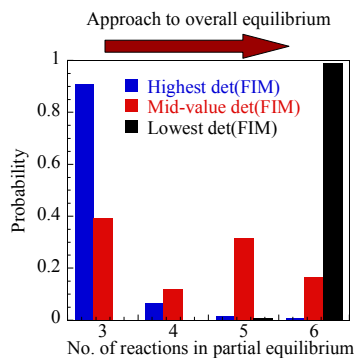


- Compared D, A, E and physics-aided designs
- Inlet composition space – no clear pattern
- Optimum at relatively low temperature, intermediate cat. surface area/reactor volume



Prasad and Vlachos, *Ind. Eng. Chem. Res.* (submitted)

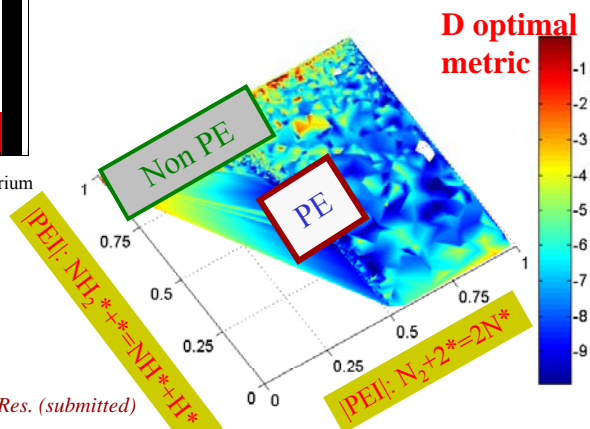
## Kinetic relevance – D Optimality and partial equilibrium (PE)



High values of the det. of the Fisher info matrix correlate with fewer reactions in PE and farther from equil.

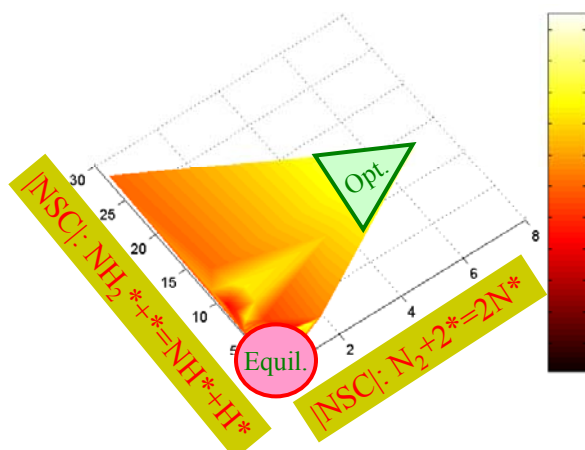
Partial equil. index:  
 $PEI = r_f / (r_f + r_b)$

Prasad and Vlachos, *Ind. Eng. Chem. Res.* (submitted)



## Kinetic relevance – D Optimality and sensitivity coefficients

D optimal metric



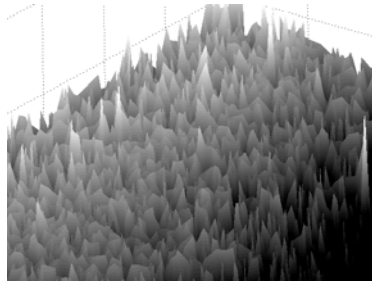
High values of the Fisher information matrix correlate with larger normalized sensitivity coefficients of the sensitive reactions

Prasad and Vlachos, *Ind. Eng. Chem. Res.* (submitted)

## Is a Single Optimal Point Good Enough?

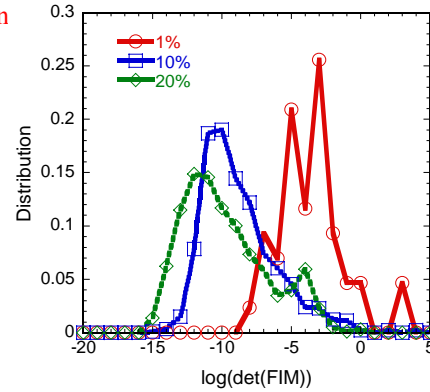
- The D optimal response surface is highly nonlinear
- You must be very close to the optimal point to ensure optimality
- Experimental constraints may make this unachievable

Representative cross-section of D optimal response surface

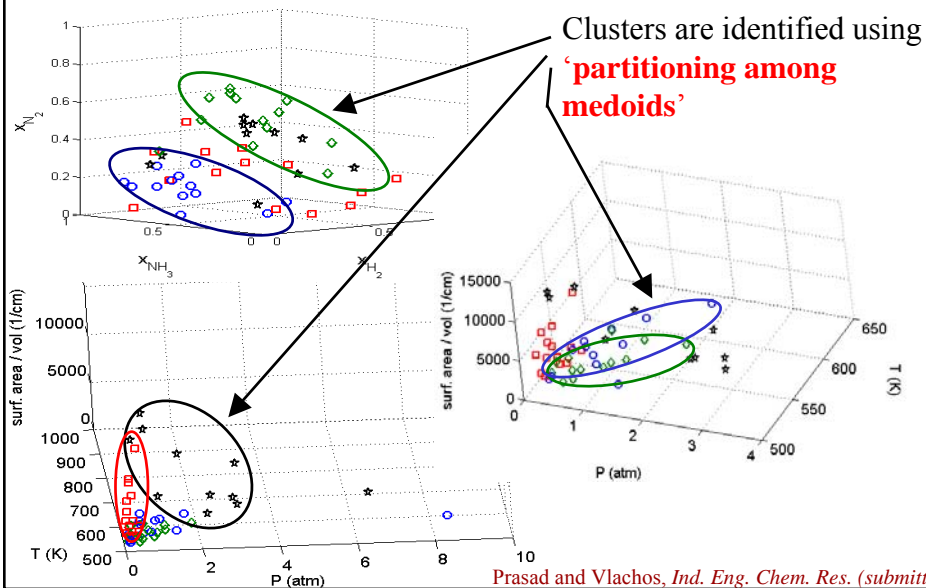


Prasad and Vlachos, *Ind. Eng. Chem. Res.* (submitted)

D optimal metric vs. distance from optimal point

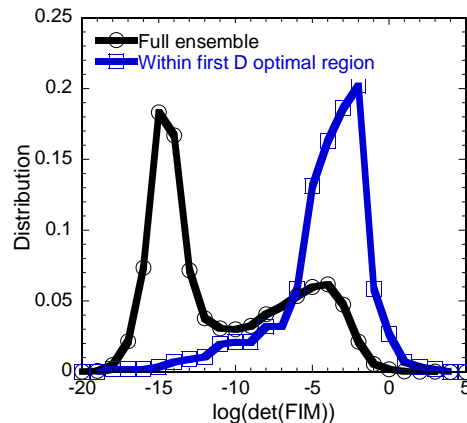


## Identifying regions (clusters) of D-optimal data using informatics tools



## Assessment of Informatics Approach

Distribution of D optimal metric within optimal region and in entire parameter space

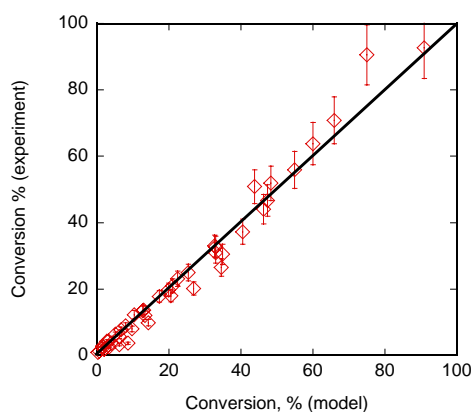


Sample anywhere within clusters (experimental flexibility)

Substantial improvement over single optimal points

Prasad and Vlachos

## Proof of concept via experiments



- 44 new experiments conducted in optimal region
- Varied
  - Temperature
  - Catalyst amount
  - Inlet composition
- Good agreement of model prediction and data

Karim, Prasad, and Vlachos (in preparation)

## Summary and future directions

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- Future energy generation will happen at much smaller scales
- Downscaling is different even at the <1 mm scale
  - ✓ Dynamics of microsystems, systems integration, optimization, and control
- **Hierarchical multiscale modeling**
- Application of multiscale modeling to
  - Microreactor and process design
    - ✓ Model reduction is essential
  - Experiment design
    - ✓ Informatics tools could be valuable to replace ‘the optimum’ point with an ensemble of suitably chosen experiments
  - Catalyst design
    - ✓ Reverse engineering of processes and products

## Acknowledgements

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- Funding: ARO, ARL, PRF, DOE, NSF, Rohm Haas, ConocoPhillips
- Students and postdocs
  - Dan Norton (GE;  $\mu$ burner modeling, fab, and exps)
  - Soumitra Deshmukh (Velocys;  $\text{NH}_3$  microreactors; system integration)
  - Ashish Mhadeshwar (GE; Multiscale chemistry)
  - Justin Federici (UD; Microreactor exps)
  - Marina Lebedeva (PennState; Model reduction)
  - Ben Feist (Air Liquide; HTE with Jochen Lauterbach)
  - Niket Kaisare (IIT Madras; Dynamics; Size optimization)
  - Vinay Prasad (visiting Prof. from IIT Bombay; DOEs)
  - Zack Ulissi (UD; Catalyst optimization)
  - Ayman Karim (UD;  $\text{NH}_3$  experiments)