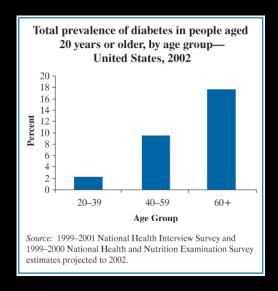
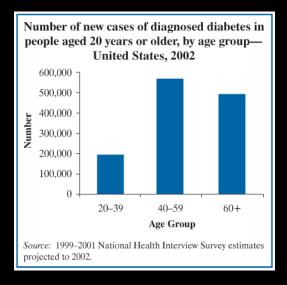


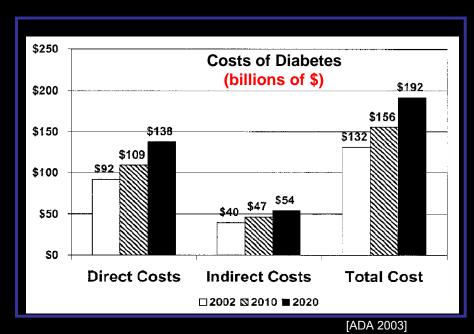
### Type 1 Diabetes Mellitus

- About one in every 400 to 600 children and adolescents has type 1 diabetes mellitus (T1DM)
  - National Diabetes Fact Sheet, 2005,
     Centers for Disease Control and Prevention
- Complications of T1DM reduce life expectancy by 20 years through micro- and macro-vascular disease
  - Heart disease and stroke
  - Blindness
  - Kidney disease
  - Nervous system disease
- Evidence that intensive insulin therapy (IIT) reduces complications
  - Diabetes Control and Complications Trial Research Group, 1993
- Increased hypoglycemic events with IIT
  - Diabetes Control and Complications Trial Research Group, 1993

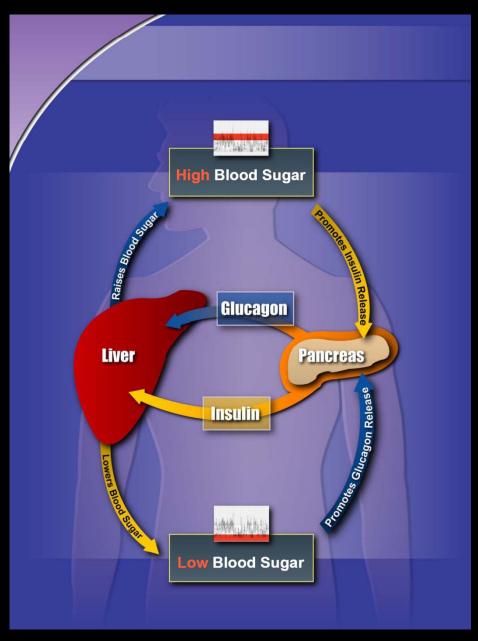
### The Cost of Diabetes

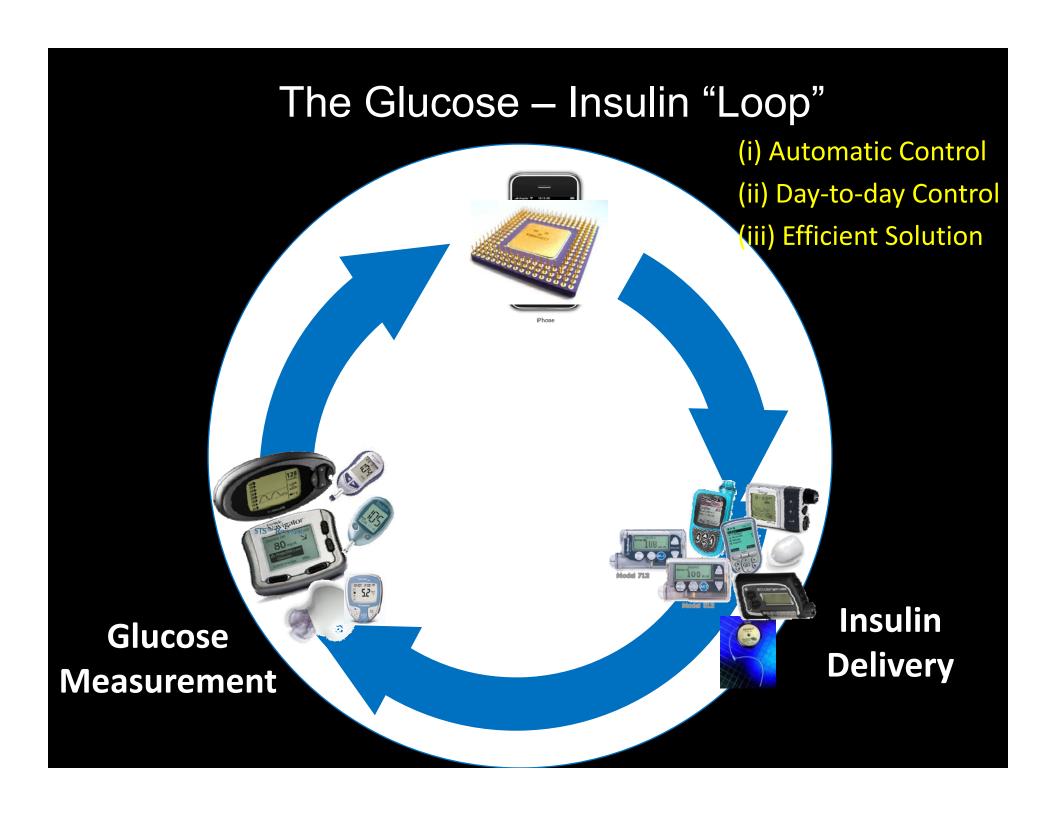






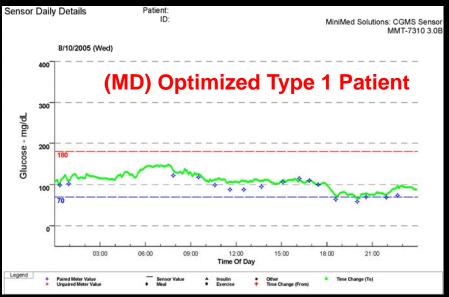
## Glucose Homeostasis

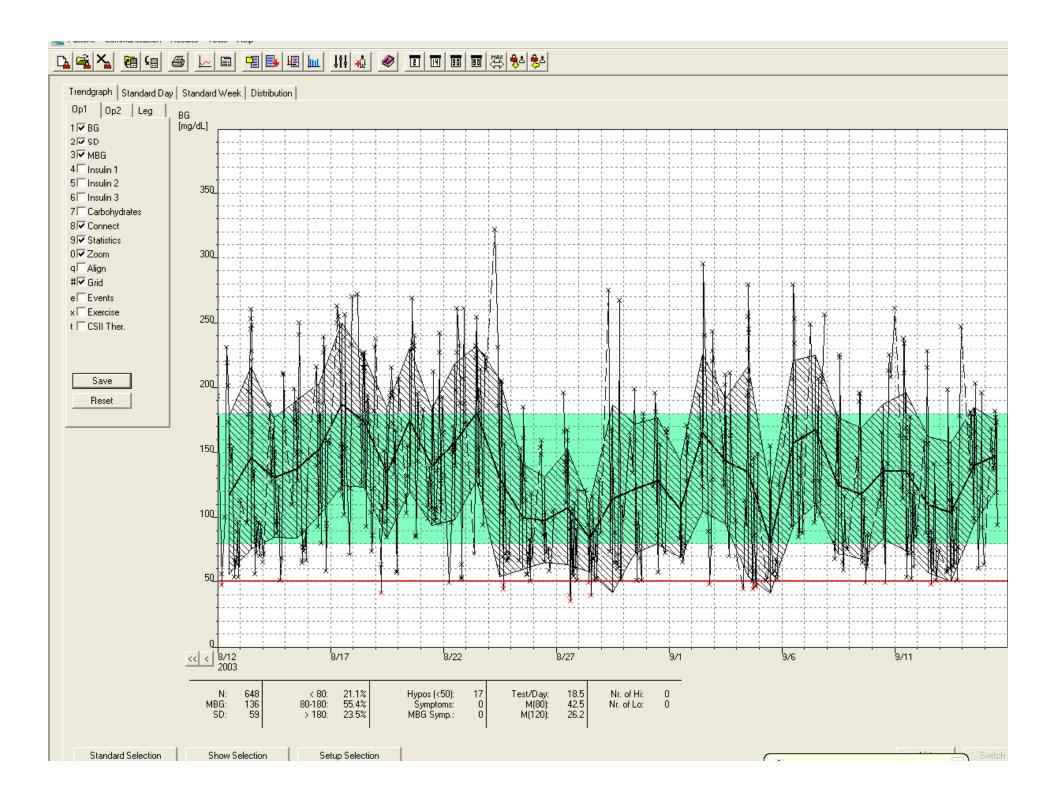




### Normalization of Glycemia







### UCSB/Sansum Approach

- Feedback control algorithm
  - Core insulin delivery algorithm

Ellingsen et al., 2009, J. Diabetes Sci. Tech.; Percival et al., submitted, 2009

- Hypoglycemia prediction
  - Alarms and pump shut-off Dassau et al., 2008, Diabetes
- Meal detection
  - Augment control algorithm

Dassau et al., 2008, Diabetes Care

- Iterative learning control
  - Account for intra-subject variations

Zisser et al., 2005 Diabetes Technol. Ther.; Wang et al., 2009, IEEE Trans Biomed Eng, 2009

- Hardware-in-the-loop trials
  - Testing communication protocols of off-the-shelf devices

Dassau et al., 2009, Diabetes Technol . Ther



## Glucose Sensing and Insulin Delivery

### Current State of the Art: Self-Monitoring Blood Glucose Meters (SMBG)











AWP = average wholesale price.

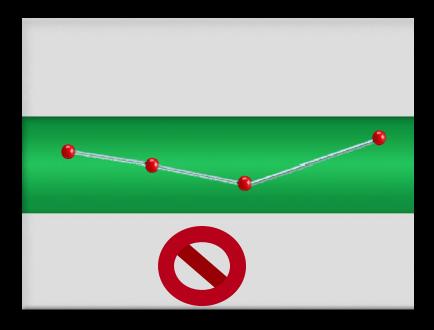
\* Standard list price. This monitor will not be manufactured after January 2006.

Data from Red Book®, 109th ed. Montvale, NJ: Thomson; 2005.39

[Graham, P&T, 2005]

### Benefits of Continuous Glucose Monitoring

#### **Standard Blood Glucose Monitoring**



### **Continuous Glucose Monitoring**



Source: Medtronic Diabetes modified by H. Zisser

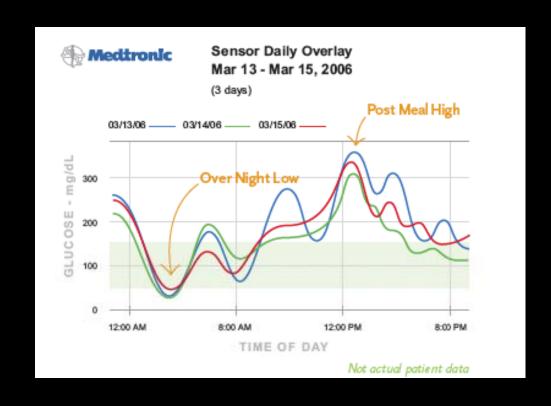
### Receiver for Sensor



### **Archival Data Analysis**



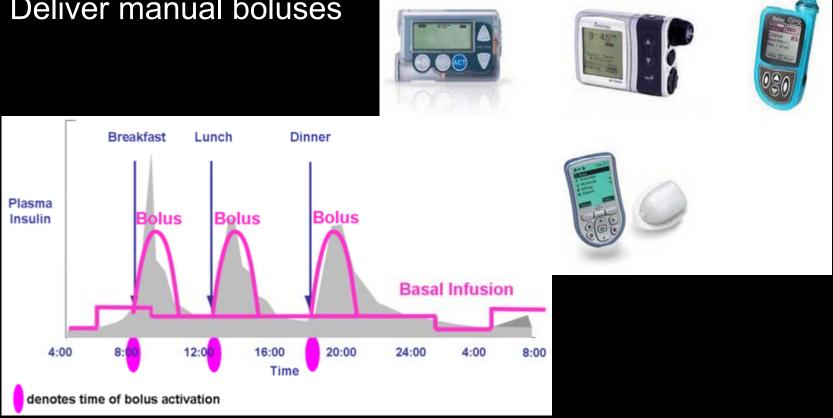




**Source: Medtronic Diabetes** 

### Continuous Subcutaneous Insulin Infusion (CSII)

- Patients can easily accommodate metabolic changes
- Set basal rate
- Deliver manual boluses



http://www.endotext.org/diabetes

# Opportunities for Process Systems Engineering:

**SMBG Systems** 

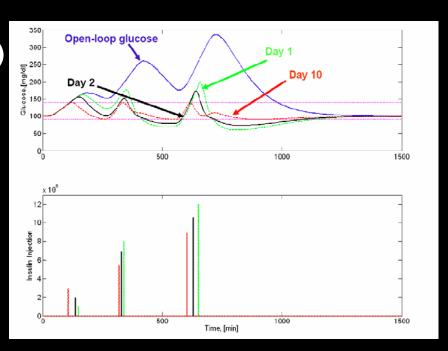
### Meal Bolus Dosing Analogy: Run-to-Run Control

[Doyle III et al., 2001; Zisser et al., 2005; Owens et al., 2006]

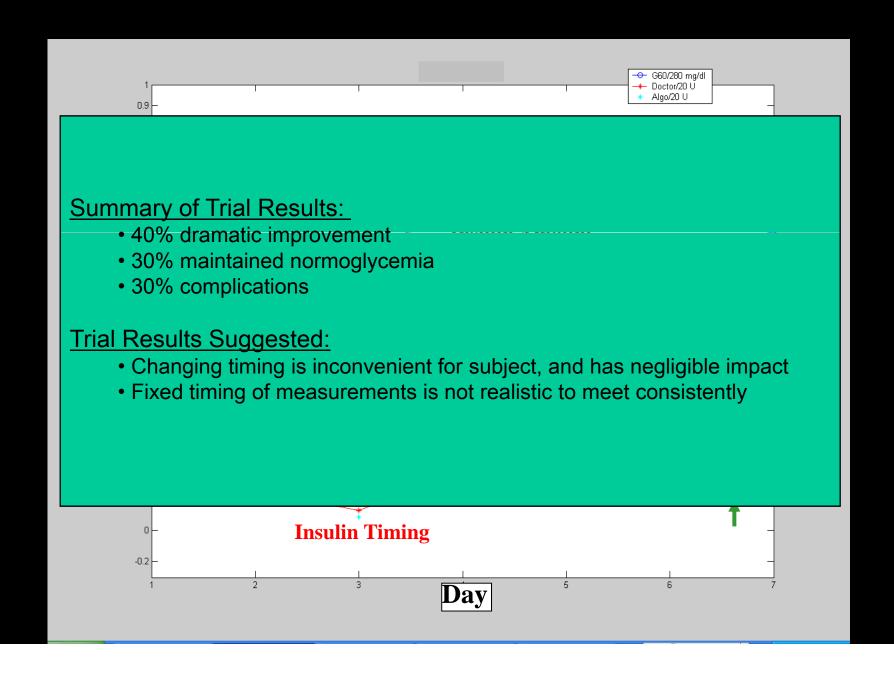
- Emerged from robotics and semiconductor processing problems where "repetition" is key
  - emphasis on measurement-based framework
  - batch-to-batch optimization ⇒ iteratively converge to optimal input profile in fewest number of (sub-optimal) runs
  - terminal constraints (end-conditions) are a critical element of the optimization problem
- Concept: Use meal cycle (run) to manage diabetes

$$T(k+1) = T(k) + K_T \min(0, G_{\text{max}}^r - G_{\text{max}}(k))$$

$$Q(k+1) = Q(k) + K_Q \max(0, G_{\min}^r - G_{\min}(k))$$



### Clinical Evaluation of Run-to-Run Control



### **Modified Algorithm**

$$\nu_{k+1} = \nu_k + K \left( \psi^r - \psi_k \right)$$

$$\psi_k = \begin{bmatrix} G(T_{B_1}) - G(T_{B_2}) \\ G(T_{L_1}) - G(T_{L_2}) \\ G(T_{D_1}) - G(T_{D_2}) \end{bmatrix}$$

rate of postprandial glucose rise

$$\nu_k = \begin{bmatrix} Q_B & Q_L & Q_D \end{bmatrix}^T$$

insulin meal bolus

- Only changing insulin dose, timing always fixed to the beginning of the meal
- Still require two post-meal measurements
  - First measurement 60-90 minutes after the start of the meal
  - Second measurement 30-60 minutes after the first
  - For each meal, denote these times as:
     T<sub>B1</sub>, T<sub>B2</sub>, T<sub>L1</sub>, T<sub>L2</sub>, T<sub>D1</sub>, T<sub>D2</sub>

$$e_{k+1} = \psi^r - \psi_{k+1}$$

$$= \psi^r - S\nu_{k+1}$$

$$= \psi^r - S(\nu_k + Ke_k)$$

$$= \psi^r - \psi_k - SKe_k$$

$$= (I - SK) e_k$$

$$e_{k+1} = (I - S(I + \Delta) K) e_k$$

### Specific uncertainties:

Measurement timing

$$\Delta = \text{diag} \begin{pmatrix} -0.064 & -0.070 & -0.119 \end{pmatrix}$$

Measurement noise

$$\Delta = \text{diag} \left( -0.236 \quad -0.382 \quad -0.260 \right)$$

Meal timing

$$\Delta = \text{diag} \begin{pmatrix} -0.194 & -0.450 & -0.473 \end{pmatrix}$$

Meal carbohydrate content

$$\Delta = \text{diag} \left( -0.281 \quad -0.496 \quad -0.414 \right)$$

Meal estimate

$$\Delta = \text{diag} \begin{pmatrix} -0.184 & -0.415 & -0.395 \end{pmatrix}$$

### Clinical Evaluation of New Algorithm

11 subjects with type 1 diabetes & CSII pumps

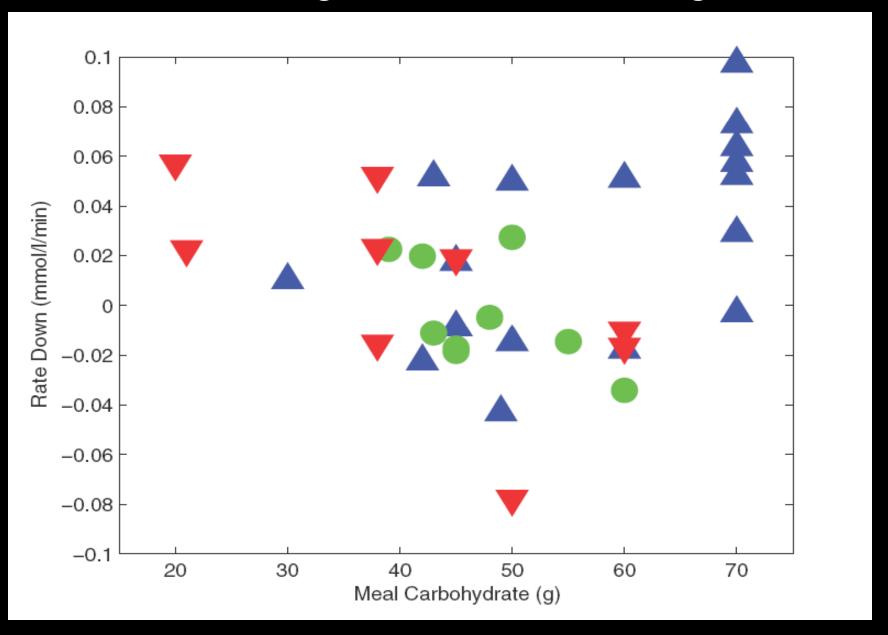
### Phase 1

- Optimized basal rates
- Brought out of control (1h post-prandial 170–200 mg/dl)
- Lunch only
- Carbohydrate content kept constant
- Algorithm adjusted dosing over 2 weeks

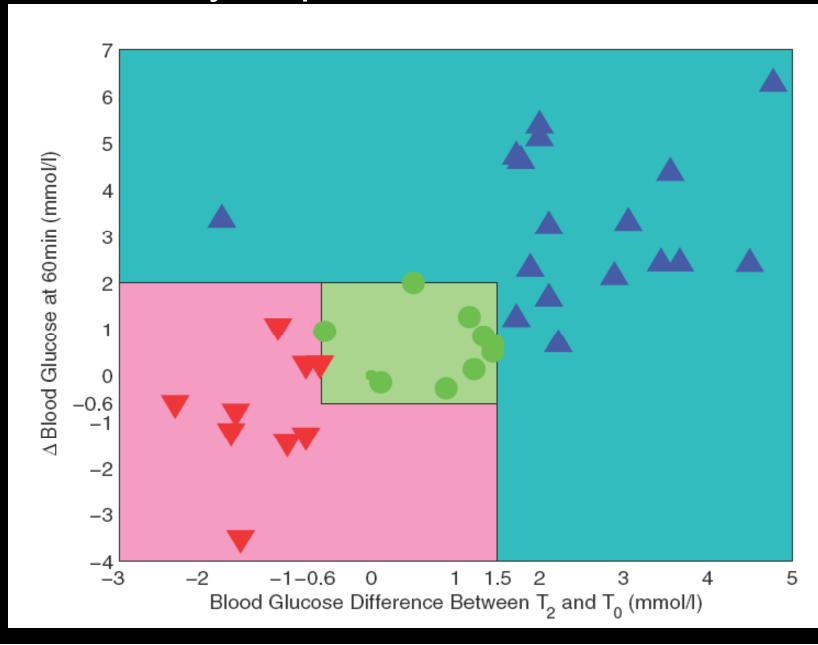
### Phase 2

- All three meals
- Carbohydrate content varied
- Algorithm adjusted dosing over 2–3 weeks

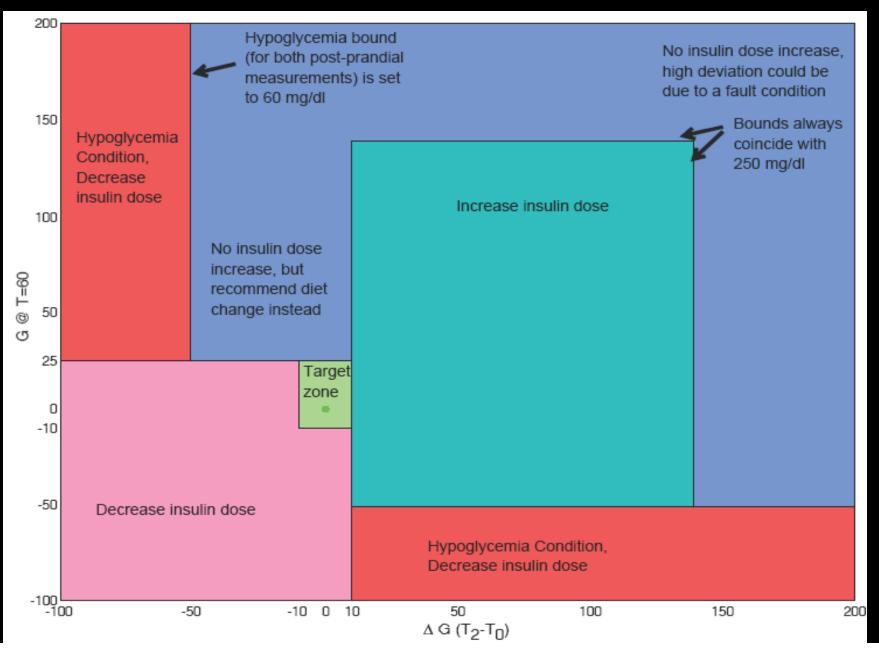
## Challenge in Data Clustering

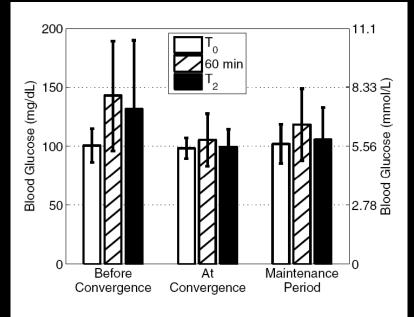


### Medically-Inspired Performance Measure

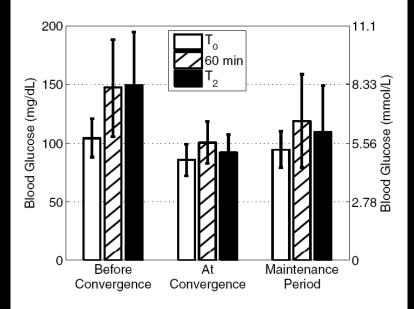


### Modifications for Phase 2



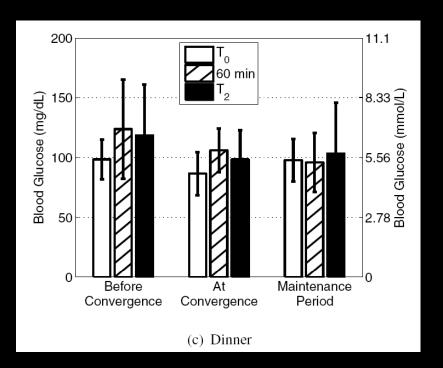






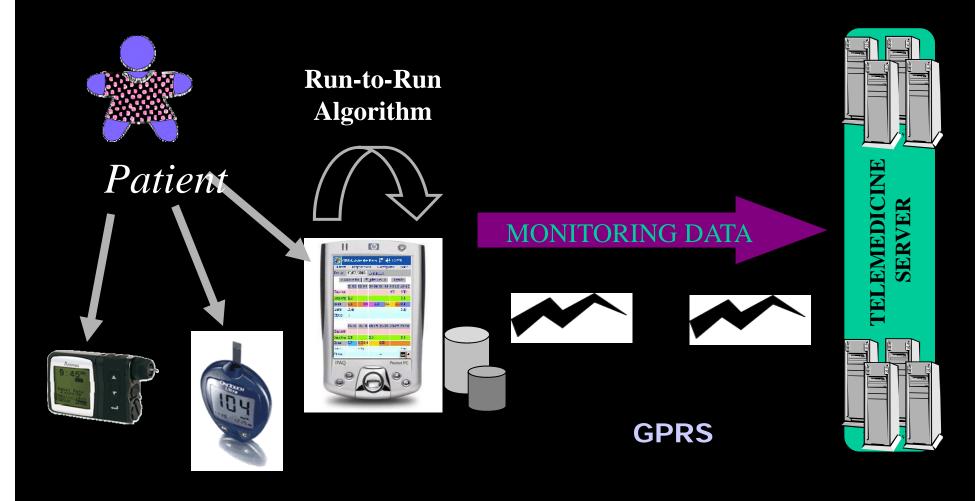
#### (b) Lunch

### Clinical Results



## Implementation of Run-to-Run Controller on PDA Platform

[Gema Garcia Saez and colleagues]

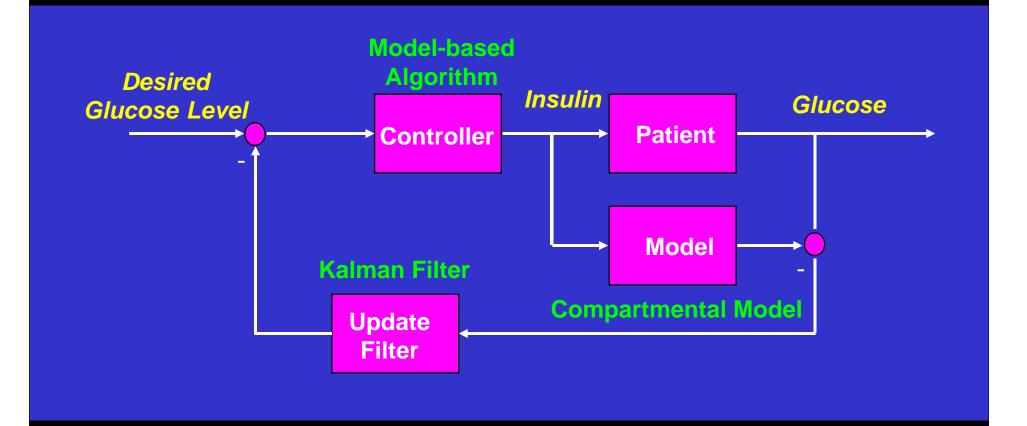


# Opportunities for Process Systems Engineering:

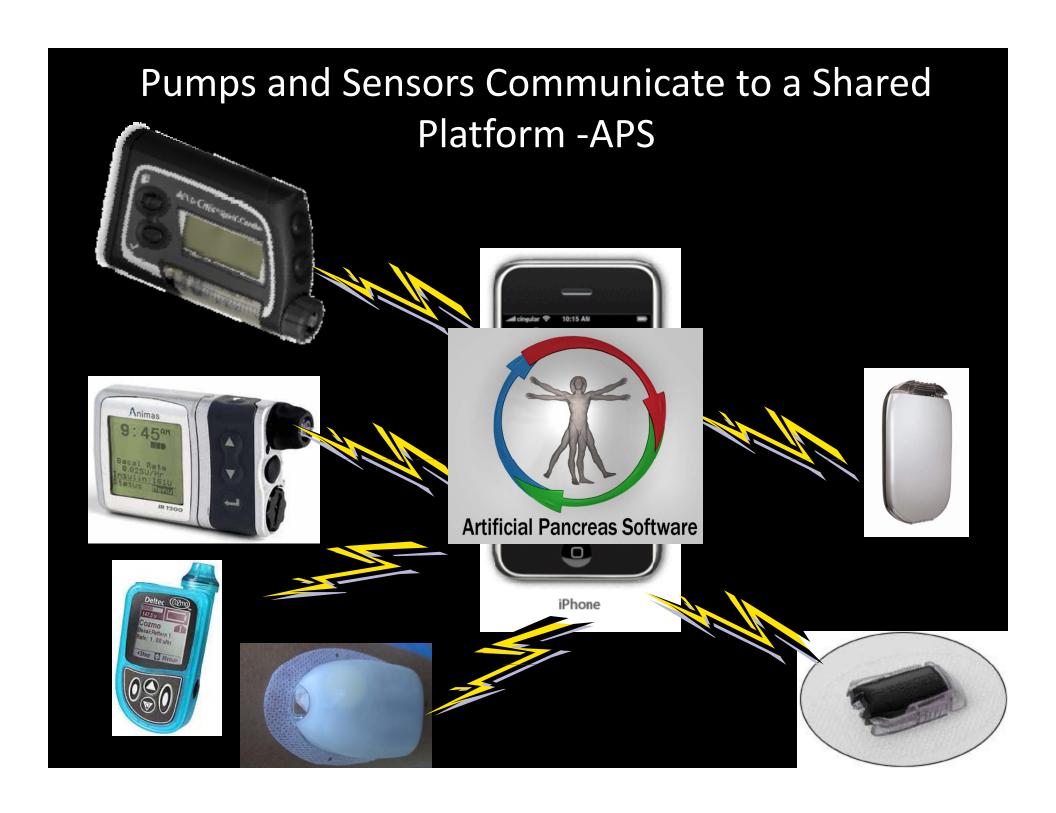
CGM Systems

### Model-Based Control Approach for Diabetes

[Parker, Doyle III, Peppas, IEEE Trans. Biomed. Eng., 1999]

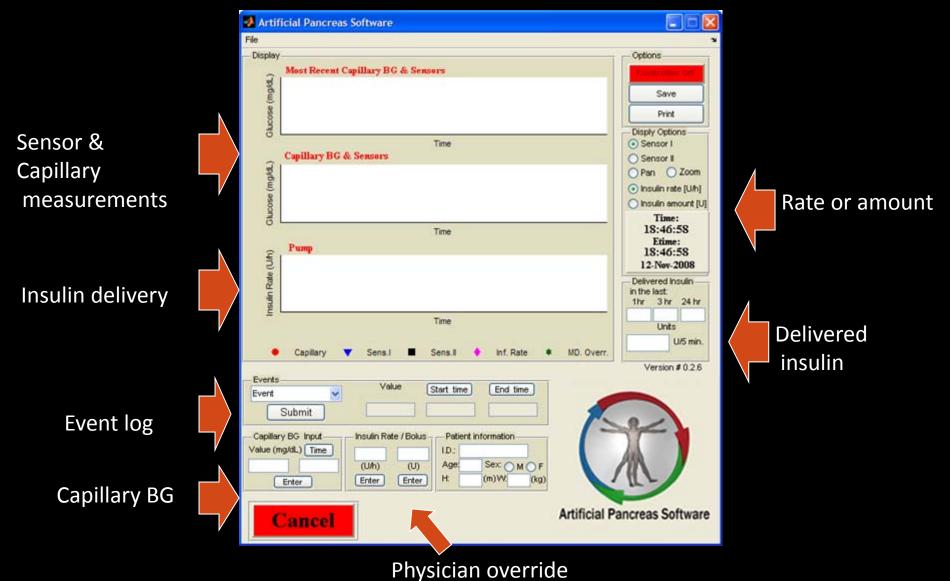


Key tenet of Robust Control Theory:
Achievable performance is directly tied to model accuracy



### Artificial Pancreas (β-cell) Software

### **Human Machine Interface**



### Hardware-in-the-Loop Testing

 A complete artificial β-cell system testing platform, allowing:

Systematic analysis

Component Verification and Validation

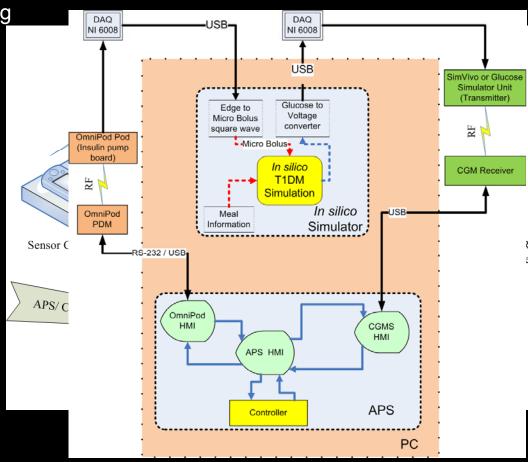
Complete system V&V

PnP for in silico patients

PnP for control algorithms

Realistic virtual clinical trial





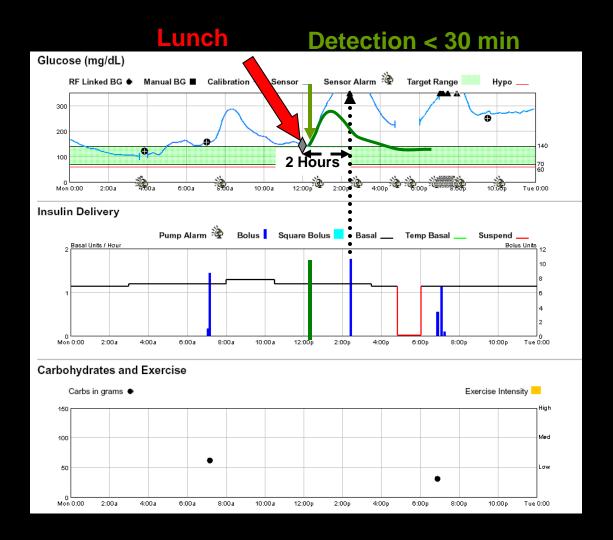
Dassau et al., 2007, 7th DTM, San Francisco CA, USA

Dassau *et al.*, 2008, "*In Silico* Evaluation Platform for Artificial Pancreatic β–Cell Development – a Dynamic Simulator for Closed-Loop Control with Hardware-in-the-Loop." *Diabetes Technol Ther.*, 2009

## Algorithm Engineering MPC for T1DM

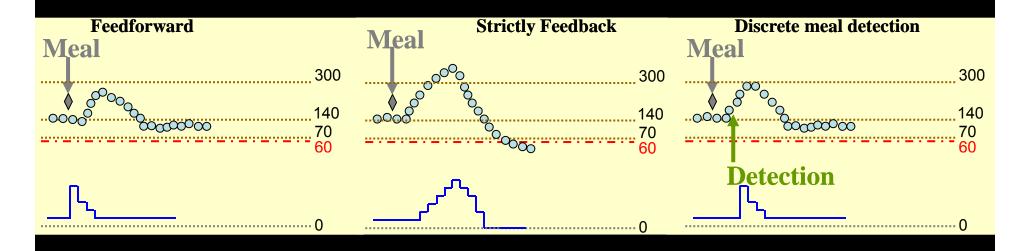
- Patient Model Identification
- Disturbance Estimation (i.e., meals)
- Programming Implementation (mpMPC)
- Safety Constraints (Insulin-on-Board)

### **Meal Detection**



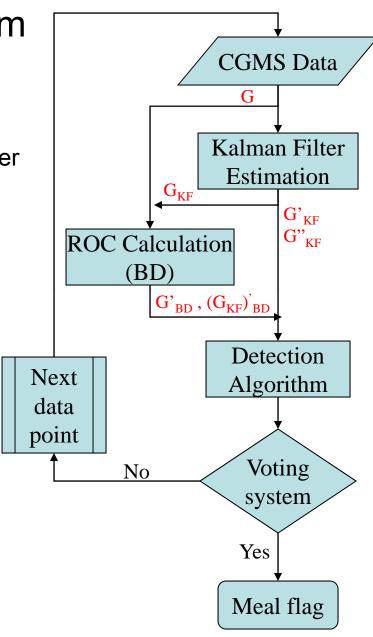
### Classes of Control Action for Meals

- Feedforward control
  - User intervention: clicking a button, thus initiating an insulin bolus
- Strictly feedback method
   Totally automated: the algorithm will respond only after a sufficiently large rise in glucose
- Discrete meal detection
   Safety net: this will trigger an insulin bolus as part of an algorithm using continuous feedback from a CGM



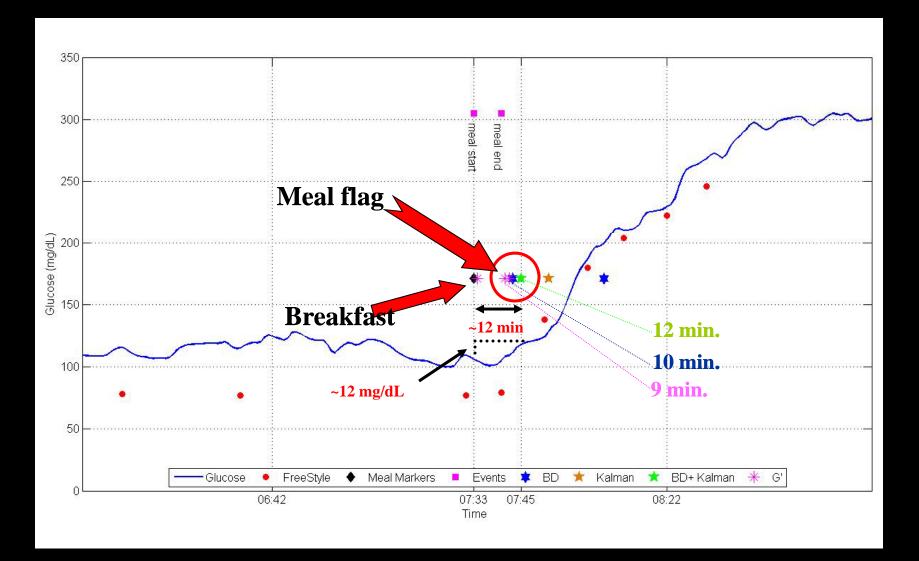
### Meal Detection – Voting Algorithm

- Data acquisition
- Algorithms:
  - Glucose profile estimation by Kalman Filter (KF), G<sub>KF</sub>
  - Glucose rate (velocity) estimation using Backward Difference G'<sub>BD</sub>& KF ,G'<sub>KF</sub>, (G<sub>KF</sub>)'<sub>BD</sub>
  - Glucose velocity rate (acceleration) estimation by KF, G"<sub>KF</sub>
- Detection procedure:
  - Satisfying threshold conditions
  - Heuristics
  - Tradeoff between speed of response and accuracy in flagging a meal
- Voting algorithm
  - Minimizing false detections
- Meal flag to the controller



[Dassau et al., Diabetes Care, 2008]

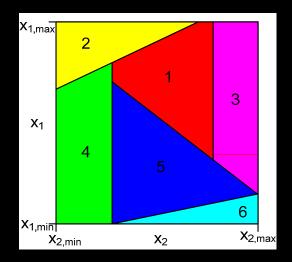
## Detection of a Single Meal

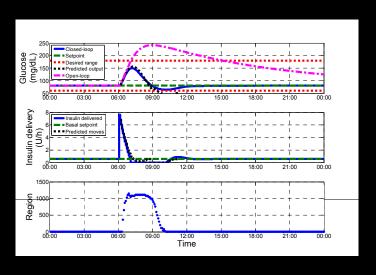


### Multi-Parametric Programming Implementation

[Percival et al., AIChE, 2008]

- Biomedical devices are subject to stringent FDA regulation
  - Restrictions on online optimization permissible
  - Prior risk analysis mandatory
- MPC is transformed into a multi-parametric program (mpMPC)
  - Offline optimization over state-space region of interest
    - · Lookup table of optimal control laws
  - Online optimization
    - Determine critical region in state-space
    - Evaluate an affine function of the state vector
- Simulated response to announced 60 g CHO meal
  - Bolus-style controller response
  - Hyperglycemia and hypoglycemia avoided
  - Euglycemia restored in under three hours
  - Variations in the state vector change the critical region used to evaluate the control law





### **Controller Derivation**

[Dua, Doyle III, Pistokopoulos, IEEE TBME, 2006]

$$\min_{U} J(U, x(t)) = x_{t+N_{y}|t}^{T} P x_{t+N_{y}|t}$$

$$+ \sum_{k=0}^{N_{y}-1} \left[ x_{t+k|t}^{T} Q x_{t+k|t} + u_{t+k}^{T} R u_{t+k} \right]$$

$$s.t. \ x_{\min} \le x_{t+k|t} \le x_{\max}, k = 1, \dots, N_{c}$$

$$u_{\min} \le u_{t+k} \le u_{\max}, k = 1, \dots, N_{c}$$

$$x_{t+k+1|t} = A x_{t+k|t} + B u_{t+k}, k \ge 0$$

$$u_{t+k} = K x_{t+k|t}, N_{u} \le k \le N_{y}$$



$$\min_{U} \frac{1}{2} U^T H U + x_t^T F U + \frac{1}{2} x_t^T Y x_t$$

$$s.t. GU \leq W + E x_t$$

$$V_z(x) = \min_{z} \frac{1}{2} z^T H z$$

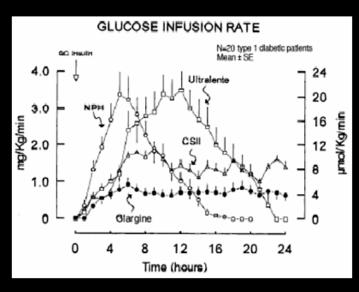
$$s.t. Gz \le W + Sx_t$$



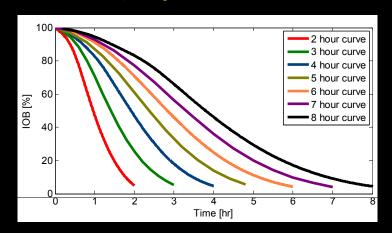
where  $z = U + H^{-1}F^Tx_t$ ,  $z \in R^s$ , and  $S = E + GH^{-1}F^T$ 

### Safety Constraints – Insulin on Board (IOB)

- Residual insulin (IOB) remains active for up to 8 hours
- Clinicians and bolus "wizards" factor in IOB
- Constraint formulation
  - Choose IOB curve
  - Calculate IOB
  - Allow insulin for correction
  - Allow insulin for meals
  - Constrain control algorithm



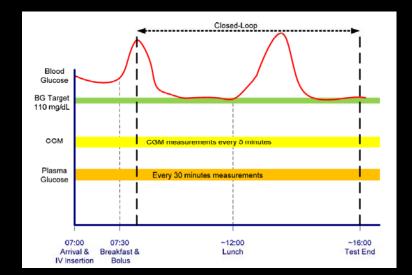
**Time–Action Profile Of Insulin Glargine Following Subcutaneous Injection.** Glycemic clamp study. [Taken from Lepore et al, *Diabetes* 49:2142–2148, 2000]



Walsh and Roberts, *Pumping Insulin*, 2006 Zisser et al., *Diabetes Technol Ther*, 2008 Ellingsen et al., *J Diabetes Sci Technol*, 2009

### Clinical Evaluation

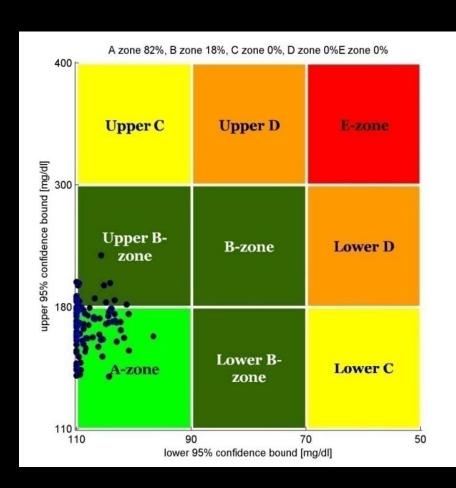
- FDA requirements
  - Investigational Device Exemption (IDE)
  - Detailed proof of safety of protocol/software
  - Master file already acknowledged for APS
- Phase I in silico trial
  - UVa-Padova simulation platform
  - 300 virtual subjects
  - Master file already acknowledged
  - Evaluate same clinical protocol

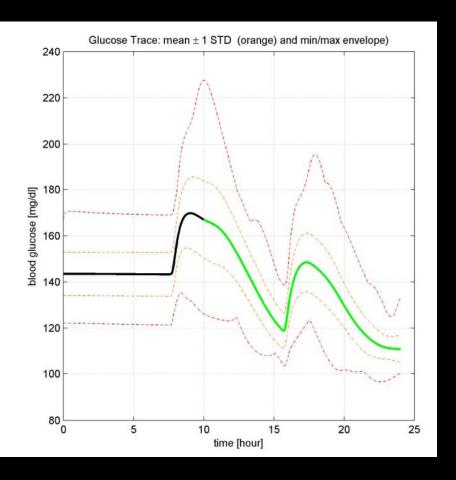


- Phase II human subject studies
  - Initial studies underway in Israel
  - Planned studies in Santa Barbara in late 2009
  - Large international trial (multi-site) planned for 2010

### In Silico Trial Results

[100 adult subjects]

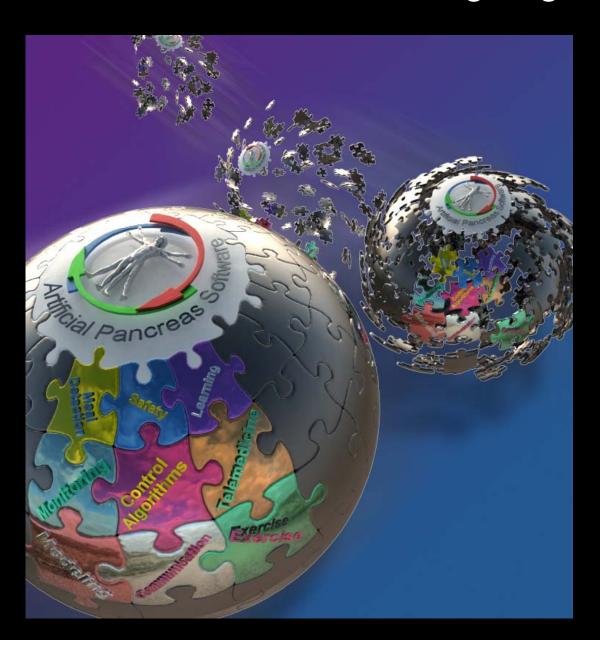




### **Clinical Trial Results**

[Schneider Children's Medical Center of Israel, Tel Aviv]

### Pieces of the Puzzle Are Coming Together



## Looking Towards the Future:

Safety Issues

Human Variability

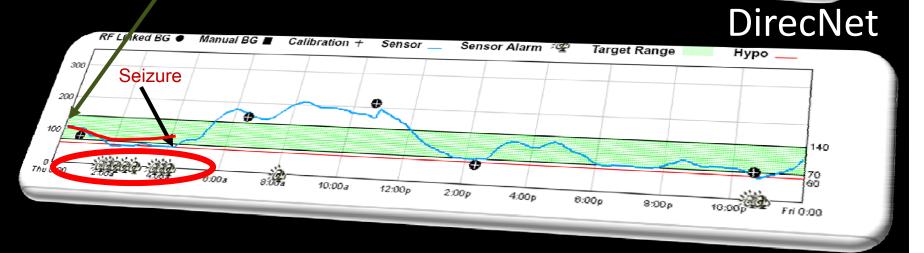
### Hypoglycemia Prediction

Intensive insulin therapy has an inherent risk of nocturnal hypoglycemia

- No response to any alarm
- Threshold alarms are insufficient

Prediction of pending hypoglycemic event & pump suspension





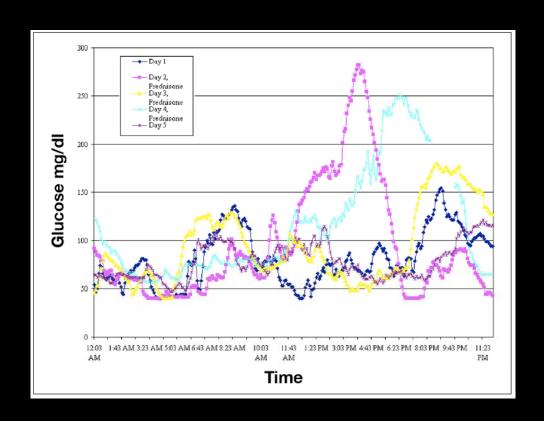
### Hypoglycemia Prediction System

[collaboration w/ Bruce Buckingham, Stanford Medical]

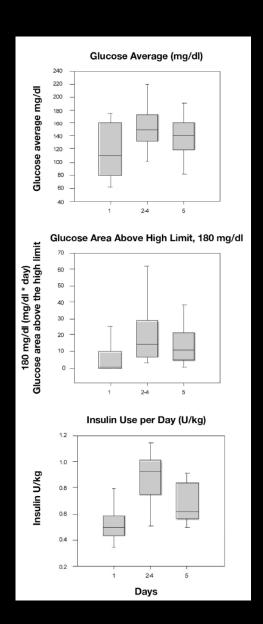
- A Hypoglycemia Prediction System (HPS) was developed using data derived from 21 Navigator studies which assessed Navigator function over 24 hours in children with Type 1 diabetes in clinical research centers (CRC)\*
- The HPS functionality was confirmed using a separate dataset from 22 CRC admissions of T1DM subjects
  - mean age = 20 years (range 6 -38)
  - hypoglycemia was induced by gradual increases in the basal insulin infusion rate by a mean of 180%
  - 18 of the 22 subjects (82%) reached a glucose value of ≤ 60 mg/dL

\*DirecNet, Diabetes Care

### Variability in the Human Body: Stress Effects



Clinical evaluation of the effect of Prednisone [Bevier, et al., 2007]

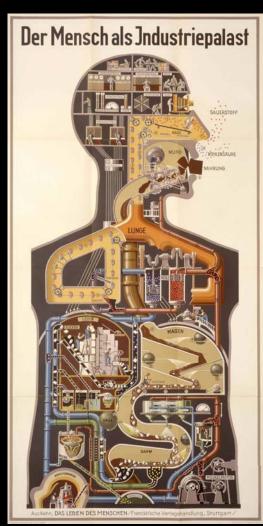


### Summary

Process systems engineering offers tremendous capability to

enable the artificial pancreas

- Promising technologies:
  - Run-to-run control
  - Model predictive control
  - Parametric programming implementation
- Many challenges still remain:
  - Patient model identification
  - Reliable (long-term) sensors
  - Transport and site issues
  - Patient variability (incl. stress, activity, etc.)
  - Regulatory issues



### Acknowledgments

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- Matt Percival
- Rachel Gillis [Eastman]
- Dr. Youqing Wang
- Rebecca Harvey
- Dr. Benyamin Grosman
- Christian Ellingsen



### **Collaborators:**

Lois Jovanovic (Sansum), Howard Zisser (Sansum), Dale Seborg (UCSB)





